

# Electrical Impedance Tomography

David Isaacson

Jonathan Newell

Gary Saulnier

RPI

**Part 1.**

**Adaptive Current Tomography  
and Eigenvalues**

With help from

D.G.Gisser, M.Cheney, E. Somersalo,  
J.Mueller, S.Siltanen

and

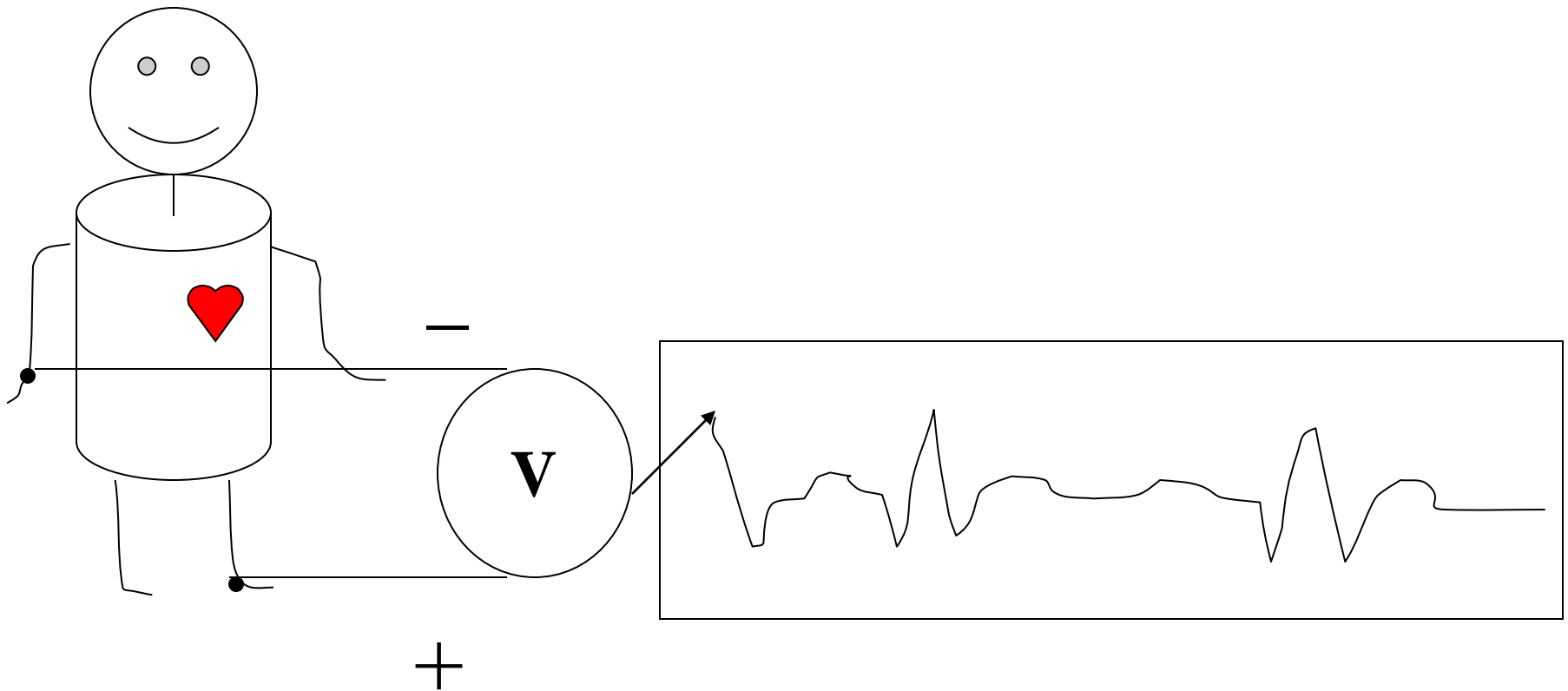
Denise Angwin, B.S. Greg Metzger, B.S. Hiro Sekiya, B.S. Steve  
Simske, M.S. Kuo-Sheng Cheng, M.S. Luiz Felipe Fuks, Ph.D.  
Adam Stewart Andrew Ng, B.S. Frederick Wicklin, M.S. Scott  
Beaupre, B.S. Andrew Kalukin, B.S. Tony Chan, B.S. Matt  
Uyttendaele, M.S. Steve Renner, M.S. Laurie Christian, B.S.  
Van Frangopoulos, M.S. Tim Gallagher, B.S. Lewis Leung, B.S.  
Jeff Amundson, B.S. Kathleen Daube, B.S. Candace Meindl  
Matt Fisher Audrey Dima, M.Eng. Skip Lentz Nelson Sanchez,  
M.S. Clark Hochgraf John Manchester Erkki Somersalo, Ph.D.  
Hung Chung Molly Hislop Steve Vaughan Joyce Aycock  
Laurie Carlyle, M.S. Paul Anderson, M.S. John Goble, Ph.D.  
Dan Kacher Chris Newton, M.S. Brian Gery Qi Li Ray  
Cook, Ph.D. Paul Casalmir Dan Zeitz, B.S. Kris Kusche, M.S.  
Carlos Soledade, B.S. Daneen Frazier Leah Platenik Xiaodan  
Ren, M.S. David Ng, Ph. D. Brendan Doerstling, Ph.D. Mike  
Danyleiko, B.S. Cathy Caldwell, Ph.D. Nasriah Zakaria Peter M.  
Edic, Ph. D. Bhuvanesh Abrol Julie Andreasson, B.S. Jim  
Kennedy, B.S. Trisha Hayes, B.S. Seema Katakkar Yi Peng  
Elias Jonsson, Ph. D. Pat Tirino M.S. Hemant Jain, Ph. D.  
Rusty Blue, Ph. D. Julie Larson-Wiseman, Ph. D.

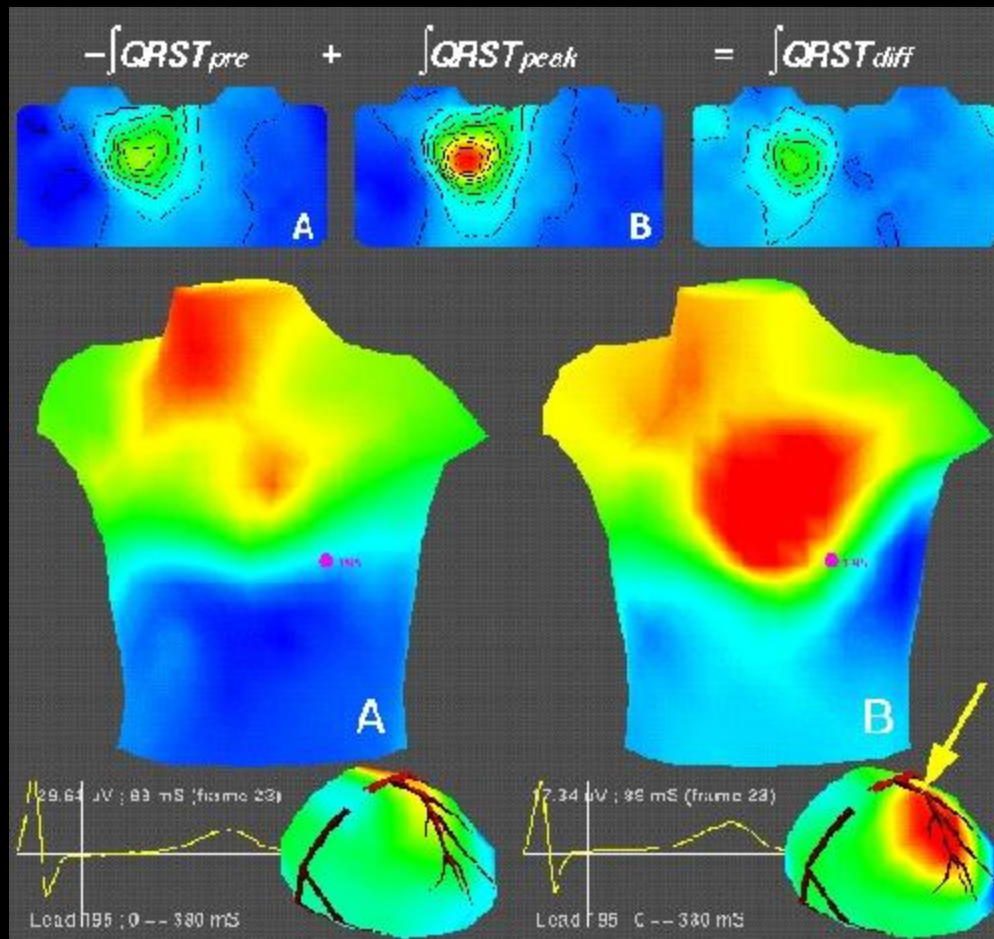
# **Main Problem!**

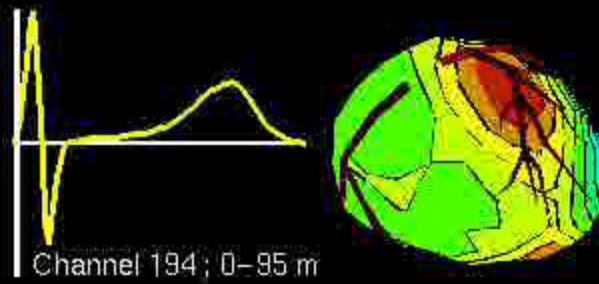
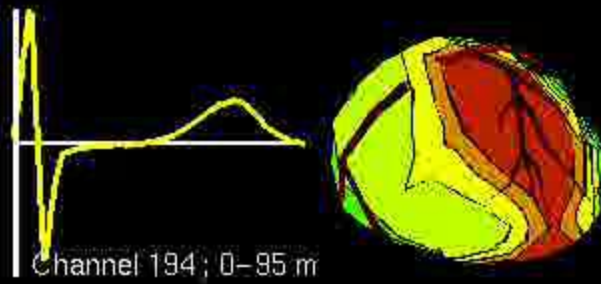
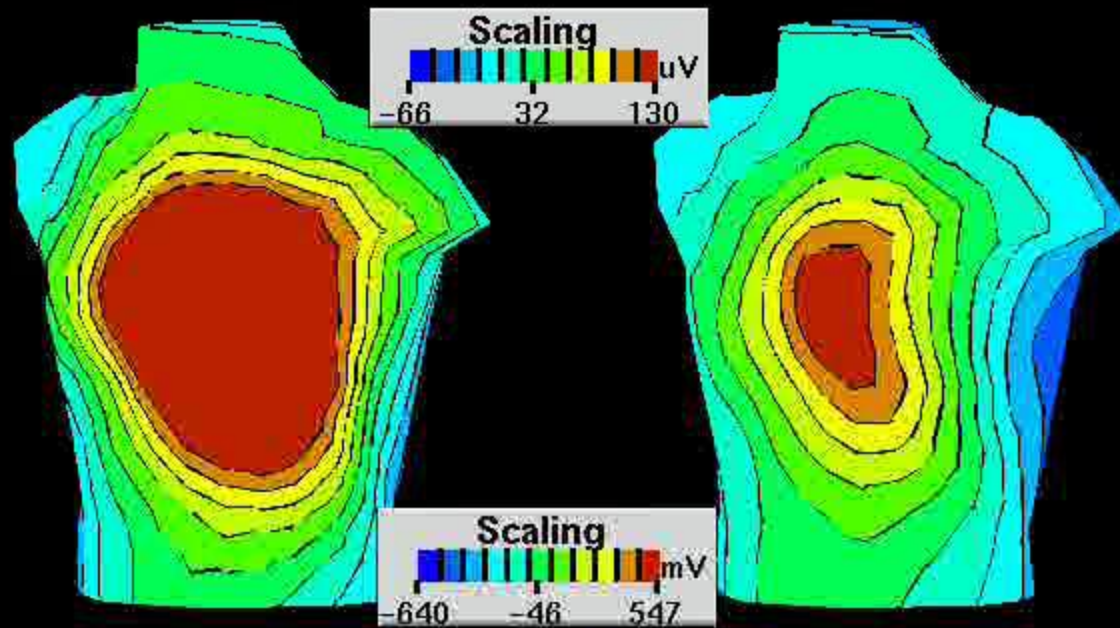
**Can we improve the Diagnosis  
and Treatment of Disease,  
especially Heart Disease and  
Breast Cancer with  
Electromagnetic Fields?**

# Example of E&M for Diagnosis

## EKG



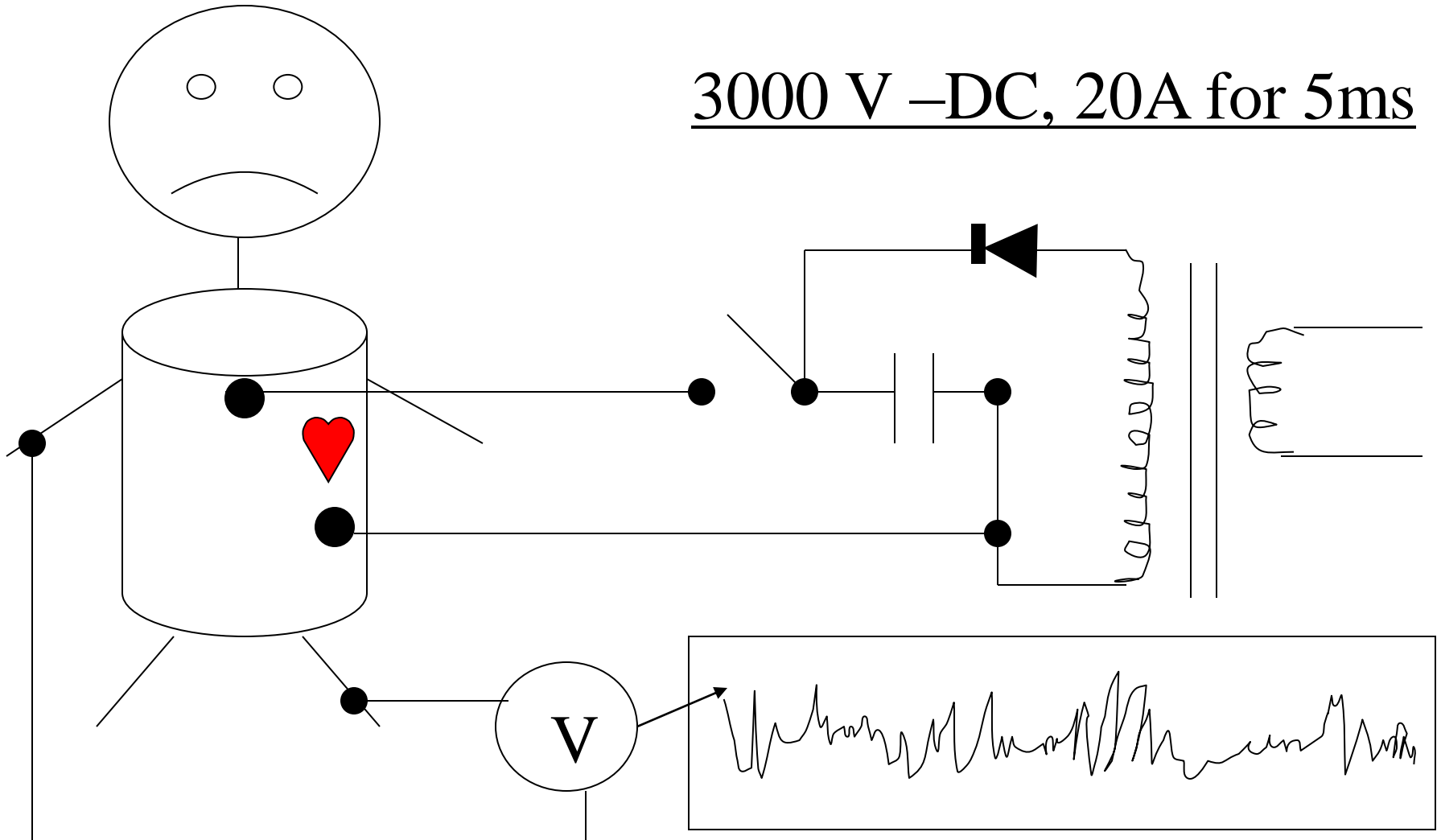






# Example of E&M for Treatment- Defibrillation!

3000 V –DC, 20A for 5ms



# **Impedance Imaging Problem;**

**How can one make clinically  
useful images of the electrical  
conductivity and permittivity  
inside a body from  
measurements on a body's  
surface?**

# Potential Applications

## I. Continuous Real Time Monitoring of Function of:

1. **Heart**
2. **Lung**
3. Brain
4. Stomach
5. Temperature

## II. Screening:

1. **Breast Cancer**
2. Prostate Cancer

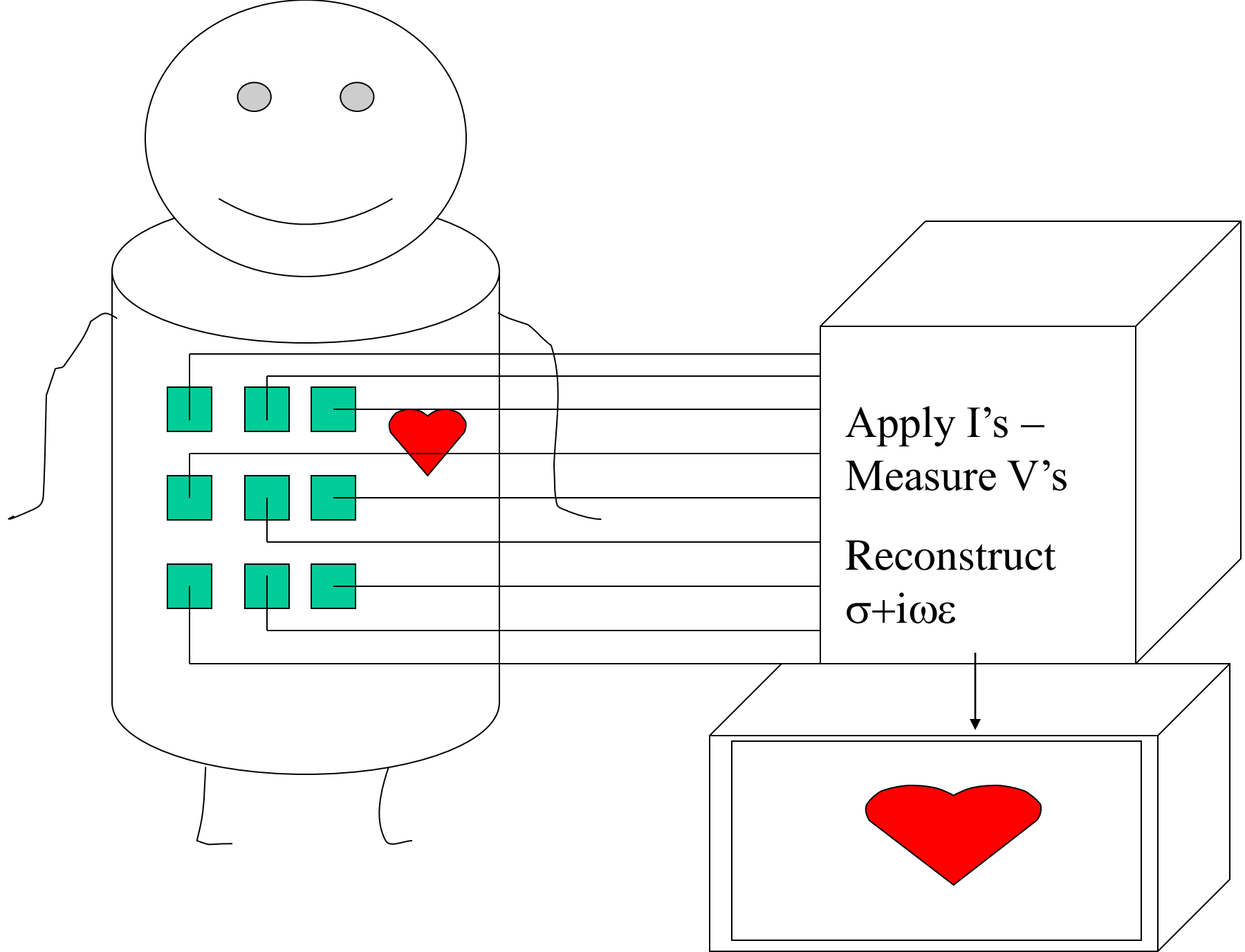
## III. Electrophysiological Data for Inverse problems in:

