HW 8 Math 261, F19

Please see the course syllabus for details on how to turn in your homework assignments. This one is due at the beginning of your class on **Friday**, **November 8**.

- 1. (5 pts.) True or False:
 - (a) Let R denote a plane region, and (u, v) = (u(x, y), v(x, y)) be a different set of coordinates for the Cartesian plane. Then for any function F(u, v)

$$\int_{R} F(u,v) du dv = \int_{R} F(u(x,y),v(x,y)) dx dy.$$

(b) Let R denote a plane region, and (u, v) = (u(x, y), v(x, y)) be a different set of coordinates for the Cartesian plane. Then

$$\int_{R} du dv = \int_{R} |u_{x}v_{y} - u_{y}v_{x}| dx dy$$

(c) Let R denote a square of sidelength 2 defined by the inequalities $|x| \le 1, |y| \le 1$, and (u, v) = (3y, 2x). Then the area of R is computed as

$$\int_{-2}^2 \int_{-3}^3 du dv.$$

(d) Let R denote a square of sidelength 2 defined by the inequalities $|x| \le 1, |y| \le 1$, and (u, v) = (3y, 2x). Then the area of R is computed as

$$\int_{-2}^{2} \int_{-3}^{3} (1/6) du dv.$$

(e) Let R denote a square of sidelength 2 defined by the inequalities $|x| \le 1, |y| \le 1$, and (u, v) = (3y, 2x). Then the area of R is computed as

$$\int_{-1}^{1} \int_{-1}^{1} (1/6) du dv.$$

- 2. (3 pts.) Using *cylindrical* coordinates, set up the integral to find the volume of the region enclosed by the vertical cylinder $x^2 + y^2 = 4$ and the planes z = 0 and y + z = 4. Do **NOT** evaluate the integral; just set it up.
- 3. (3 pts.) Using *spherical* coordinates, set up the integral to find the volume of the region enclosed by the vertical cylinder $x^2 + y^2 = 4$ and the planes z = 0 and z = 2. Do **NOT** evaluate the integral; just set it up.
- 4. (3 pts.) Use *cylindrical* coordinates and set up the integral to find the volume of the region enclosed by a circular cone of base radius 1 and height 2. Do **NOT** evaluate the integral; just set it up. Your set-up should include a description of how the cone is positioned in \mathbb{R}^3 .

- 5. (3 pts.) Consider using the substitution $\begin{cases} x = u v, \\ y = 2u + v \end{cases}$ for the integral of $x + y^2 2$. What is the *integrand* in terms of u and v? (Don't bother with the integral signs, the bounds, or the du dv.)
- 6. (3 pts.) Using the same substitution as in the previous problem, suppose the (x, y) region over which we wish to integrate includes the boundary line 2x y = 3. Convert this line into a (u, v) boundary line.