

## HW 4

### Math 261, F19

Please see the course syllabus for details on how to turn in your homework assignments. This one is due at the beginning of your class on **Friday, October 4**.

1. (5 pts.) TRUE OR FALSE

(a) Let  $x = 3, y = 4, z = 5t$ , and  $f(x, y, z)$  be a function from  $\mathbb{R}^3$  to  $\mathbb{R}$ . Then  $\frac{\partial f}{\partial t} = \frac{\partial f}{\partial z}$ .

(b) Let  $x = 3, y = 4, z = 5t$ , and  $f(x, y, z)$  be a function from  $\mathbb{R}^3$  to  $\mathbb{R}$ . Then  $\frac{\partial f}{\partial t} = 5 \frac{\partial f}{\partial z}$ .

(c) Let  $x = 3, y = 4, z = 5t$ , and  $f(x, y, z)$  be a function from  $\mathbb{R}^3$  to  $\mathbb{R}$ . Then  $\frac{\partial f}{\partial t} = 1/5 \frac{\partial f}{\partial z}$ .

(d) Let  $h(x, y)$  be a function from  $\mathbb{R}^2$  to  $\mathbb{R}$  and  $P$  a point in the domain of  $h$ . It is possible that the directional derivative of  $h$  at  $P$  is equal to 1 for every direction vector.

(e) Let  $h(x, y)$  be a function from  $\mathbb{R}^2$  to  $\mathbb{R}$  and  $P$  a point in the domain of  $h$ . It is possible that the directional derivative of  $h$  at  $P$  is equal to 0 for every direction vector.

2. (3 pts.) Suppose function  $f(x, y)$  depends on variables  $x$  and  $y$ , which are themselves functions of variables  $\alpha, \beta$ , and  $\gamma$  (i.e.,  $x = x(\alpha, \beta, \gamma)$  and  $y = y(\alpha, \beta, \gamma)$ ). Fill in the blanks for the chain rule to compute  $\frac{\partial f}{\partial \beta}$ :

$$\frac{\partial f}{\partial \beta} = \frac{\partial \square}{\partial \square} \frac{\partial \square}{\partial \square} + \frac{\partial \square}{\partial \square} \frac{\partial \square}{\partial \square}$$

3. (3 pts.) Let

$$g(u, v) = u^2 + v^3,$$

$$u(t) = \cos(t),$$

$$v(t) = \ln(t).$$

Compute  $\frac{dg}{dt}$ . (Please use only the variable  $t$  in your response, but do not bother multiplying everything out.)

4. (3 pts.) Suppose  $z$  is a function of  $x$  and  $y$  and that  $x^2 z^2 + y \sin(z) = 1$ . Find  $\frac{\partial z}{\partial x}$ .

5. (3 pts.) Find the derivative of  $f(x, y) = xy - y^2$  at point  $(1, 2)$  in the direction of  $\mathbf{v} = \langle 3, 4 \rangle$ . Please simplify your answer to a number. (Notice that  $\mathbf{v}$  is not a unit vector!)
6. (3 pts.) Find a direction vector  $\mathbf{v}$  such that the derivative of  $f(x, y) = xy - y^2$  at point  $(1, 2)$  in the direction of  $\mathbf{v}$  is equal to 0.