1. **EKG**
2. EEG
3. EMG

# Reasons

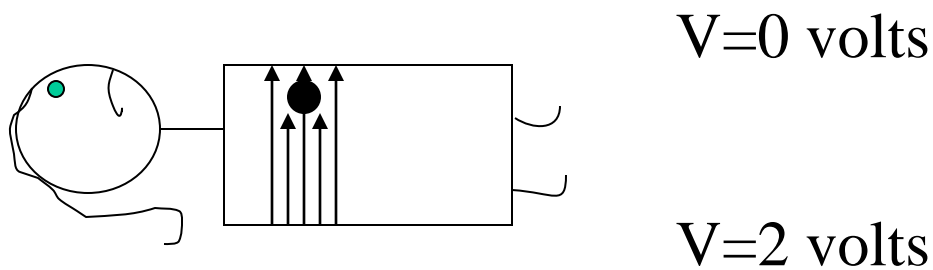
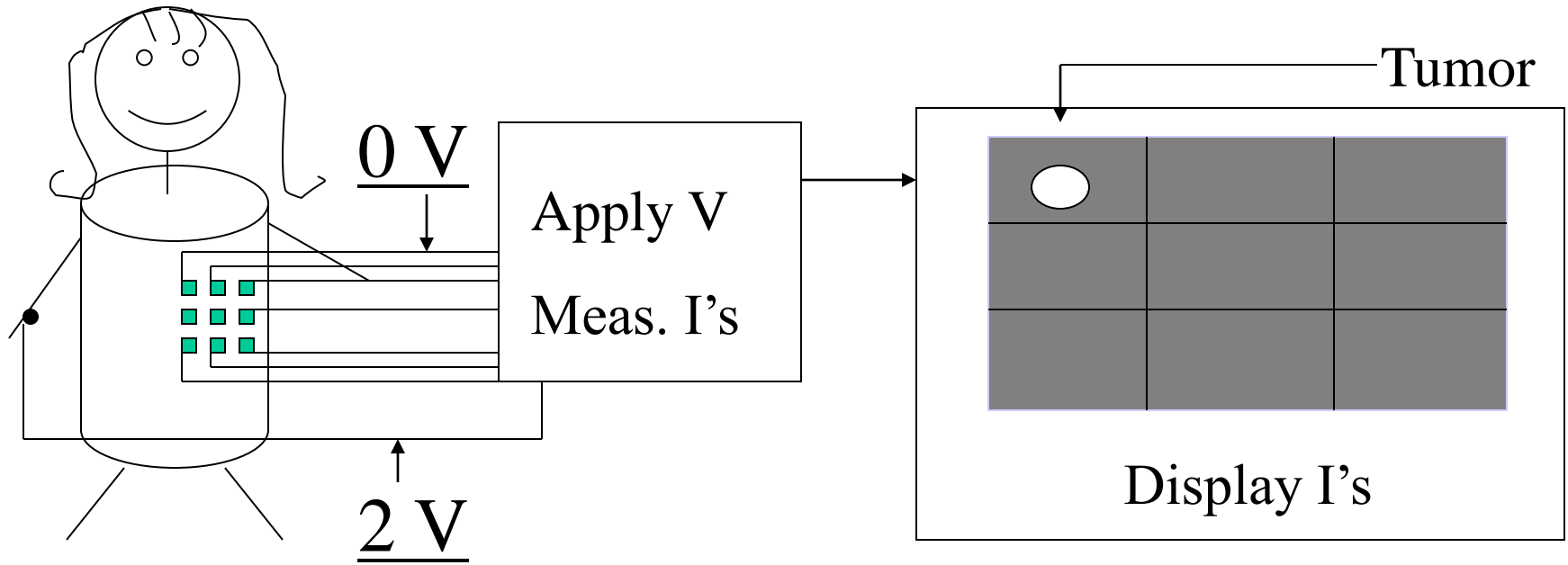
<u>TISSUE</u>	<u>Conductivity</u> S/M	<u>Resistivity</u> Ohm-Cm
Blood	.67	150
Cardiac Muscle	.2	500
Lung	.05	2000
Normal Breast	.03	3000
Breast Carcinoma	.2	500

Procedure  
For Imaging Heart and Lung  
Function in 3D  
Electrical Impedance  
Tomography



Procedure used by T-Scan for  
Electrical Impedance  
Mammography

# T-Scan = Only Commercial System



Current I's in ma.



Is it useful?  
Test by blinded Trials!

$$\text{Sensitivity} = \frac{\text{\# predicted to have cancer}}{\text{Total \# that have cancer}}$$

$$\text{Specificity} = \frac{\text{\# predicted NOT to have cancer}}{\text{Total \# that do NOT have cancer}}$$

X 100

**Table 5: Results for Equivocal Mammograms (N=273)**

	<b>Mamm. alone</b>	<b>T-Scan Adjunctive</b>	<b>McNemar p-value (Mamm vs. djunctive)</b>
<b>Sensitivity (Biopsy pos.=50)</b>	60%	82%	0.02
<b>Specificity (Biopsy neg.=223)</b>	41%	57%	0.0003

How can one increase the sensitivity and specificity?

Increase Resolution?

# What determines “resolution”?

FIRST LIMIT IS THE NUMBER OF  
ELECTRODES

because

# Degrees of freedom (voxels)

reconstructed  $< L(L-1)/2$

Where  $L = \#$  of Electrodes

How to get Higher Resolution?

Let  $L \rightarrow \infty$

# Problem

## Theorem

**The ability to “distinguish”  
different conductivity distributions  
 $\rightarrow 0$  as  $L \rightarrow \infty$  for fixed # of I gen’s.**



# Solve the Problems:

1. Should we apply currents or voltages?
2. Can we distinguish  $\sigma$  from  $\tau$ ?
3. Which patterns of currents or voltages should we apply?
4. How many electrodes?
5. What size electrodes?
6. How can we reconstruct useful images?

How do we solve these  
problems?

Use **Mathematics**

and

**Electromagnetic** theory

to design system to reconstruct  
and display conductivity inside  
the body in 3D

What are the Equations?

# Maxwell's

$$\nabla \wedge H = J + \partial D / \partial t$$

$$\nabla \wedge E = -\partial B / \partial t$$

$$\nabla \bullet D = \rho$$

$$\nabla \bullet B = 0$$

## Assume

$$E(x, t) = E(x) e^{i\omega t}, H(x, t) = H(x) e^{i\omega t}$$

$$D(x, t) = D(x) e^{i\omega t}, B(x, t) = B(x) e^{i\omega t}$$

$$J(x, t) = J(x) e^{i\omega t}$$

# Constitutive Relations

$$D = \varepsilon E$$

$$B = \mu H$$

$$J = \sigma E$$

Thus

$$\nabla \wedge H = (\sigma + i\omega \varepsilon)E$$

$$\nabla \wedge E = -i\omega \mu H$$





$$\nabla \cdot \nabla \wedge H = \nabla \cdot (\sigma + i\omega \varepsilon) E = 0$$

$$\nabla \wedge E = -i\omega \mu H$$

Assume  $\omega = 0$



$$\nabla \cdot \sigma E = 0$$

$$\nabla \wedge E = 0$$

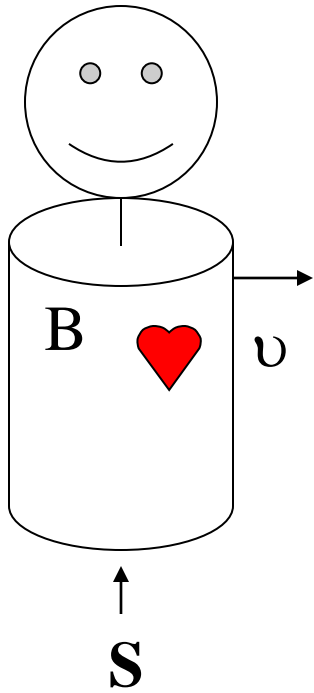
$$\nabla \wedge E = 0 \Rightarrow E = -\nabla U$$

*Thus*

$$\nabla \cdot \sigma \nabla U = 0$$

# Main Equation

$$\nabla \cdot \sigma \nabla U = 0$$



$$\nabla \cdot \sigma \nabla U = 0 \quad \text{in } B$$

$$\sigma \partial U / \partial \nu = j \quad \text{on } S$$

Forward Problem:

Given conductivity  $\sigma$  and current density  $\mathbf{j}$  find  $v = U$  on  $S$ .

**i.e.**

**Find the Neuman to Dirichletmap:**

$$\mathbf{R}(\sigma)\mathbf{j}=\mathbf{v}.$$

**Where**

$$\mathbf{R}(\sigma):H^{-1/2}(S)\rightarrow H^{+1/2}(S)$$

Inverse Problem:  
Given

**$R(\sigma)$**

Find

**$\sigma$**

Apply Currents or Voltages?



1. Apply currents  
measure voltages

since

$R(\sigma)$  is smoothing

but

$$\Lambda(\sigma) = R(\sigma)^{-1}$$

**Is desmoothing!**

$$\{\Lambda(\sigma) : H^{+1/2}(S) \rightarrow H^{-1/2}(S)\}$$

# Properties of R

R has a complete orthonormal set of eigenfunctions in  $L^2(S)$  and its eigenvalues are decreasing to 0.

See Board.

Can we distinguish different  
conductivities?

2. We can distinguish different conductivities when using infinite precision!

Calderon

Kohn and Vogelius

Sylvester and Uhlmann

Nachman

...

How to distinguish different  
conductivities when precision is  
finite?

3. Apply “the best” current patterns to distinguish conductivities;

These are eigenfunctions of N-D map.

Let

$$\langle f, g \rangle \equiv \int_S f(x) g(x) dS_x$$

$$\|f\|^2 = \langle f, f \rangle$$

The “distinguishability” of  $\sigma$  from  $\tau$  by current density  $j$  is denoted by

$$\delta(\sigma, \tau; j)$$

Given by

$$\delta(\sigma, \tau; j) \equiv \|(R(\sigma) - R(\tau))j\| / \|j\|$$



We find the “best” Current density by finding the max over  $j$  of

$$\frac{\langle (R(\sigma) - R(\tau))j, (R(\sigma) - R(\tau))j \rangle}{\langle j, j \rangle}$$

From Rayleigh the max  
distinguishability is

$$\delta(\sigma, \tau; \mathbf{j})$$

where

$$(\mathbf{R}(\sigma) - \mathbf{R}(\tau)) \mathbf{j} = \rho \mathbf{j}$$

$\rho$  is the largest eigenvalue of the  
absolute value of

$$|\mathbf{R}(\sigma) - \mathbf{R}(\tau)|$$

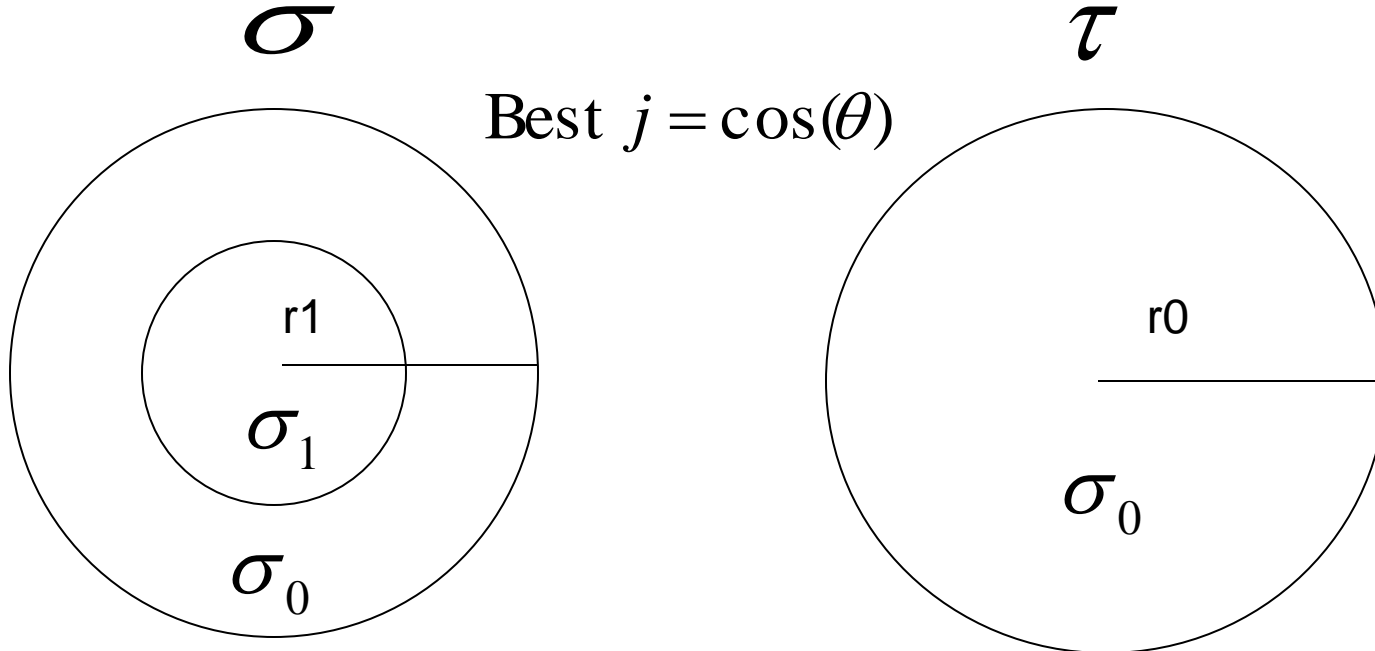
Thus  $\sigma$  is distinguishable from  $\tau$   
by measurements of precision  $\varepsilon$

iff

$$\max_j \delta(\sigma, \tau; j) = \rho > \varepsilon$$

What is the size of the smallest  
inhomogeneity?

## Example



$$\delta(\sigma, \tau; j) = (r_0 / \sigma_0) 2\mu\Gamma^2 / (1 + \mu\Gamma^2).$$

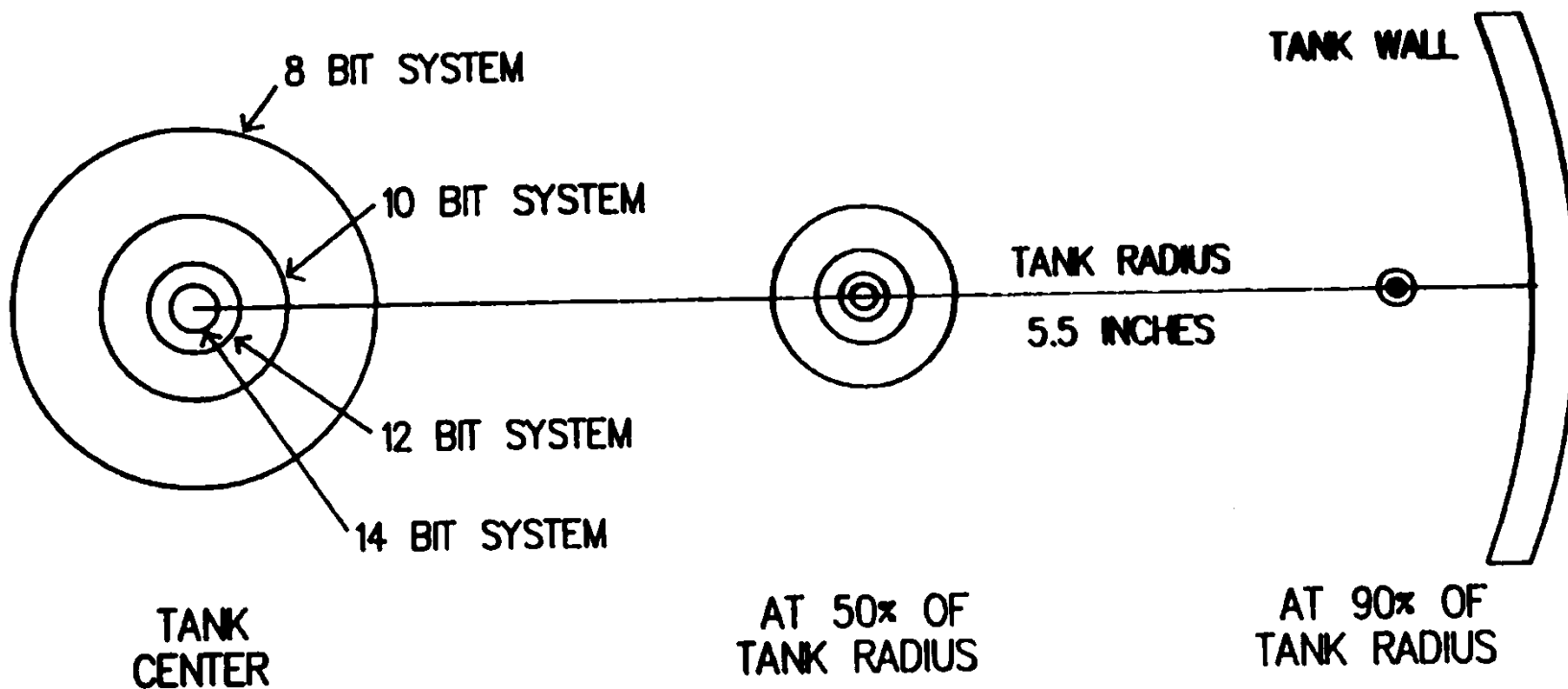
$$\Gamma \equiv r_1 / r_0; \mu \equiv (\sigma_1 - \sigma_0) / (\sigma_1 + \sigma_0).$$

Distinguishable iff

$$\delta(\sigma, \tau; j) \geq \varepsilon. \Leftrightarrow \mu\Gamma^2 = O(\varepsilon).$$

ECCT

# SMALLEST DETECTABLE DEFECT



How do we find “best” current  
patterns when we don’t know  
what is inside?

**Secret Adaptive Process!**

Adaptive method to find best current;

Guess -  $\mathbf{j}_0$

Measure (or compute) -  $\mathbf{R}(\sigma)\mathbf{j}_0$ ,  $\mathbf{R}(\tau)\mathbf{j}_0$

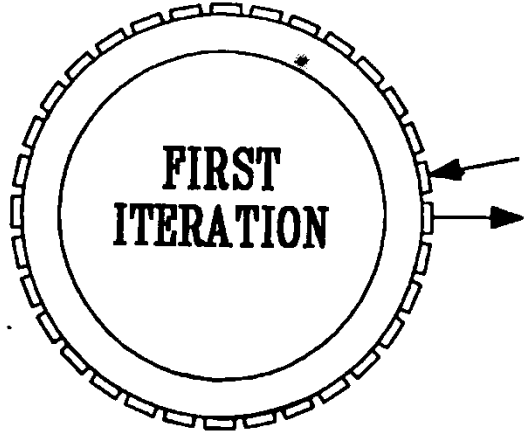
Let -

$$\mathbf{j}_1 = (\mathbf{R}(\sigma)\mathbf{j}_0 - \mathbf{R}(\tau)\mathbf{j}_0) / \|\mathbf{R}(\sigma)\mathbf{j}_0 - \mathbf{R}(\tau)\mathbf{j}_0\|$$

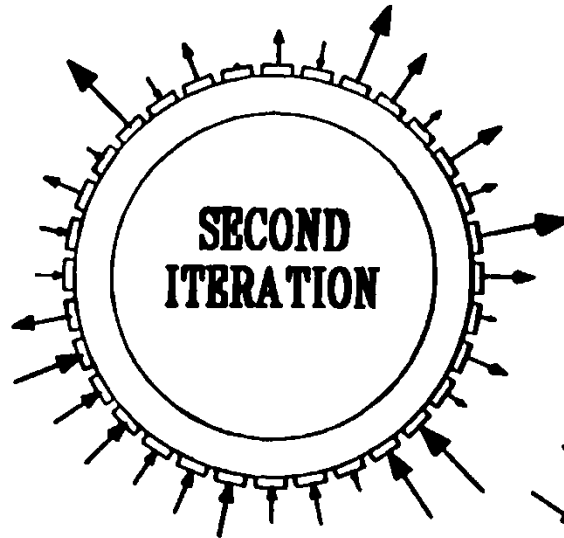
If  $\mathbf{j}_1 \neq \mathbf{j}_0$  Let  $\mathbf{j}_0 \equiv \mathbf{j}_1$  and try again!



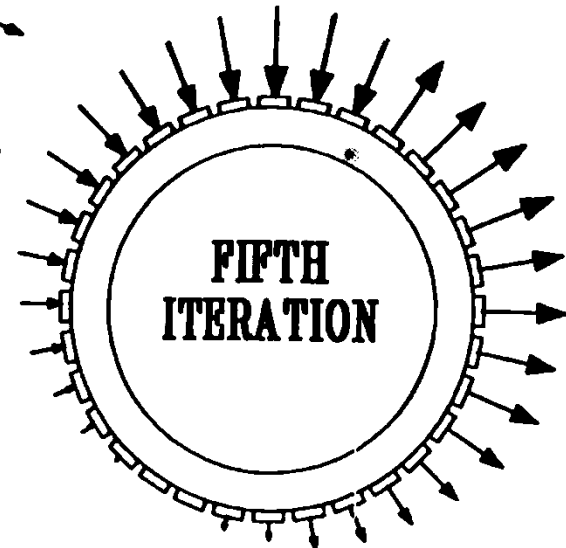
# BEST CURRENT ALGORITHM



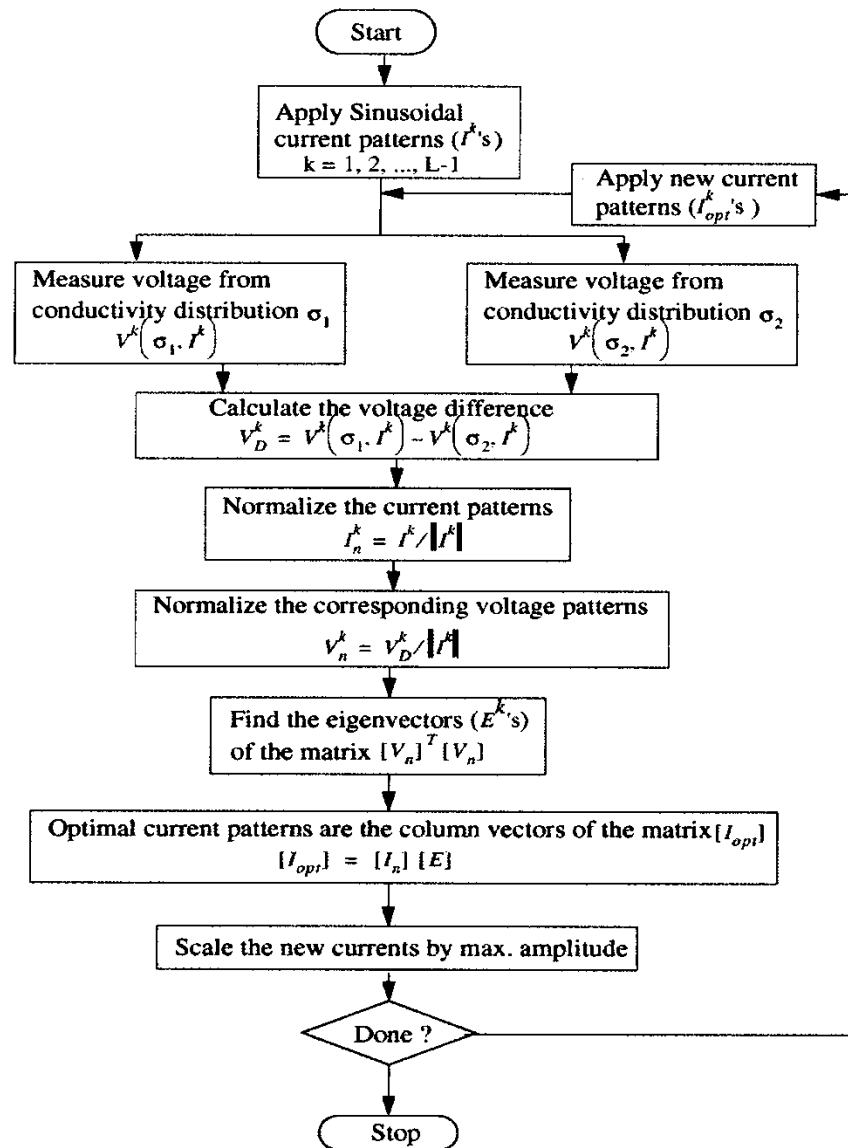
DEVELOPED AT  
RENSSELAER (RPI)  
BY D. ISAACSON



BY THE FIFTH ITERATION,  
THE SYSTEM HAS DETERMINED  
THE "BEST" PATTERN OF CURRENT  
FOR DETECTING THE UNKNOWN DEFECT!



How do we find *ALL* the Current patterns that are useful?



**Figure 1. Flow chart for computing the optimal current patterns**

Does it Work?

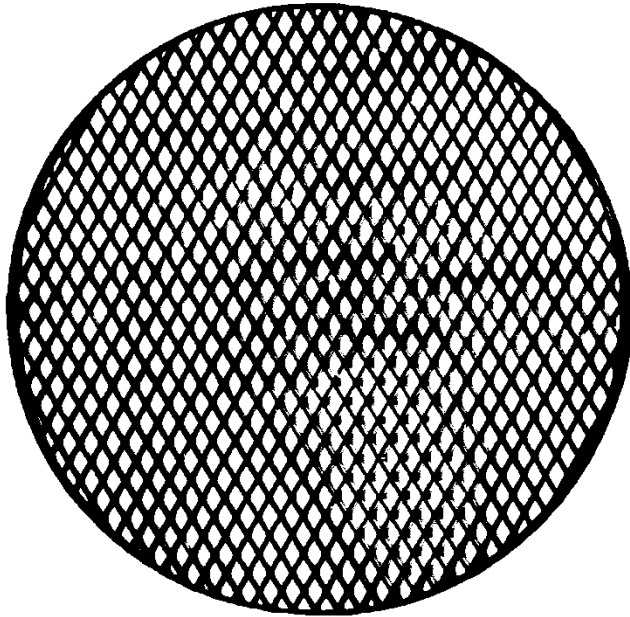
# Electric Current Computed Tomography

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PHYSICAL METALLURGY LABORATORY  
MATERIALS RESEARCH CENTER

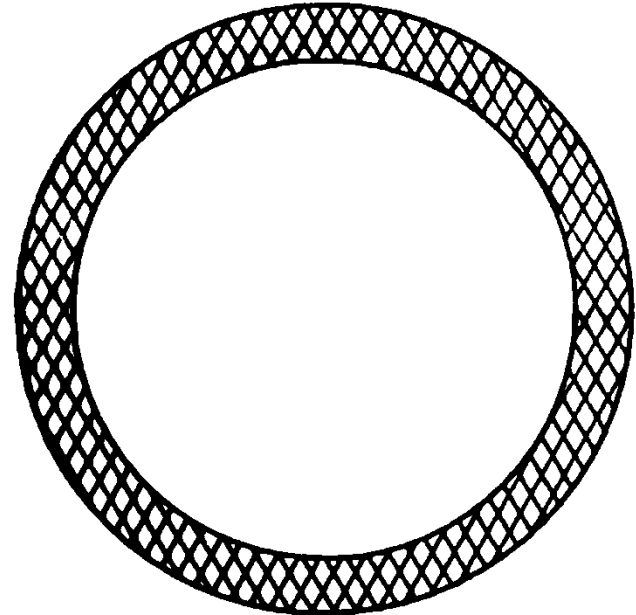
H.D. Solomon  
M.R. Eggleston  
R.J. Schwabe  
L.F. Coffin  
D. Isaacson

## SOLID CYLINDER GEOMETRY



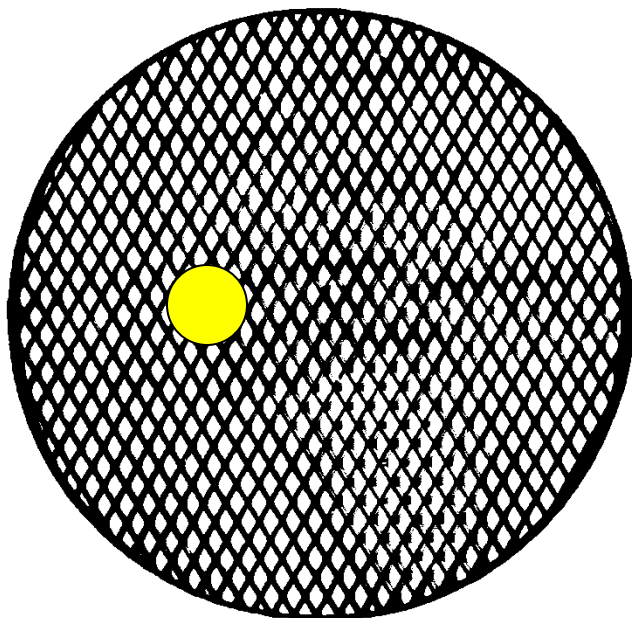
**OUTER DIAMETER IS 5.5 INCHES**

## PIPE GEOMETRY



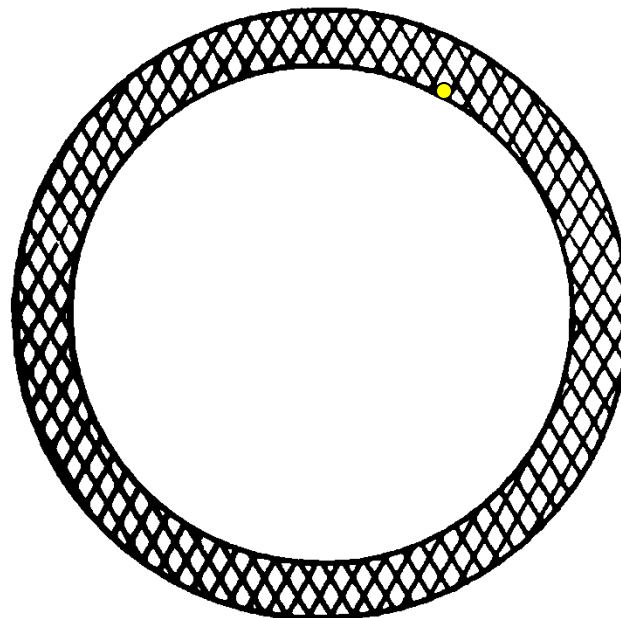
**OUTER DIAMETER IS 5.5 INCHES  
INNER DIAMETER IS 4.5 INCHES  
WALL THICKNESS IS 0.5 INCHES**

## SOLID CYLINDER GEOMETRY



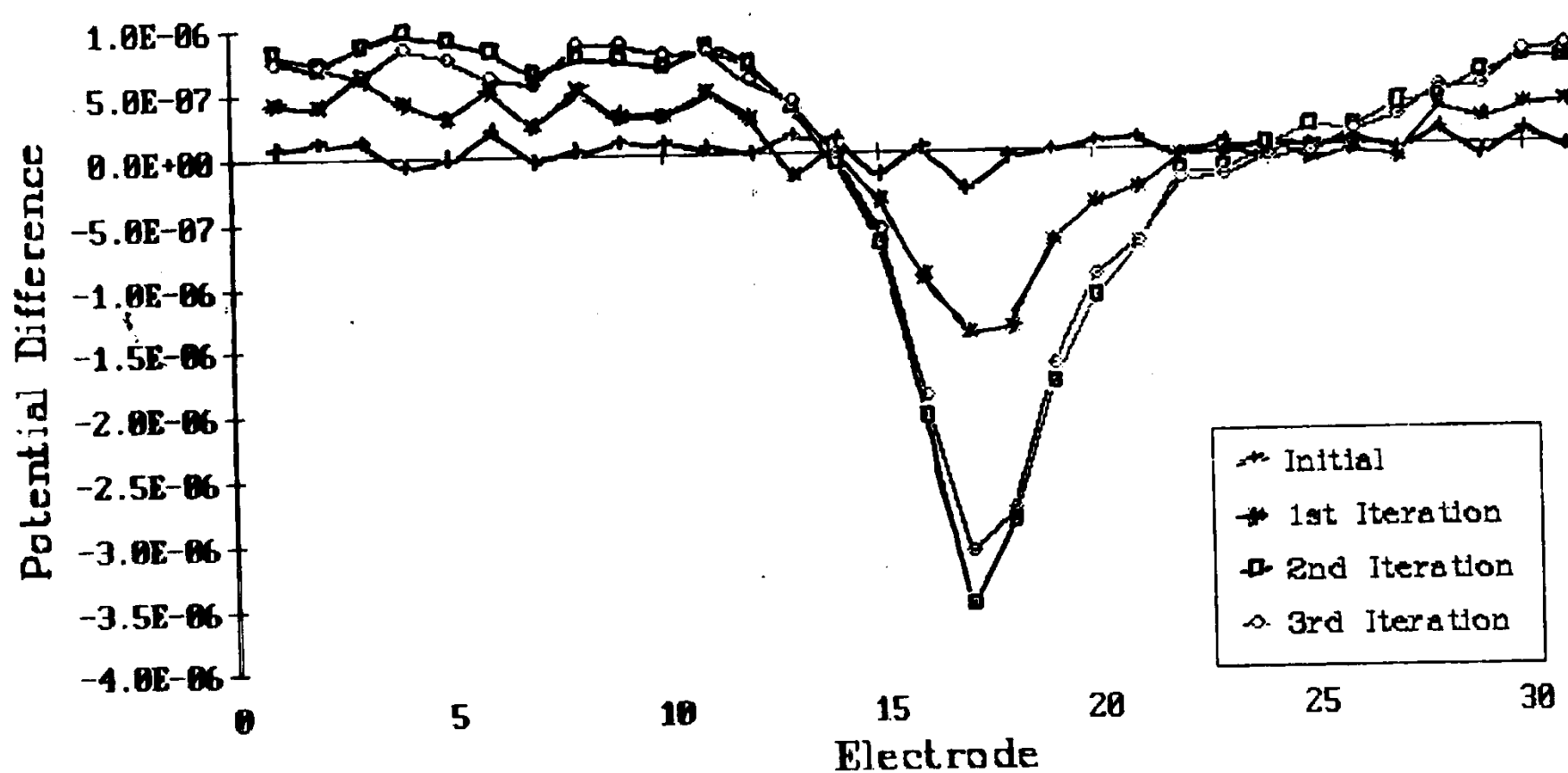
**OUTER DIAMETER IS 5.5 INCHES**

## PIPE GEOMETRY



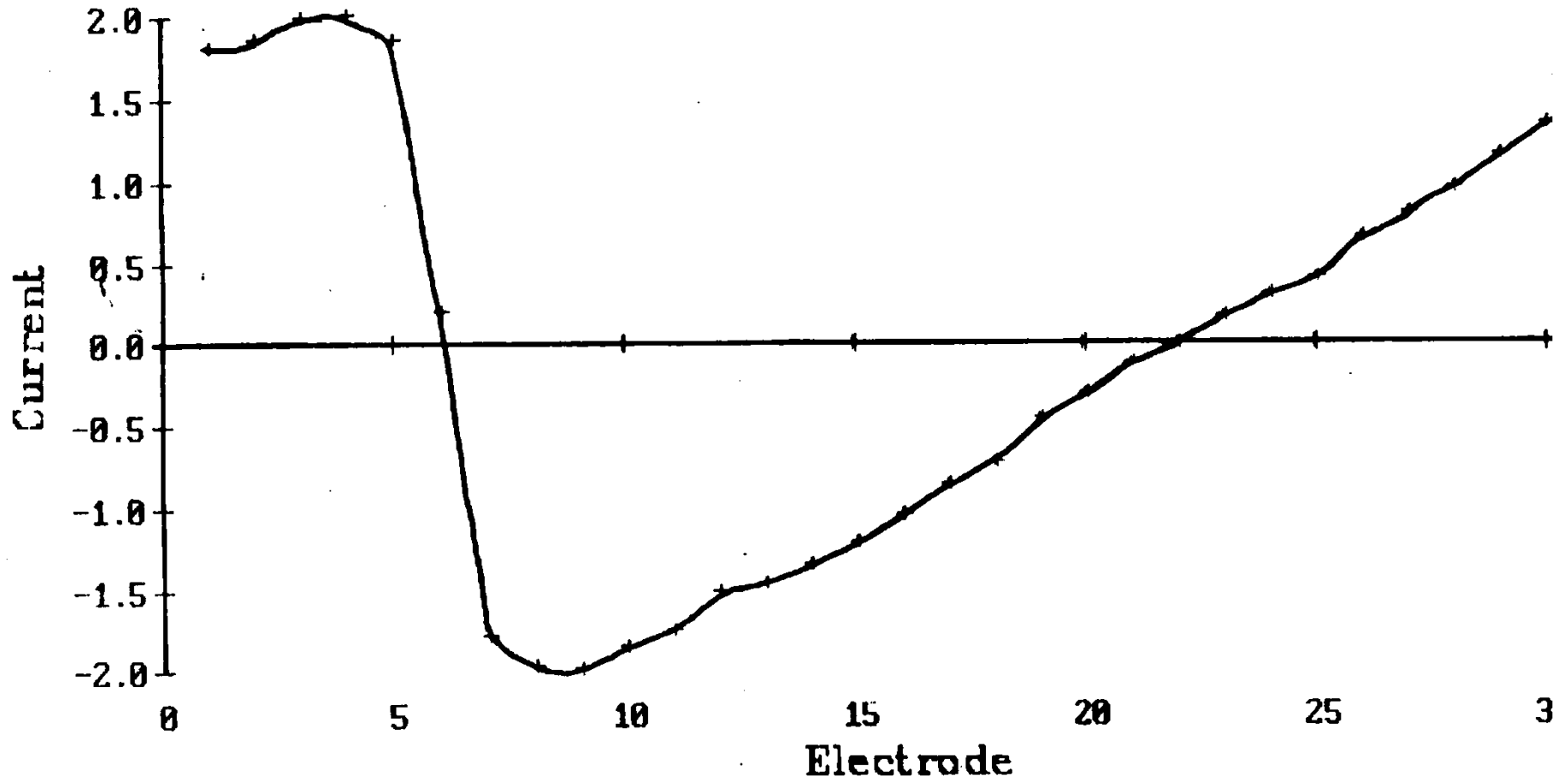
**OUTER DIAMETER IS 5.5 INCHES  
INNER DIAMETER IS 4.5 INCHES  
WALL THICKNESS IS 0.5 INCHES**

Adaptive Process  
1/2" Target at Electrode #17  
Positioned at 3/4 Tank Radius

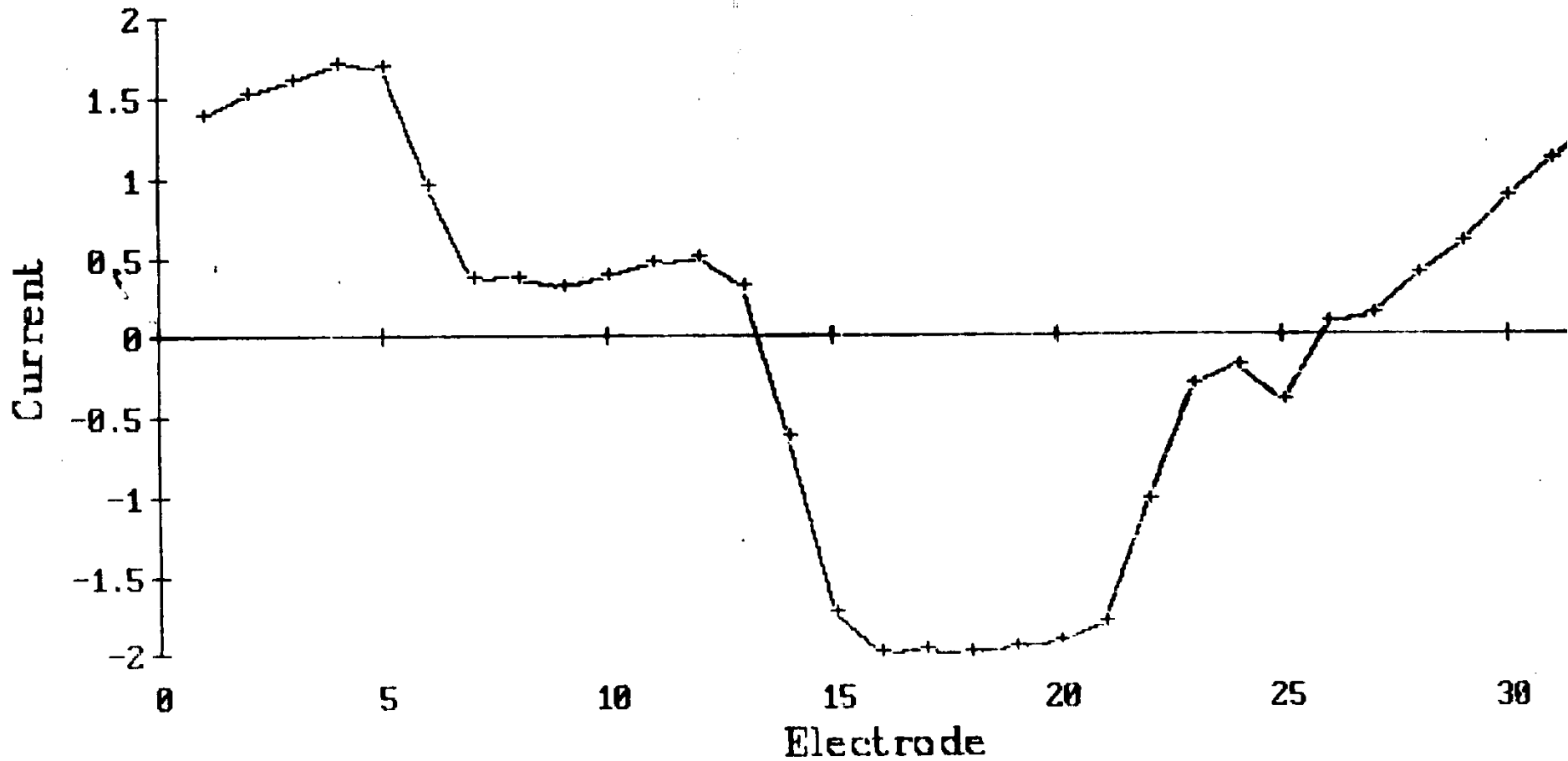




# Simulated Pipe 1/8" Defect at Electrode #6

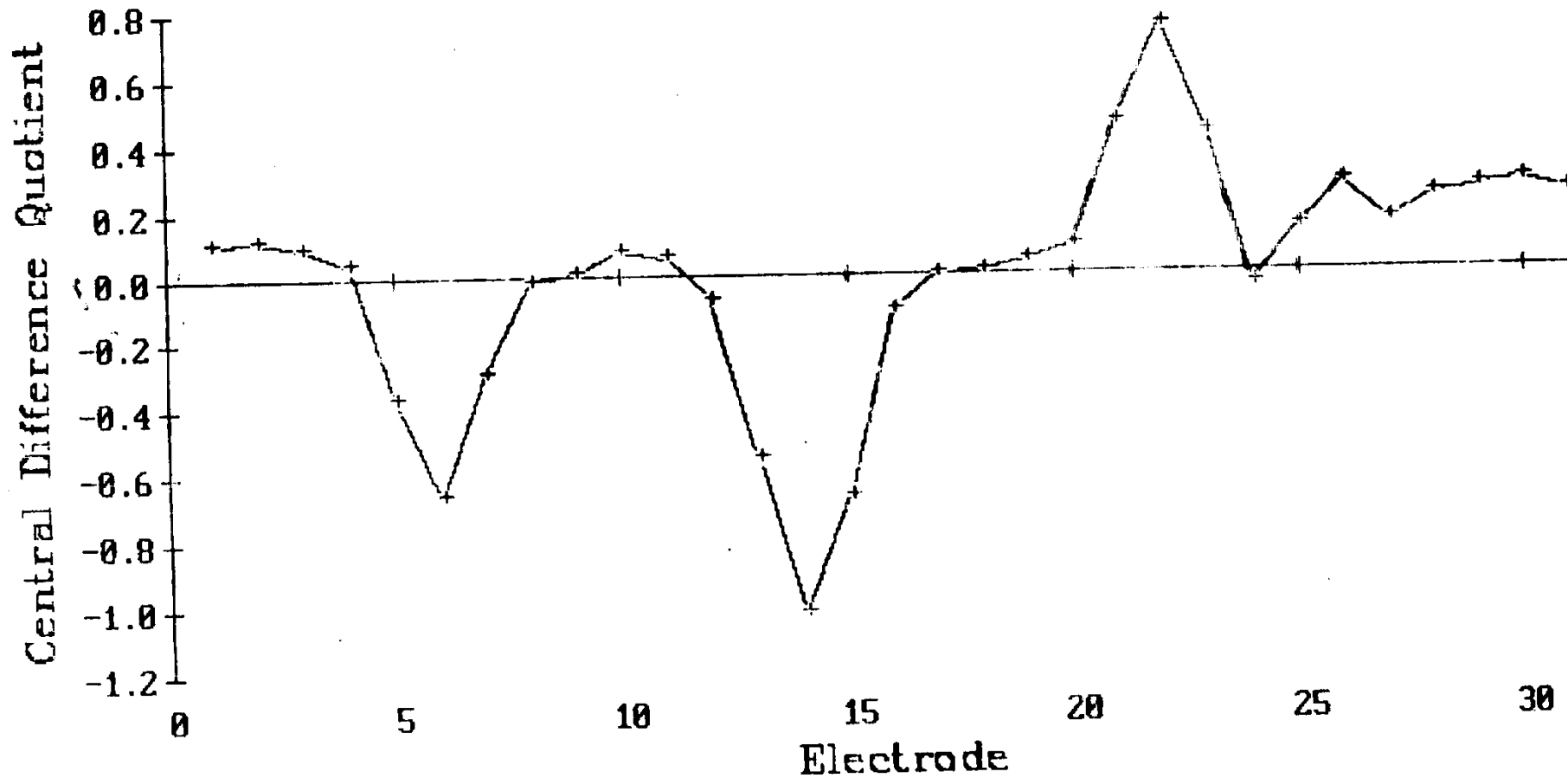


Simulated Pipe  
3 Defects: Electrodes #6, #14, and #22



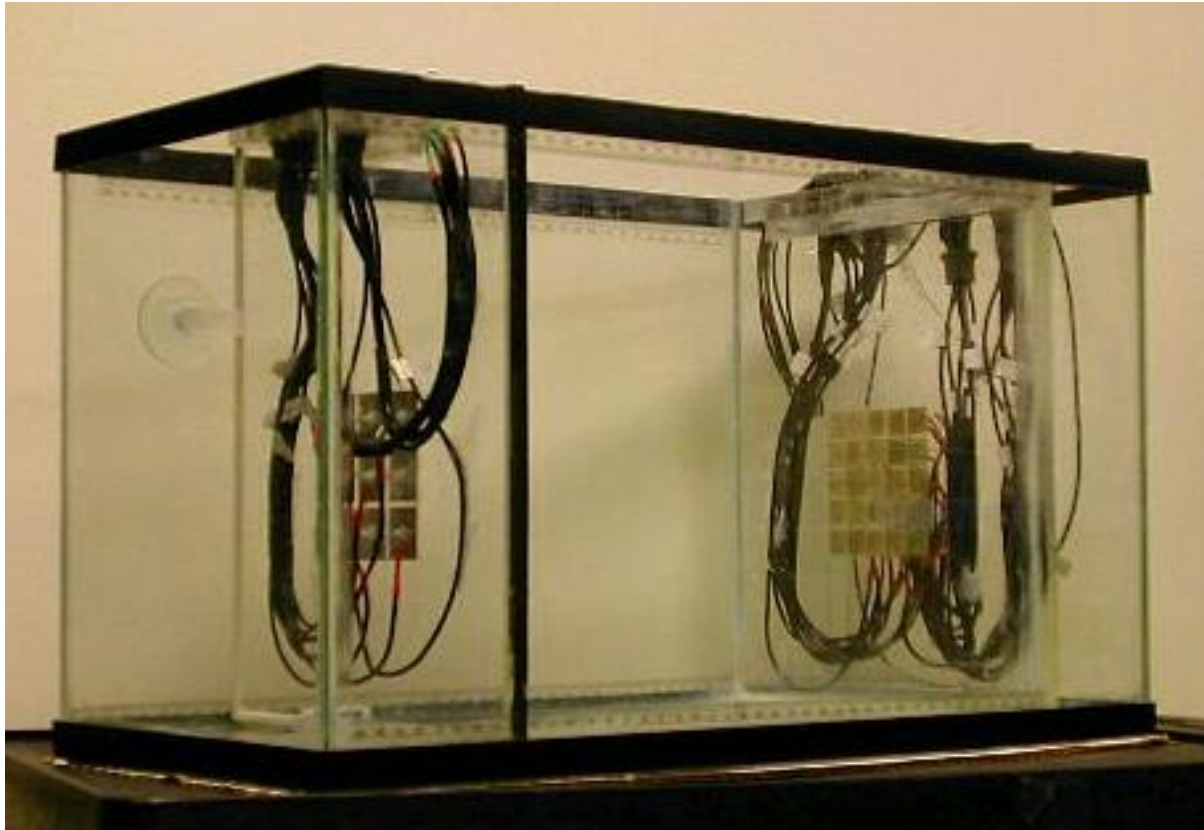
# Simulated Pipe

3 Defects: Electrodes #6, #14, and #22



Can optimal currents improve  
sensitivity and specificity in  
screening for breast cancer  
?

# 5x5 Electrode Array Tank



# Distinguishability Study Results

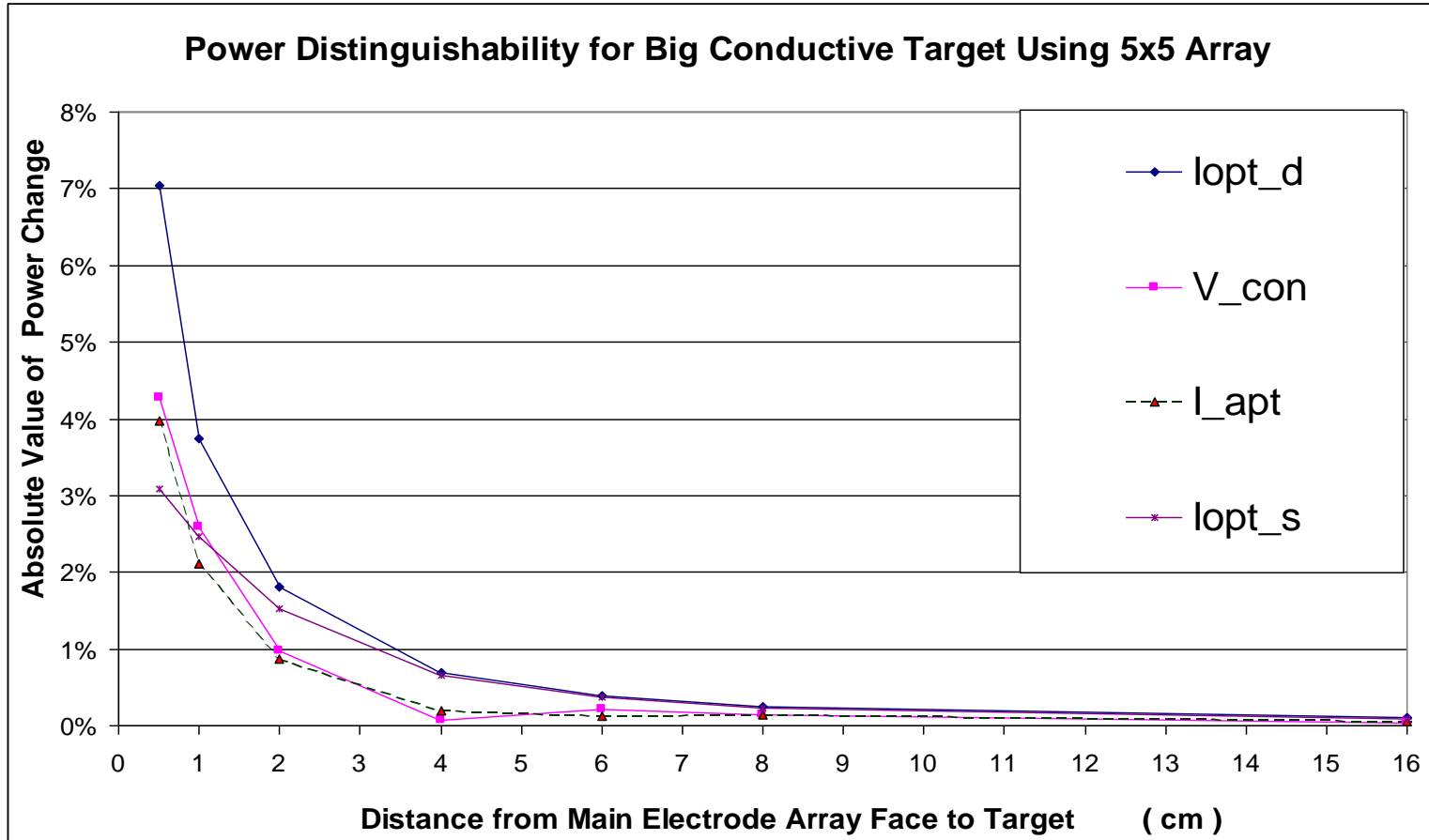
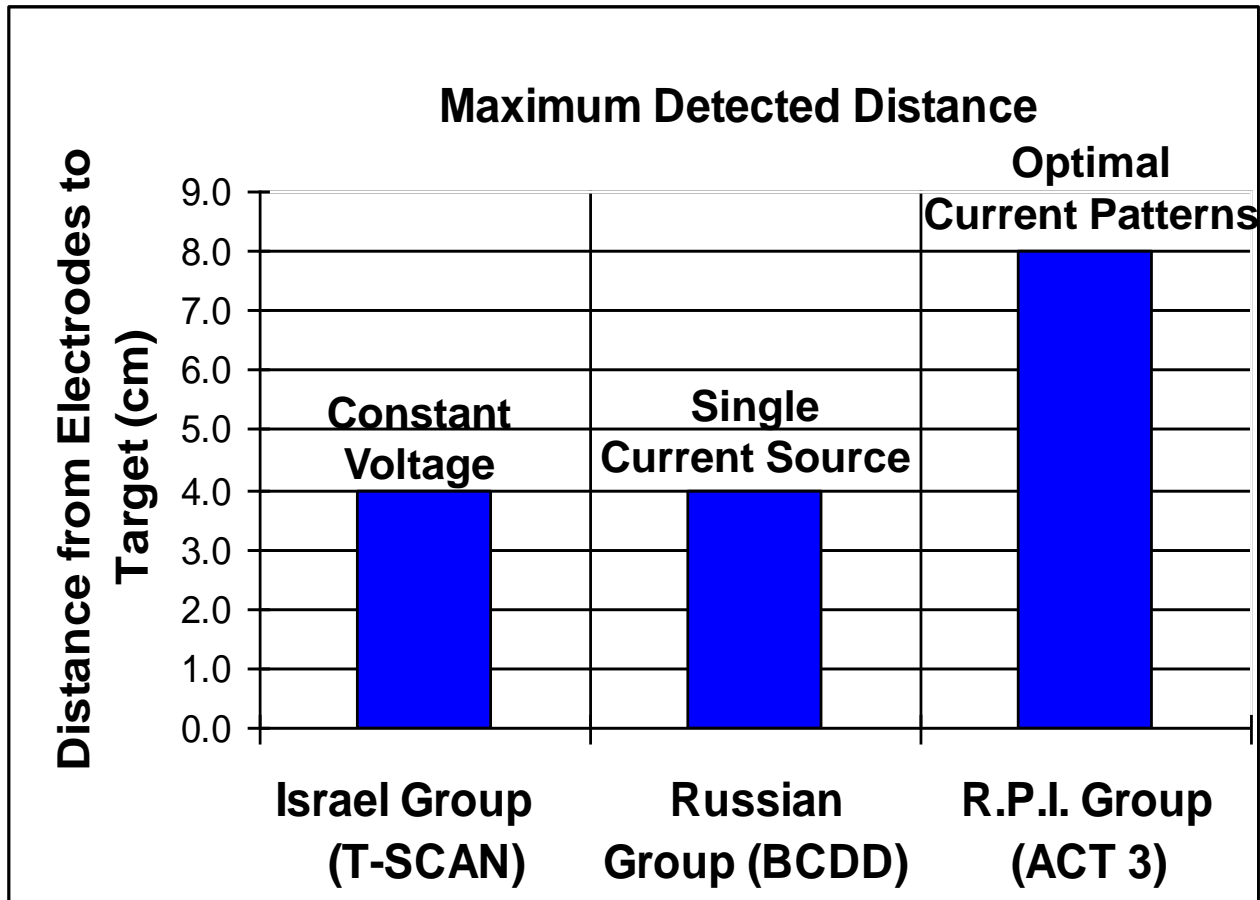


Figure 3. Optimal Current Pattern  $I_{opt\_d}$  has better power distinguishability at all distances. For this experiment, the experimental noise level of the magnitude of the power change is 0.02%, above which targets may be distinguishable.

The depth below mammography electrodes at which an inhomogeneity can be detected by .4% accuracy



Electrode Array 5x5, Array Size: 8cm Square, Electrode Size: 14.8mm Square  
Target Size: 24 mm Cube  
From Poster by Tzu-Jen Kao

How many electrodes to use?



$L \equiv$  Number of electrodes

$\varepsilon \equiv$  Measurement precision

Then

$L = O(\varepsilon^{-1/2})$  in 2D,  $O(\varepsilon^{-1/3})$  in 3D.

# How many current sources to use?

As many as we have electrodes.

See Proof that as  $L \rightarrow \infty$  distinguishability  $\rightarrow 0$  for a fixed number of current sources.

What size should we make the  
electrodes?

Space filling!

## 4. How can we reconstruct useful images?

1. Linearization (Noser 2-D , Toddler 3-D);  
Fast, useful, not accurate for large contrast conductivities.
2. Optimization (Regularized Gauss-Newton);  
Slow, more accurate , iterative methods
3. Direct methods (Layer stripping, D-Bar);  
Solve full non-linear problem, no iteration!

End Part II

How do we make images?

# Electrical Impedance Tomography

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RPI

**Part 2.**  
**Electrical Impedance Imaging**  
**Algorithms.**

# Solve the Problems:

1. Should we apply currents or voltages?
2. Can we distinguish  $\sigma$  from  $\tau$ ?
3. Which patterns of currents or voltages should we apply?
4. How many electrodes?
5. What size electrodes?
6. How can we reconstruct useful images?



## 4. How can we reconstruct useful images?

1. Linearization (Noser 2-D ,Toddler 3-D);

Fast, useful, not accurate for large contrast conductivities.

2. Optimization (Gauss Newton, Adaptive Kacmarcz);

Slow, more accurate , iterative methods.

3. Direct methods (Layer stripping, CGO, dbar);

Solve full non-linear problem, no iteration!

# What can a linearization do?

Noser – a 2-D reconstruction

Toddler – a 3-D reconstruction

(both assume conductivity differs  
only a little from a constant.)

FNoser - Fast ,20 frames/sec

Real time imaging of Cardiac and  
Lung function shown in the following  
examples.

# Linearizations

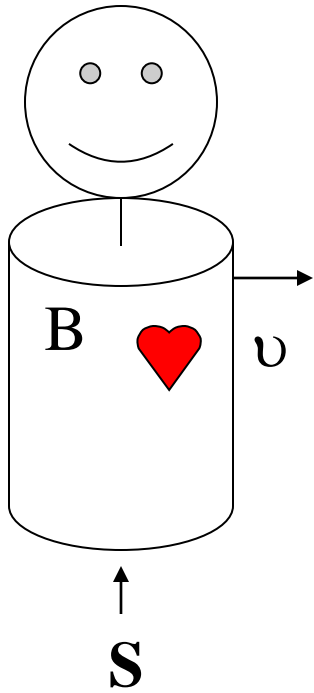
NOSER (S.Simske,...)

FNOSER(P.Edic,...)

TODDLER(R.Blue,...)

# Main Equation

$$\nabla \cdot \sigma \nabla U = 0$$



$$\nabla \cdot \sigma \nabla U = 0 \quad \text{in } B$$

$$\sigma \partial U / \partial \nu = j \quad \text{on } S$$

Forward Problem:

Given conductivity  $\sigma$  and current density  $\mathbf{j}$  find  $v = U$  on  $S$ .

**i.e.**

**Find the Neuman to Dirichletmap:**

$$\mathbf{R}(\sigma)\mathbf{j}=\mathbf{v}.$$

**Where**

$$\mathbf{R}(\sigma):H^{-1/2}(S)\rightarrow H^{+1/2}(S)$$

Inverse Problem:  
Given

**$R(\sigma)$**

Find

**$\sigma$**

$$\nabla \cdot \sigma \nabla u^m = 0$$

$$\sigma \partial u^m / \partial \nu = j^m$$

$$\nabla \cdot \sigma_0 \nabla u_0^n = 0$$

$$\sigma_0 \partial u_0^n / \partial \nu = j_0^n$$

$$u_0^n \nabla \cdot \sigma \nabla u^m = 0$$

$$u^m \nabla \cdot \sigma_0 \nabla u_0^n = 0$$

$$\int u_0^n \nabla \cdot \sigma \nabla u^m - u^m \nabla \cdot \sigma_0 \nabla u_0^n dx = 0$$

⇓

$$\int_S u_0^n \sigma \partial_\nu u^m - u^m \sigma_0 \partial_\nu u_0^n dS = \int_B (\sigma - \sigma_0) \nabla u^m \cdot \nabla u_0^n dx$$



$$\int_S u_0^n \sigma \partial_\nu u^m - u^m \sigma_0 \partial_\nu u_0^n dS = \int_S u_0^n j^m - u^m j^n dS =$$

$$\langle j^m, (R(\sigma) - R(\sigma_0)) j^n \rangle =$$

$$\text{Data}(n, m) =$$

$$\int_B (\sigma - \sigma_0) \nabla u^m \cdot \nabla u_0^n dx$$

If  $\delta\sigma \equiv \sigma - \sigma_0 \ll \sigma_0$  then  $u^m = u_0^m + O(\delta\sigma)$

$$\text{Data}(n, m) = \int_B (\sigma - \sigma_0) \nabla u^m \cdot \nabla u_0^n dx$$

$$= \int_B \delta\sigma \nabla u_0^m \cdot \nabla u_0^n dx + O(\delta\sigma^2)$$

$$Data(n, m) \approx \int_B \delta\sigma \nabla u_0^m \cdot \nabla u_0^n dx$$

Choose BASIS,  $\{\psi_k(x)\}$ ,

$$\delta\sigma(x) = \sum_k C_k \psi_k(x)$$

Thus only need to solve;

$$Data(m, n) = \sum_k C_k \int_B \psi_k(x) \nabla u_0^m \cdot \nabla u_0^n dx$$

$$Data(m, n) = \sum_k M_{m, n}^k C_k$$

What is the Basis?

**SEE TRANSPARENCIES**

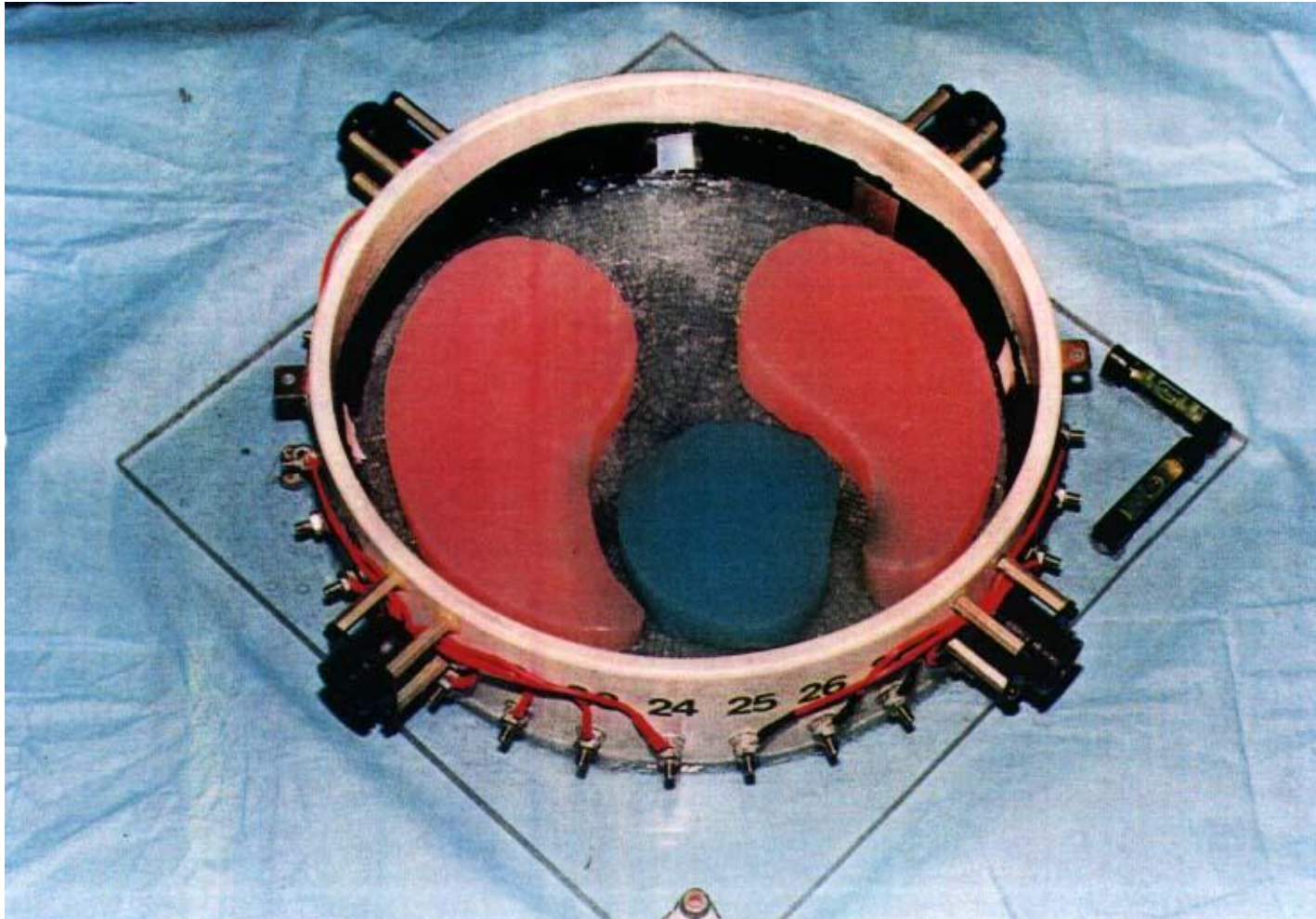
Does it work?

Test by experiment

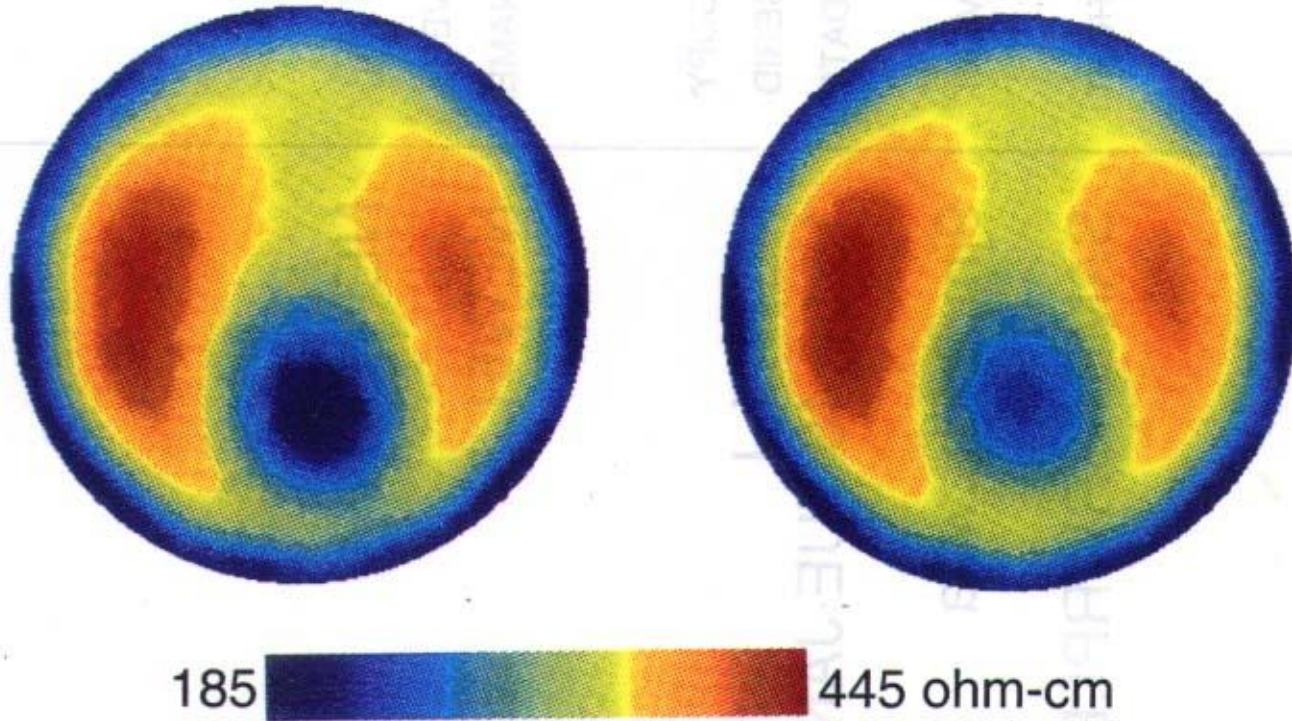
# ACT 3

- 32 Current sources
- 32 Voltmeters
- 32 Electrodes
- 30 KHZ
- 20 Frames / Sec
- Accuracy  $> .01\%$

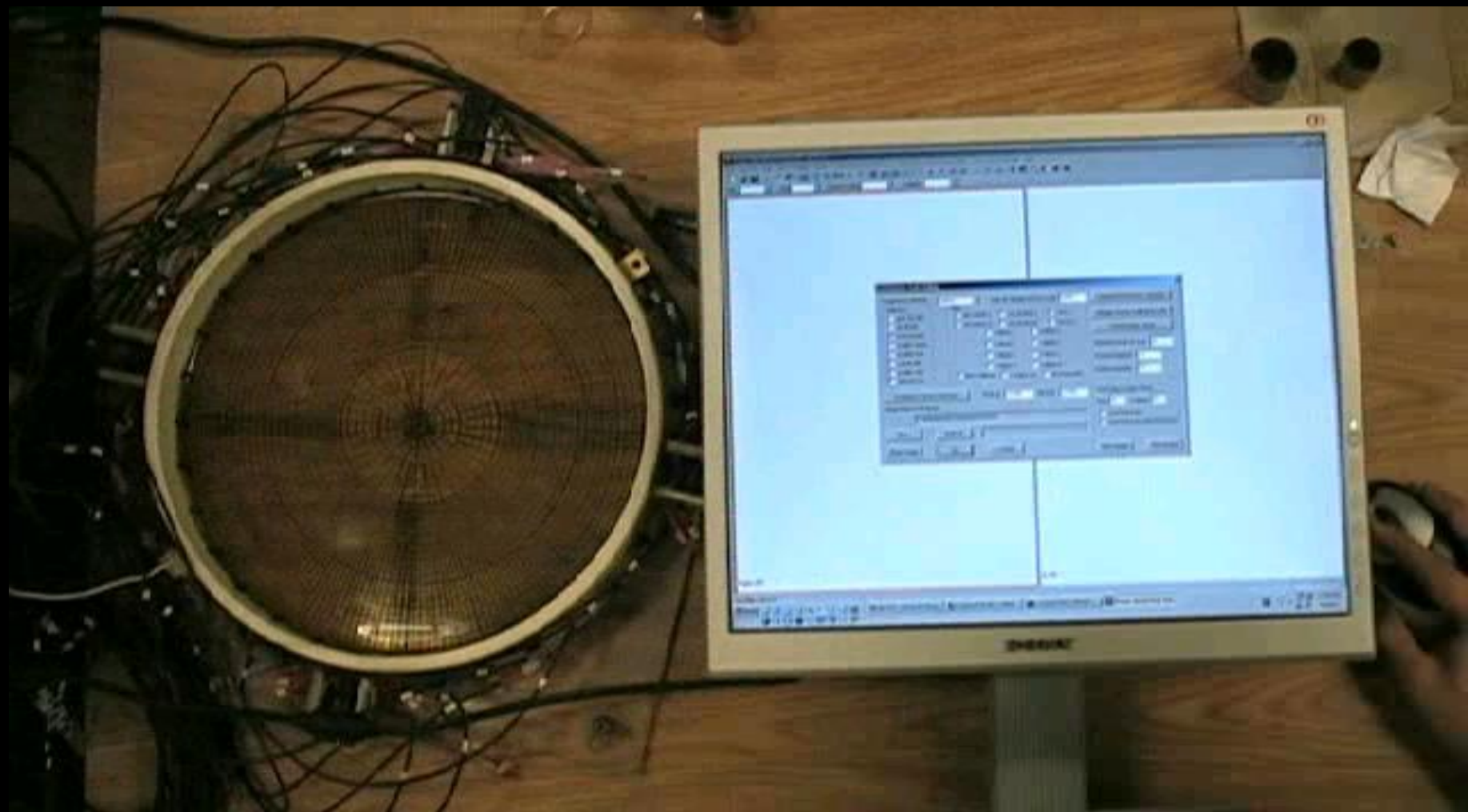
# Phantom



# Reconstructions





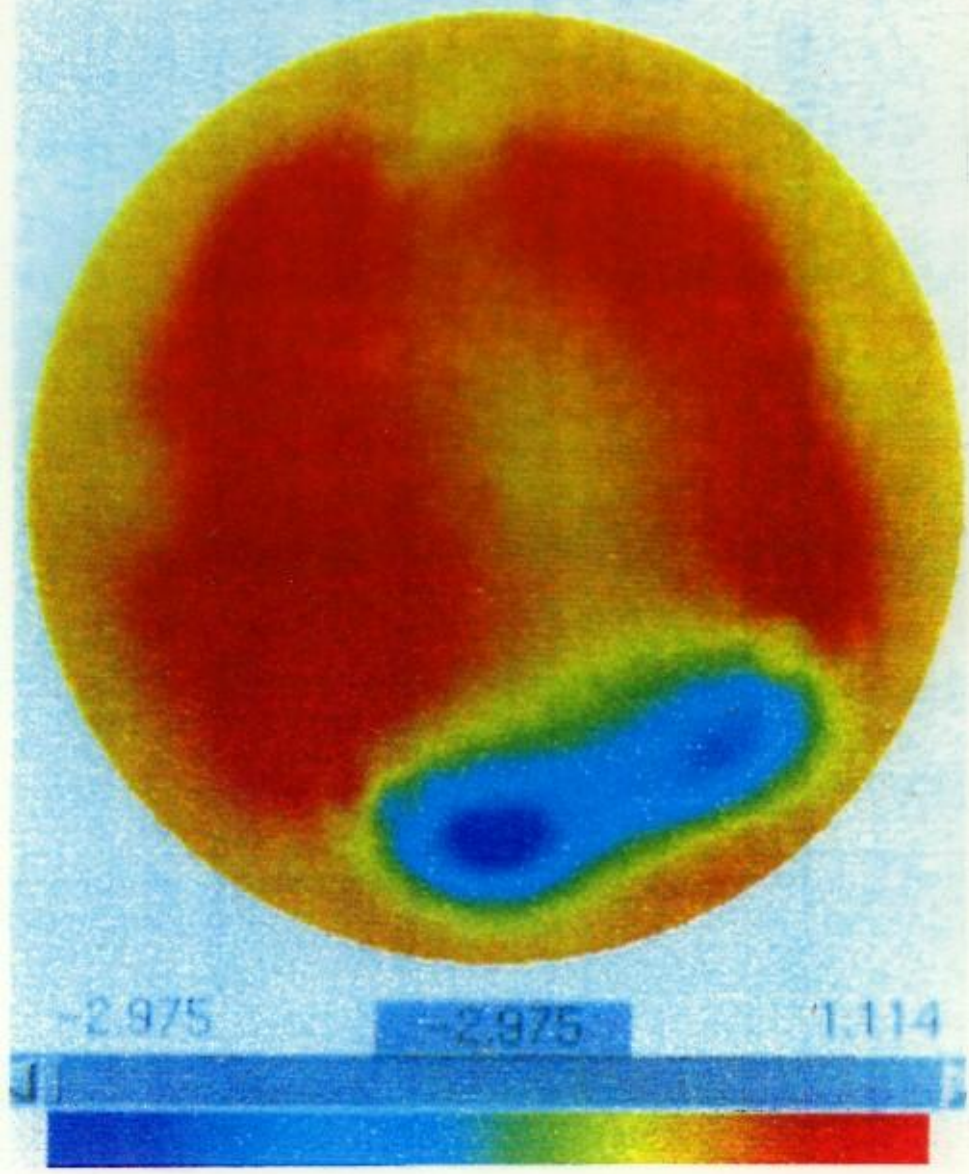




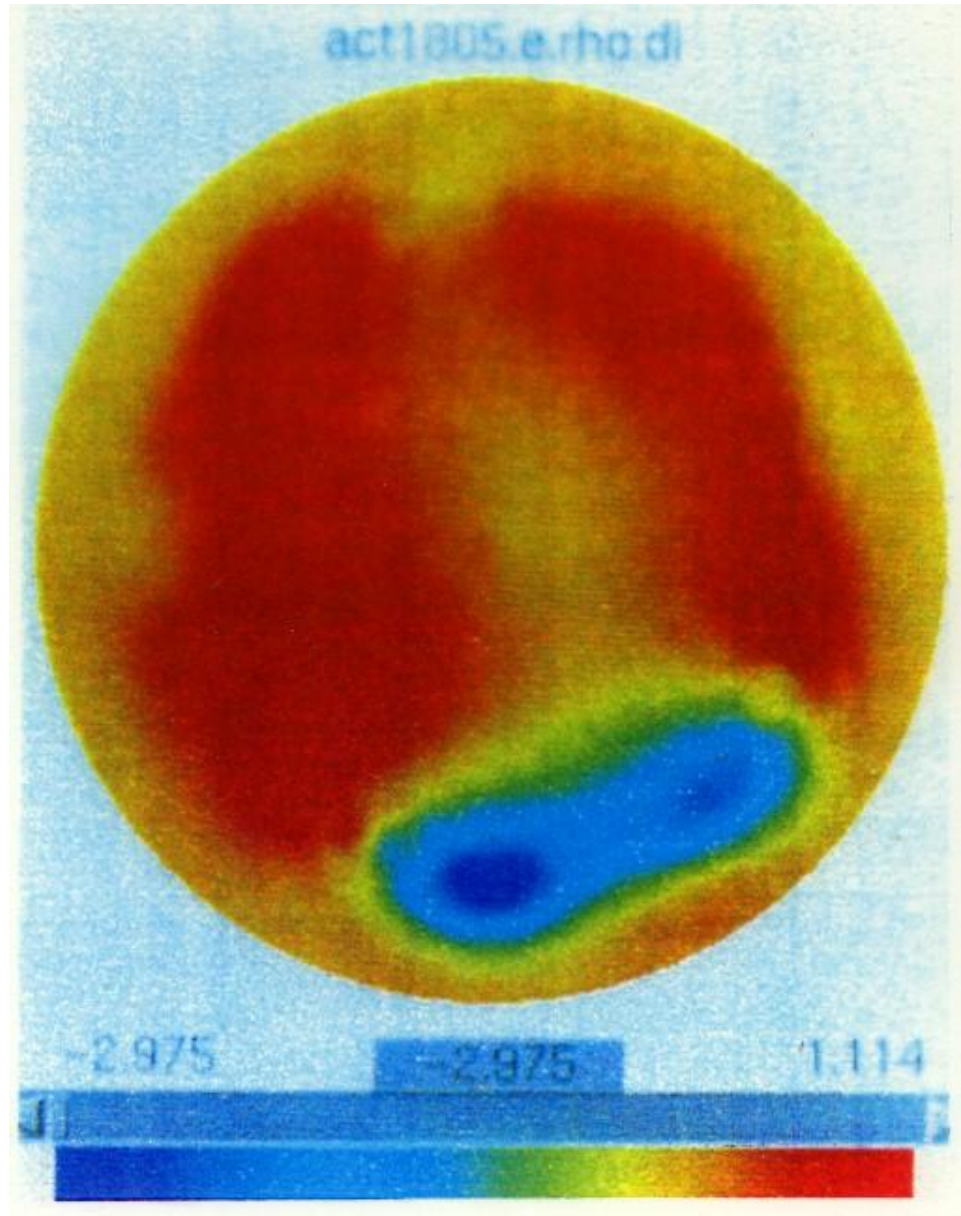
Can it image heart and lung  
function?



act1805.e.rho di







**ACT 3 imaging blood as it leaves the heart ( blue) and fills the lungs (red) during systole.**

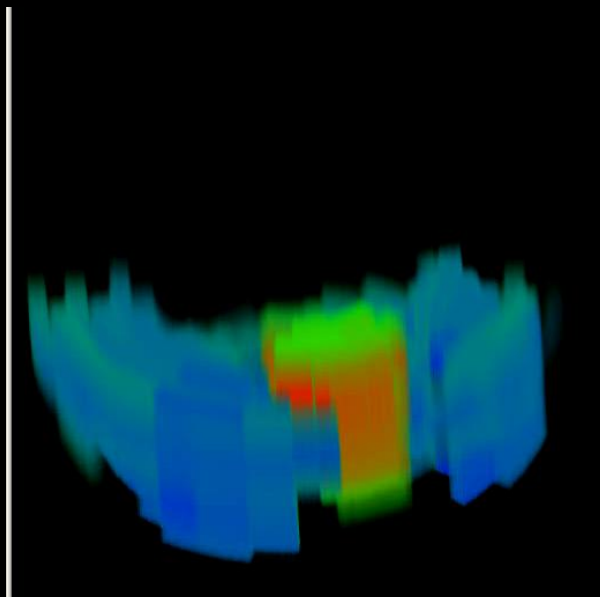
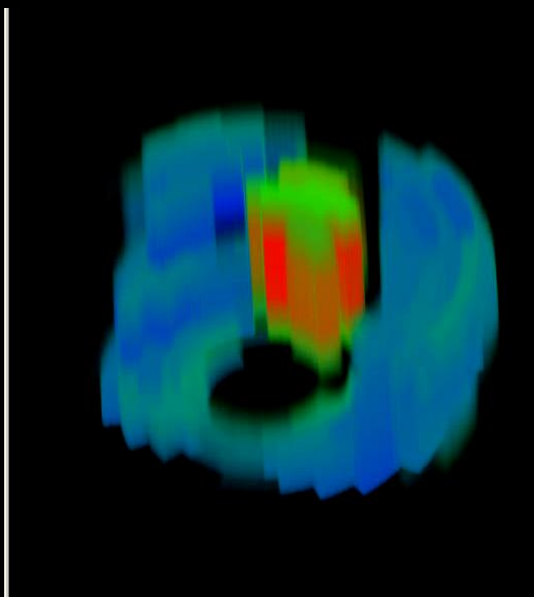
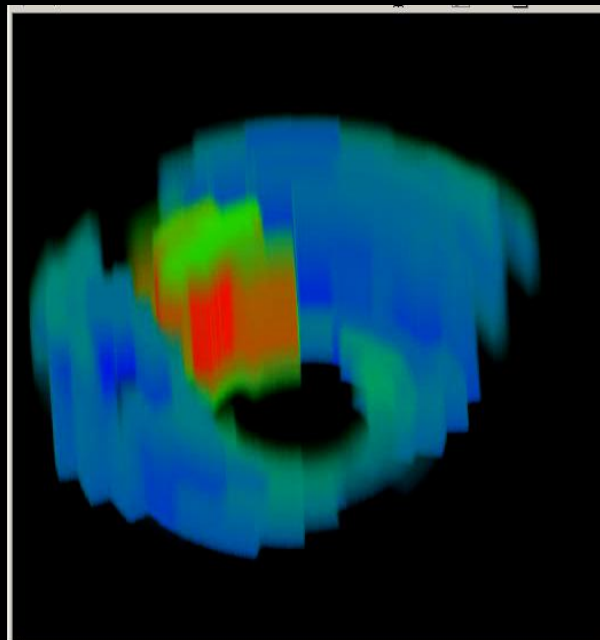
# Show 2D Ventilation and Perfusion Movie



# 3D Electrode Placement

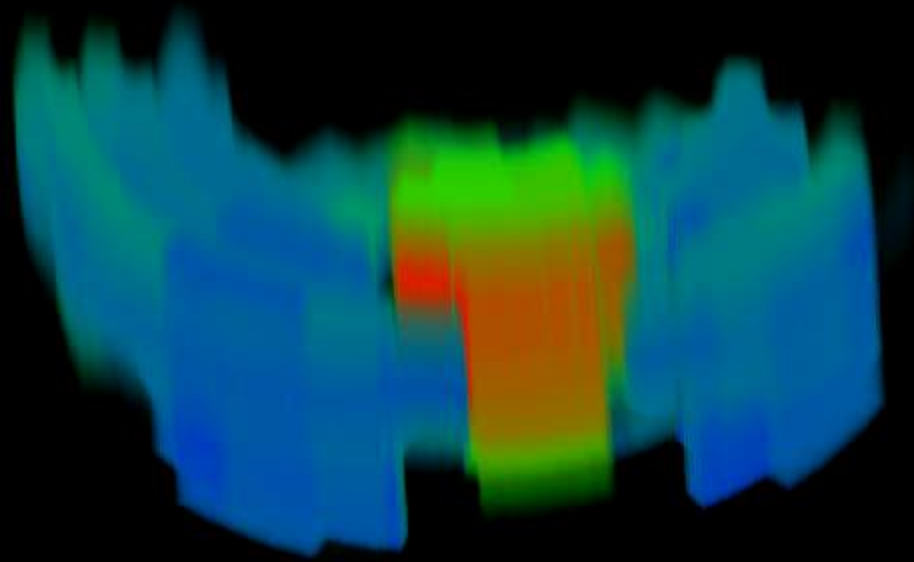






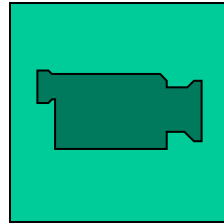


# Heart Lung Static Image



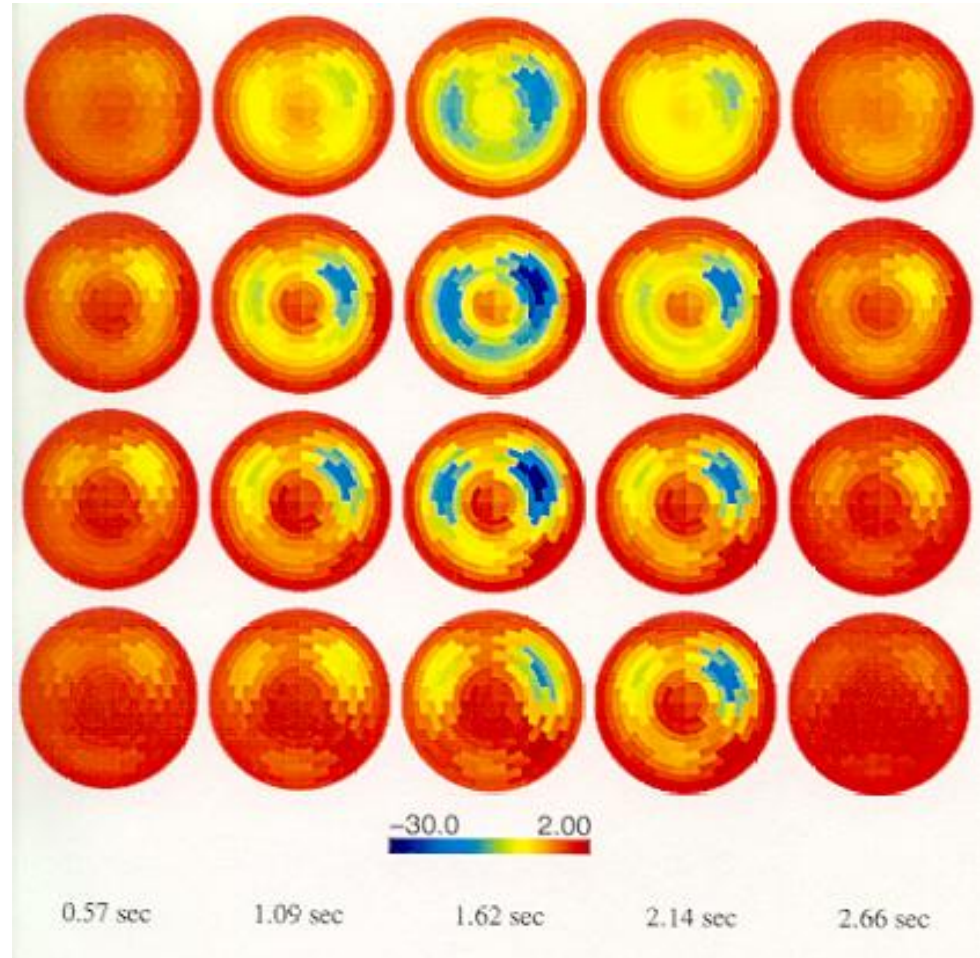
3D Heart lung

Show Heart Lung View from  
other source



# Ventilation in 3D

# 3D Human Results



- Images showing conductivity changes with respiration





# Cardiac in 3D



How can one get more accurate values of the conductivity, less artifact, and still be fast?

D-Bar method for EIT  
J. Mueller , S.Siltanen, D.I.

Special thanks to A.Nachman

# D-Bar Reconstruction method

- Convert inverse conductivity problem to an Unphysical Inverse Scattering Problem for the Schrodinger Equation.
- Use the measured D-N map to solve a boundary integral equation for the boundary values of the exponentially growing Faddeev solutions .
- Compute the unphysical Scattering transform in the complex  $k$ -plane from these boundary values.
- Solve the D-Bar integral equation in the whole complex  $k$ -plane for the Faddeev solutions in the region of interest.
- Take the limit as  $k$  goes to 0 of these solutions to recover and display the conductivity in the region of interest.

Problem: Find the Conductivity  $\sigma$   
from the measured Dirichlet to  
Neumann map  $\Lambda_\sigma$

Assume:

$$\nabla \cdot \sigma \nabla u = 0 \quad \text{inside } B.$$

$$u = V \quad \text{on } \partial B.$$

$$\Lambda_\sigma V = \sigma \partial u / \partial \nu \quad \text{on } \partial B.$$

$\sigma = 1$  in a neighborhood of  $\partial B$ .

Let ;

$$\Psi = \Psi(p, \zeta) \equiv \sigma^{1/2} u,$$

$$q = q(p) \equiv \sigma^{-1/2} \Delta \sigma^{1/2}$$

Then

$$-\Delta \Psi + q \Psi = 0 \quad \text{in } B$$

$$\Lambda_\sigma \Psi = \partial \Psi / \partial \nu \quad \text{on } \partial B$$

and  $q = 0$  in a neighborhood of  $\partial B$ .

Look for Solutions  $\Psi$  on all of  $\mathbb{R}^n$  ( $n \geq 2$ ) with  $q = 0$  outside  $\partial B$  that satisfy

$\Psi \approx \exp(i\zeta \cdot p)$  as  $|p| \rightarrow \infty$ , where  $\zeta \cdot \zeta = 0$ .

In  $\mathbb{R}^2$  take  $\zeta = k(1, i)$  where  $k = k_1 + ik_2$

Let

$$\Psi = \Psi(p, \zeta) = \exp(i\zeta \cdot p) \mu(p, \zeta)$$

where  $\mu \rightarrow 1$  as  $|p| \rightarrow \infty$ .



Observe that

$$(-\Delta - 2i\zeta \cdot \nabla)\mu + q\mu = 0$$

and  $\mu \rightarrow 1$  as  $|p| \rightarrow \infty$ .

We may recover  $\sigma$  from  $\mu$  by the property that;

$$\sigma^{1/2}(p) = \mu(p, 0) = \lim_{\zeta \rightarrow 0} \mu(p, \zeta).$$

Reason:

$$-\Delta\mu(p, 0) + q\mu(p, 0) = 0$$

$$-\Delta\sigma^{1/2} + q\sigma^{1/2} = 0$$

Since both  $\sigma^{1/2}$  and  $\mu \rightarrow 1$  at  $\infty$  they are identical.

Main Problem: Given  $\Lambda_\sigma$  find  $\mu$ ?

1. First find  $\Psi$  and hence  $\mu$  on  $\partial B$  by solving

$$[I + S(\Lambda_\sigma - \Lambda_1)] \Psi = \exp(i\zeta \cdot p) \text{ on } \partial B.$$

Here  $S$  denotes the operator

$$(Sw)(p) = \int_{\partial B} G(p-t)w(t)ds(t)$$

where  $G(p)$  is the Faddeev Greens function

$$-\Delta G = \delta, \quad G \approx \exp(i\zeta \cdot p) \text{ as } |p| \rightarrow \infty.$$

2. Compute the "unphysical" scattering transform

$$t(\mathbf{k}) = \int_{\partial B} \exp(i\bar{\zeta} \cdot \mathbf{p}) (\Lambda_\sigma - \Lambda_1) \Psi(p) ds(p)$$

3. Solve the  $\bar{\partial}$  equation for  $\mu(p, \zeta)$ ;

$$\partial \mu / \partial \bar{k} = \frac{1}{4\pi k} t(k) \exp(i(\zeta + \bar{\zeta}) \cdot p) \bar{\mu}(p, k)$$

4. Take  $\lim_{k \rightarrow 0} \mu(p, \zeta) = \sigma^{1/2}(p)$

5. Display  $\sigma$ .

Does it Work?

# Numerical Simulation

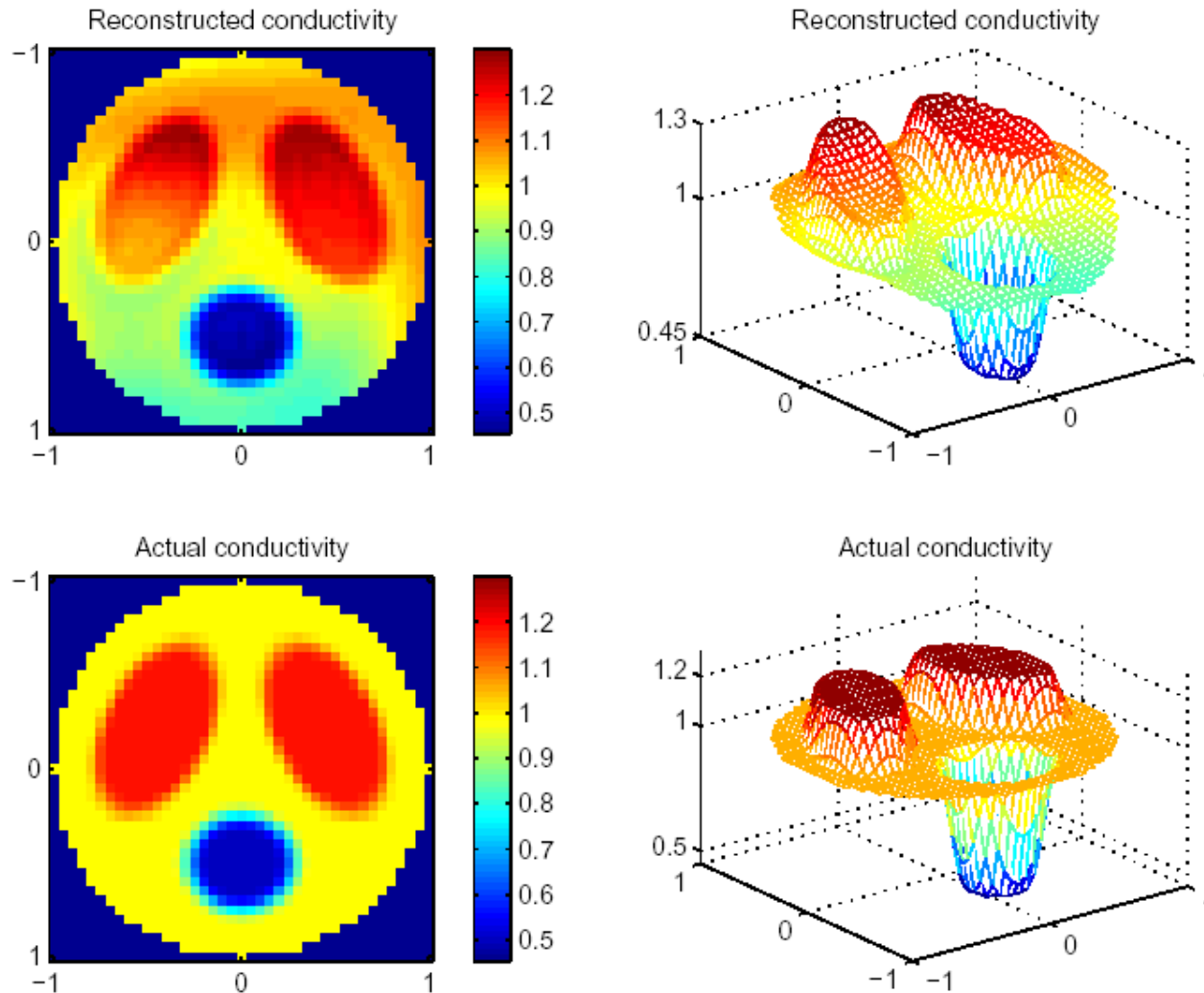
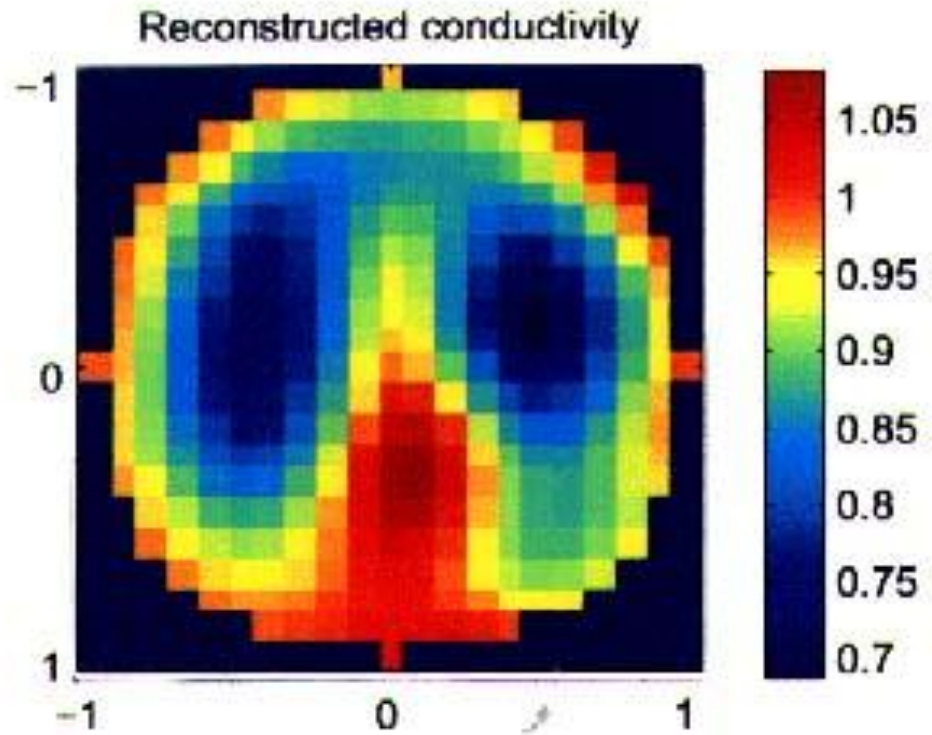
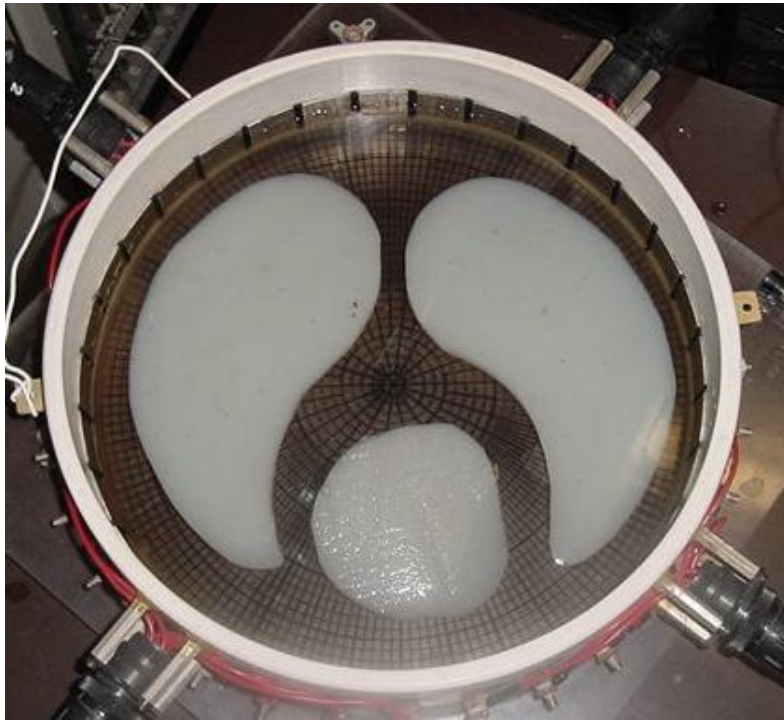
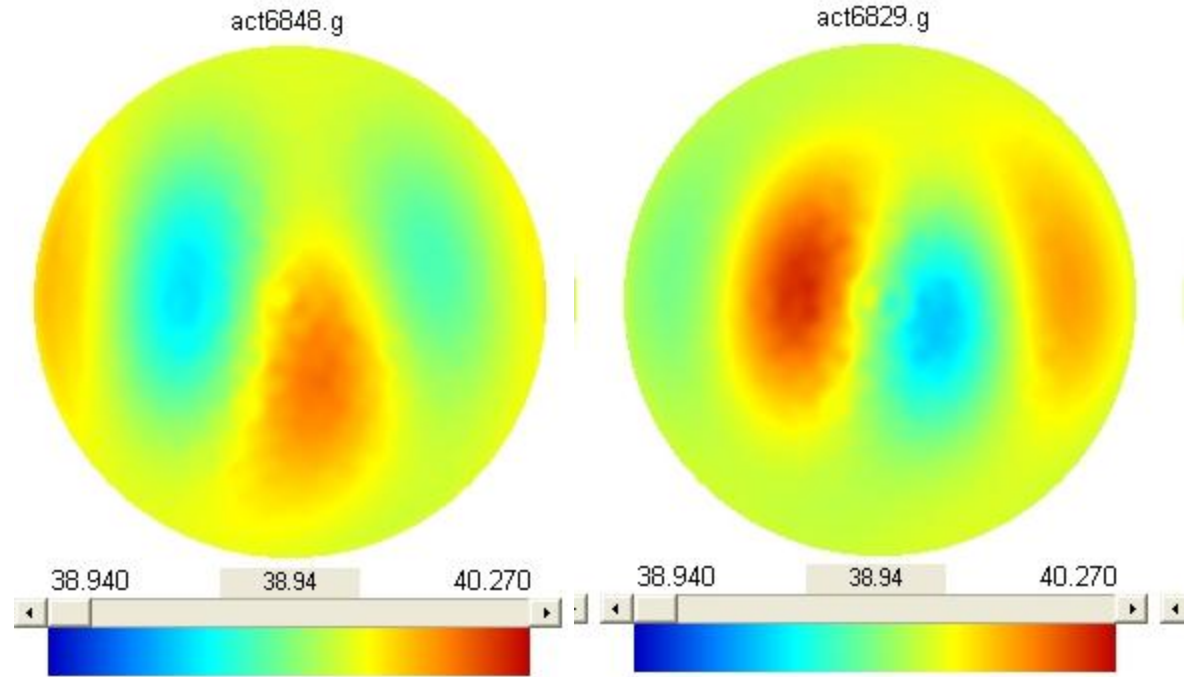


FIG. 5.2. Plots of the actual and reconstructed conductivities for the virtual phantom chest.

# First D-Bar Reconstruction Results from Experimental Data



# First D-Bar Cardiac Images



Changes in conductivity as heart expands (diastole) and contracts (systole) from one fixed moment in cardiac cycle.

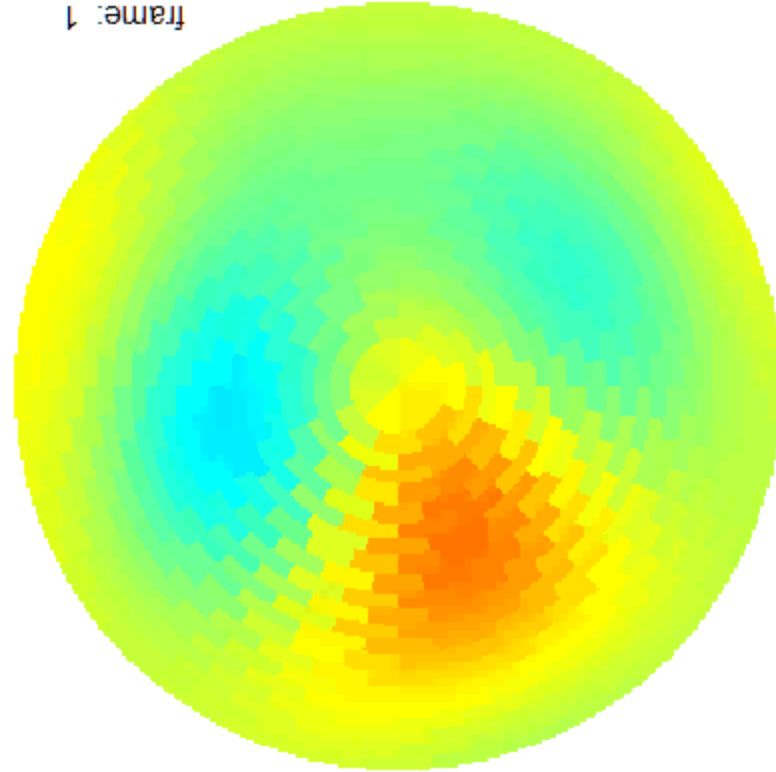
First blood fills enlarging heart (red) while leaving lungs (blue) . Then blood leaves contracting heart (blue) to fill lungs (red).

Reconstruction by D-bar. Data by ACT3.





frame: 1



Click on the image at right to see a movie of changes in the conductivity inside a chest during the cardiac cycle. Differences shown in the movie are all from one moment in the cycle. The movie starts with the heart filling and the lungs emptying.

Reconstruction by D-Bar. Data from ACT3.

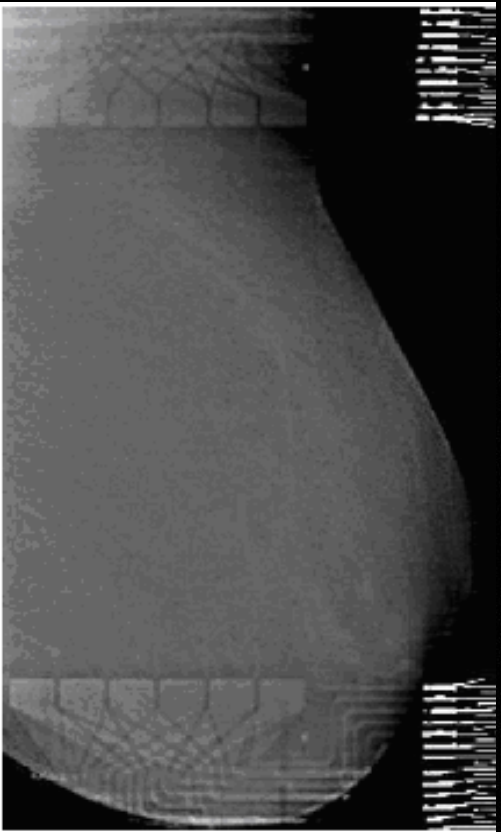
# Problems:

- How to make D-bar method work better with experimental data?
- How to make it work in 3-D?
- How to make D-bar work with Optical, Acoustic, and Microwave Data?

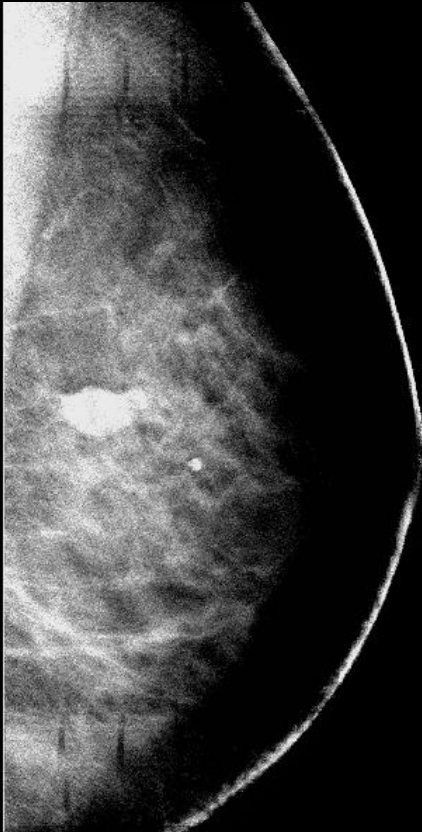
Can EIT Improve Sensitivity and  
Specificity in screening for  
Breast Cancer  
?

# Breast Cancer Problem

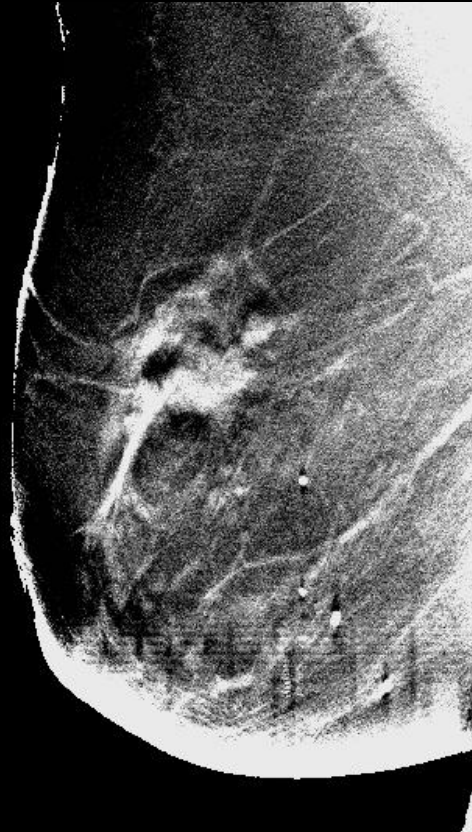
Which ones have cancer ?



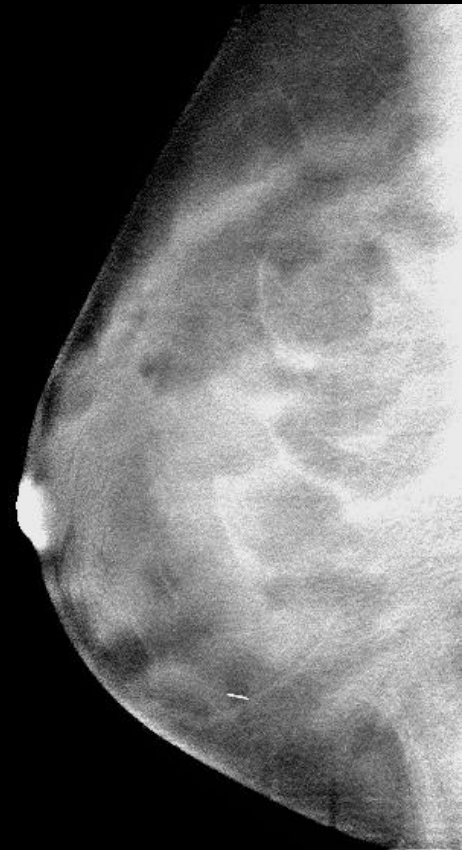
HS14R



HS21R



HS25L



HS10L

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# Electrical Impedance Tomography with Tomosynthesis for Breast Cancer Detection

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**Jonathan Newell**

**With:**

**David Isaacson  
Tzu-Jen Kao  
Richard Moore\***

**Gary J. Saulnier  
Greg Boverman  
Daniel Kopans\***

**And:**

Rujuta Kulkarni  
Dave Ardrey

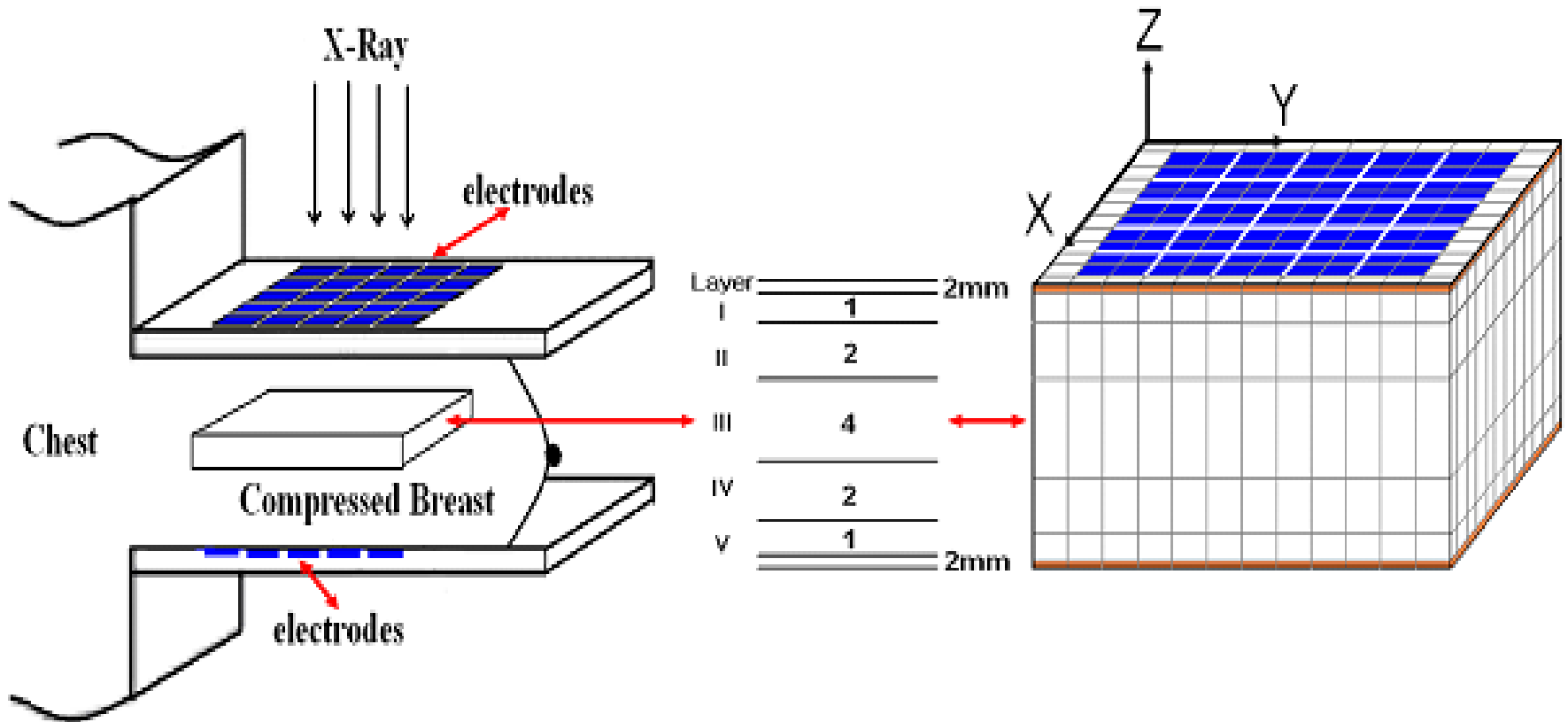
Chandana Tamma  
Neha Pol

Rensselaer Polytechnic Institute

\*Massachusetts General Hospital



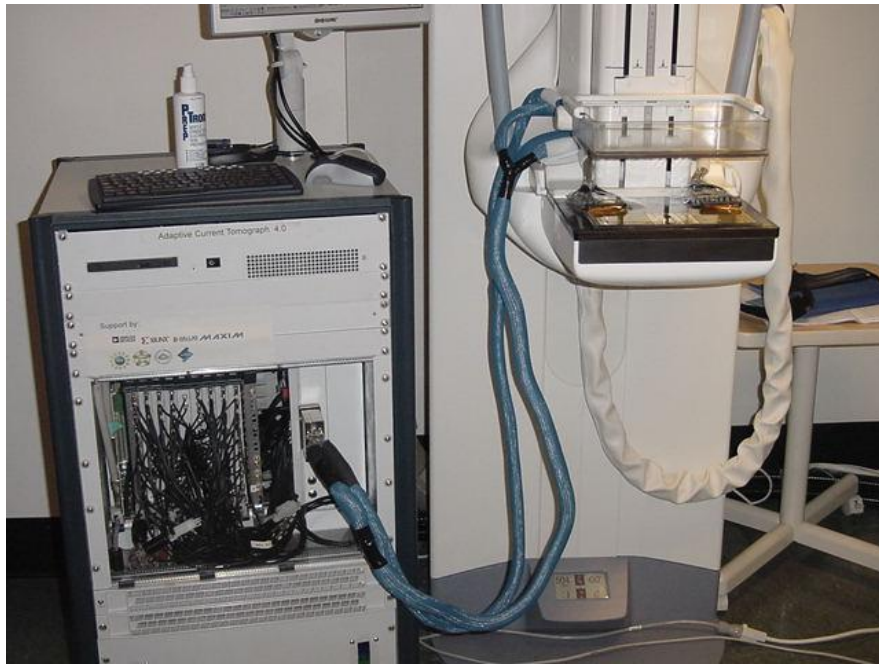
# EIT electrodes added to mammography machine.



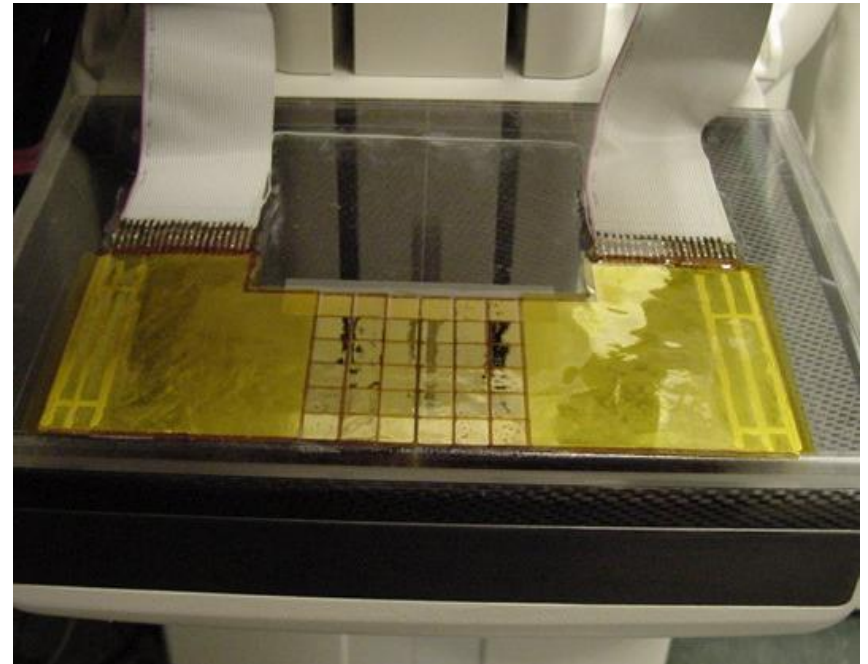
- 1 : 2 : 4 : 2 : 1 is the ratio of the mesh thicknesses.
- Only the center layer, III, is displayed in the results.



# EIT Instrumentation



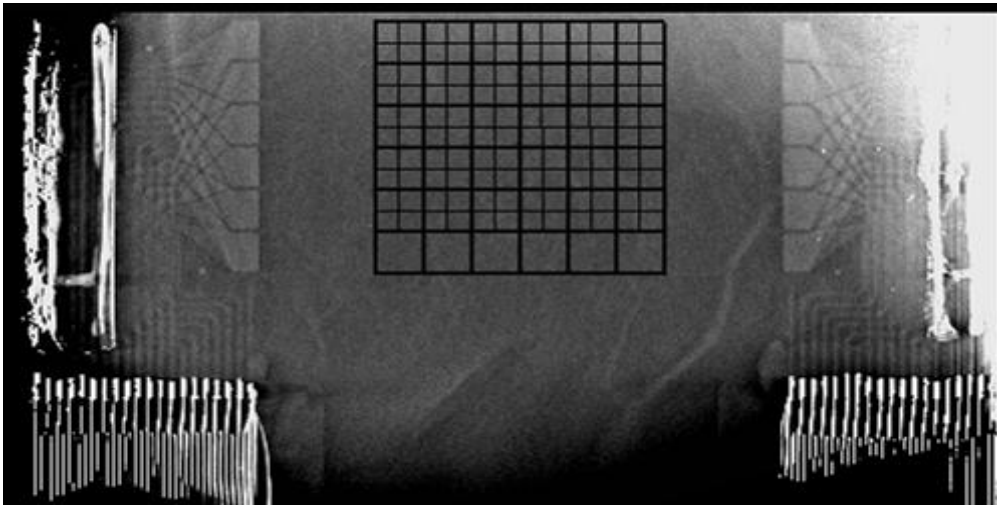
ACT 4 with Tomosynthesis unit



Radiolucent electrode array



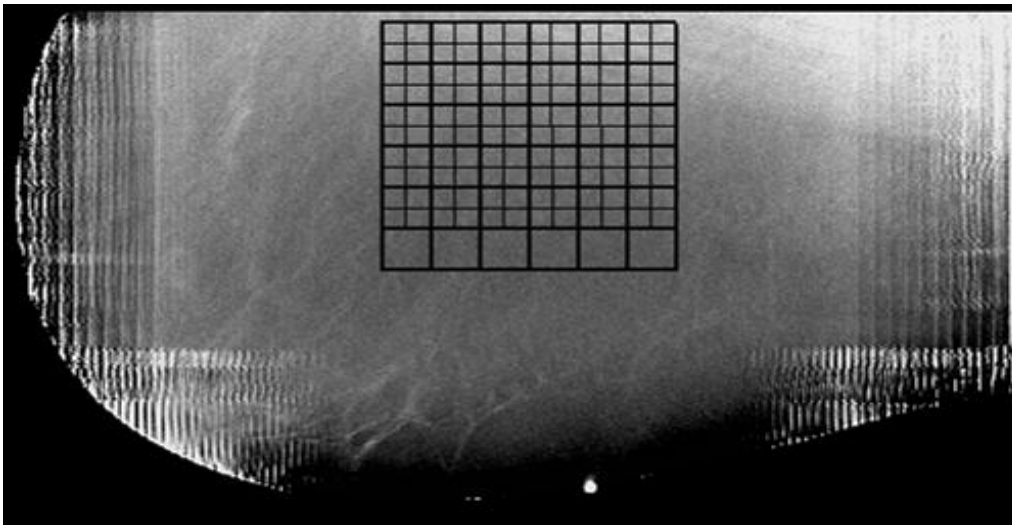
# Co-registration of EIT and Tomo Images



To find the electrode position, display the slice containing the electrodes.  
Superimpose the mesh grid with correct scale.

Slice 15 of 91

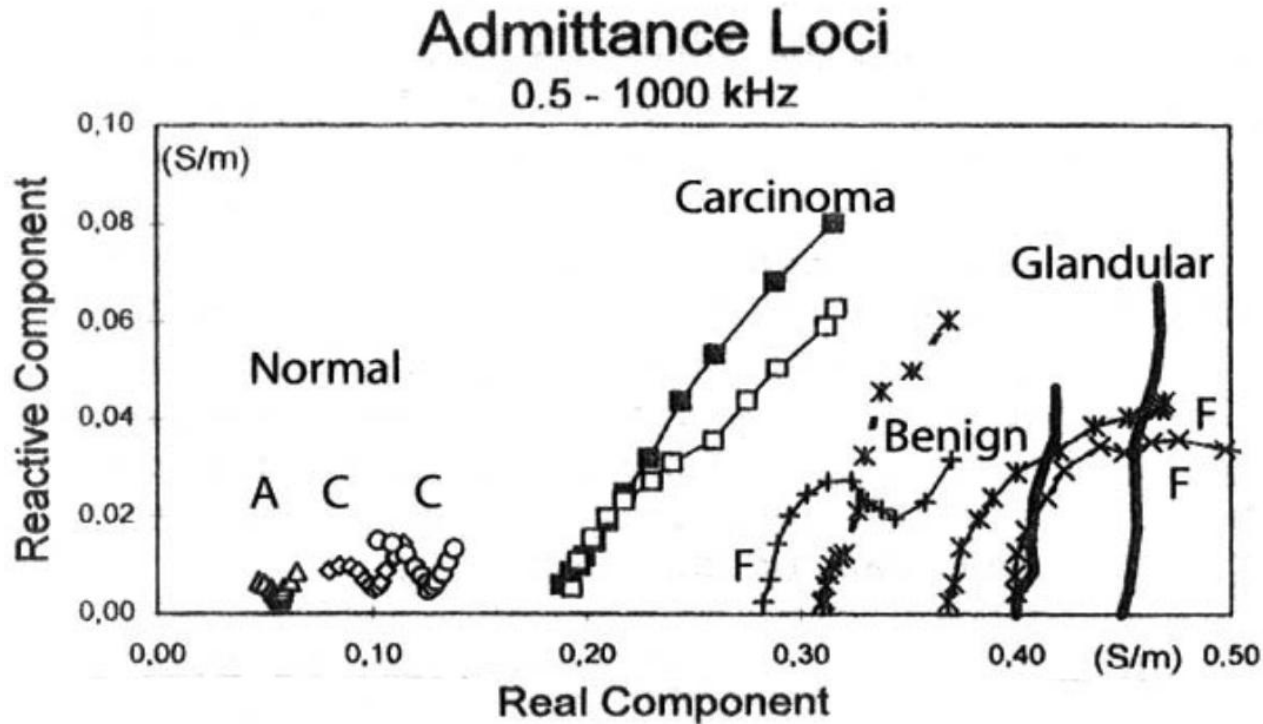
HS\_14R  
Normal



Then select the desired tomosynthesis layer.

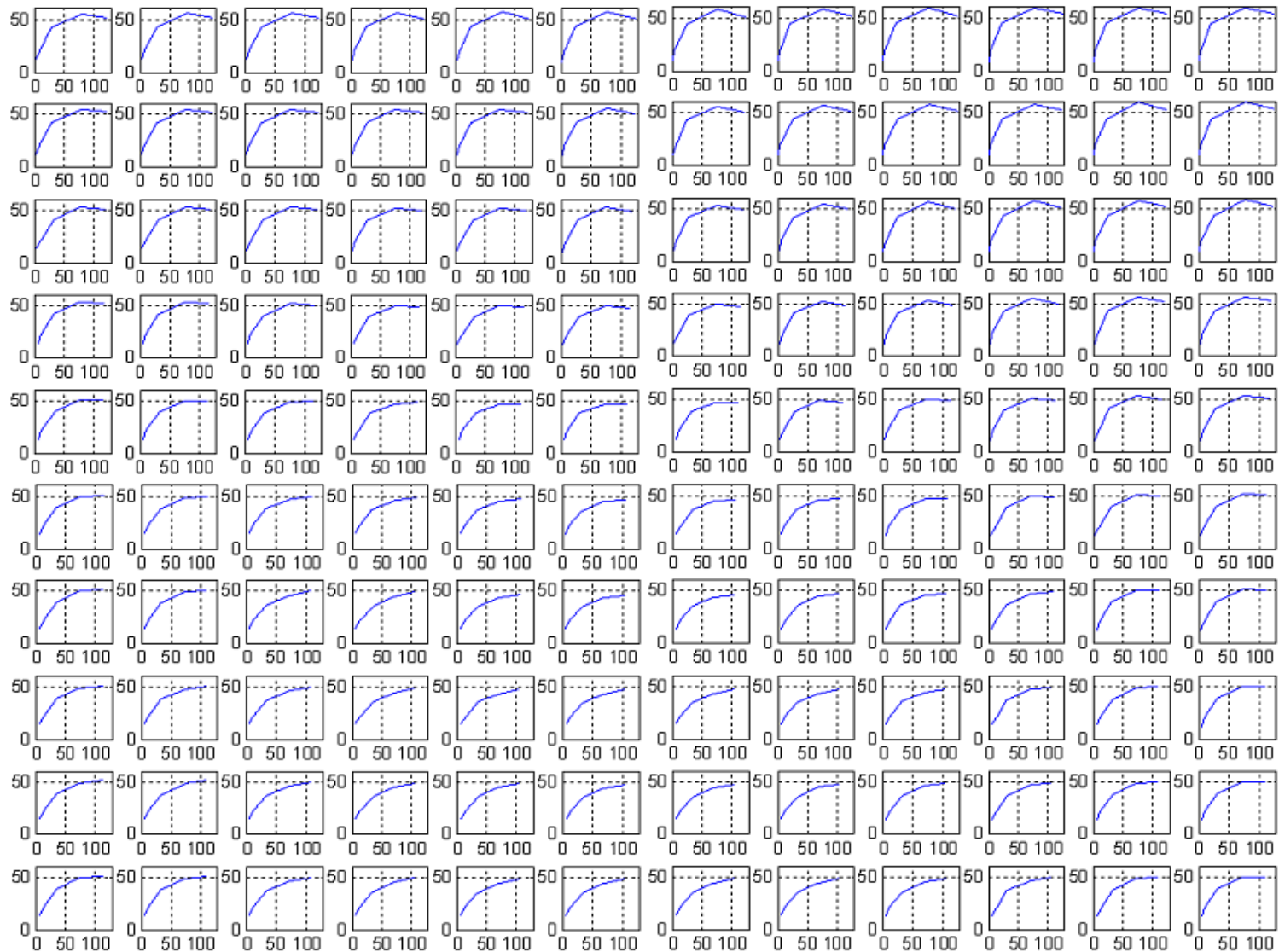
Slice 50 of 91

# Admittance Loci: format for summaries of EIS data

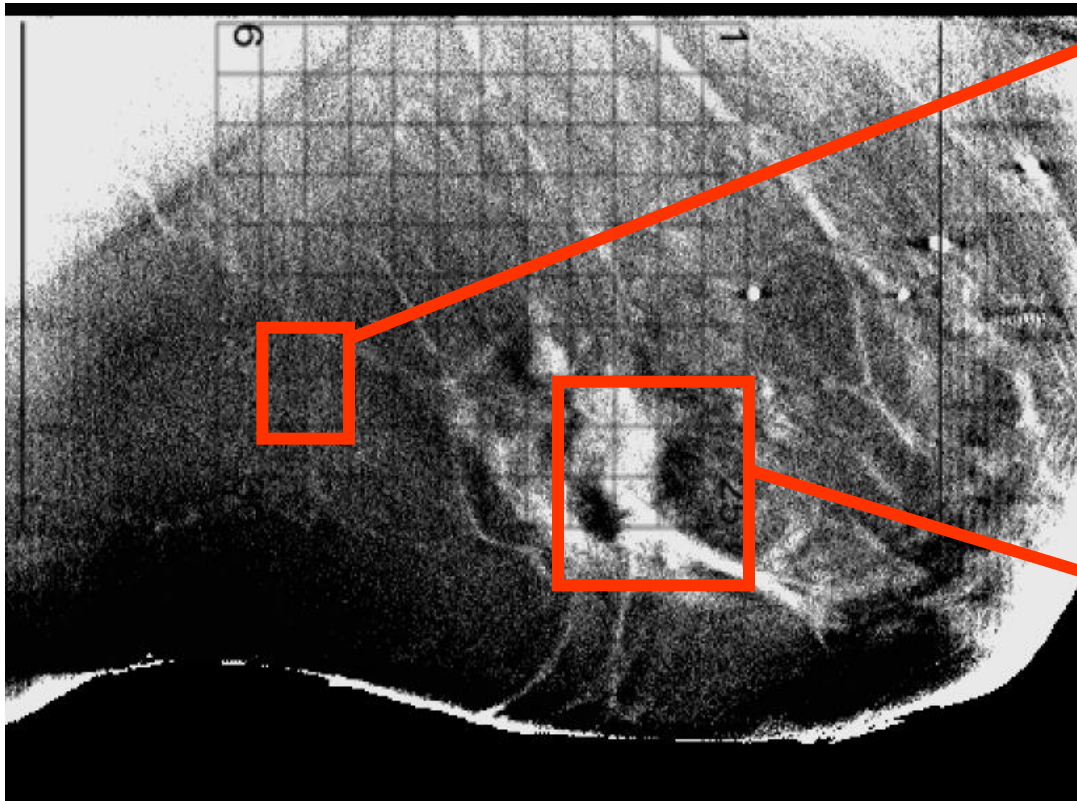


Results of in-vitro studies of excised breast tissue. *Jossinet & Schmitt 1999*

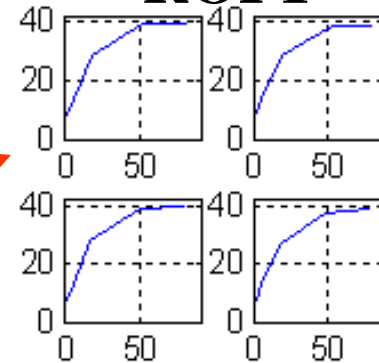
# 120 EIS plots for a normal breast (HS14\_Right)



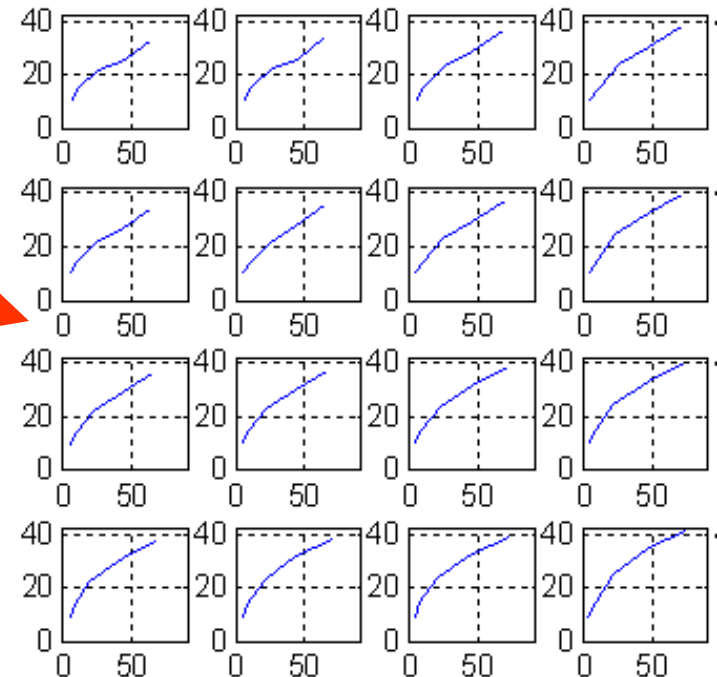
# HS25\_L: Invasive Ductal Carcinoma



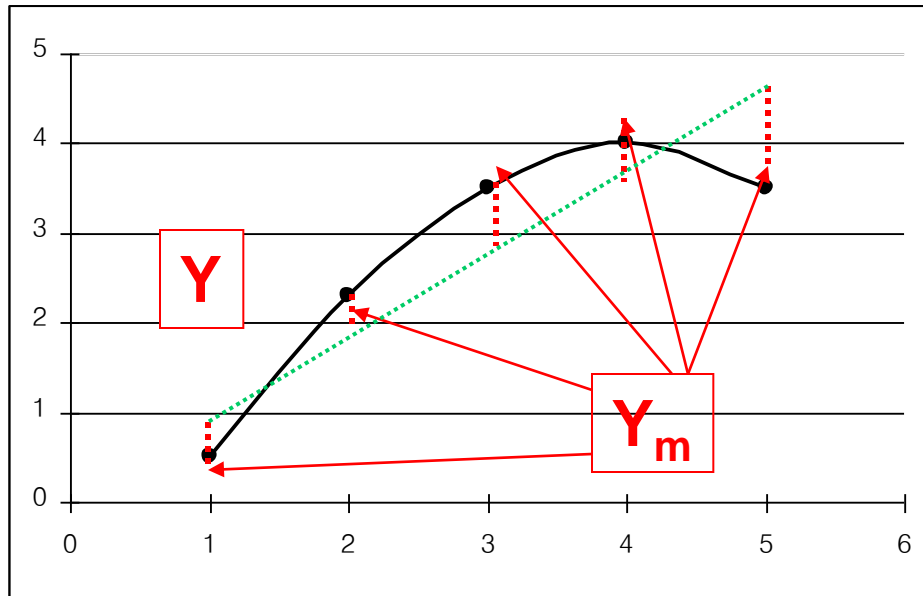
**ROI 1**



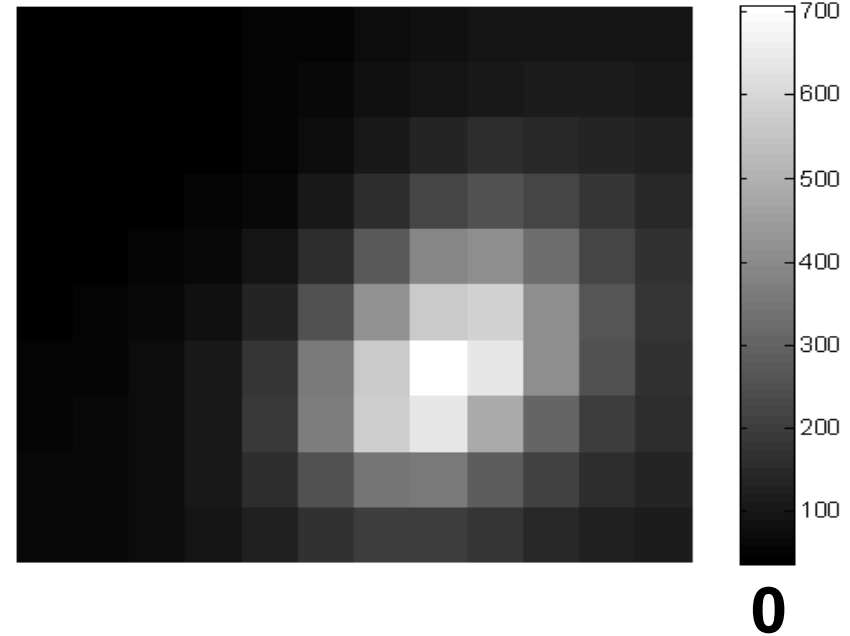
**ROI 2**



# Linear Correlation Measure –LCM



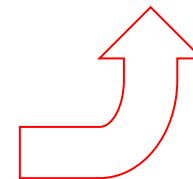
LCM Image



$$LCM = \frac{1}{1 - \frac{|\langle Y, Y_m \rangle|}{\|Y\| \|Y_m\|}}$$

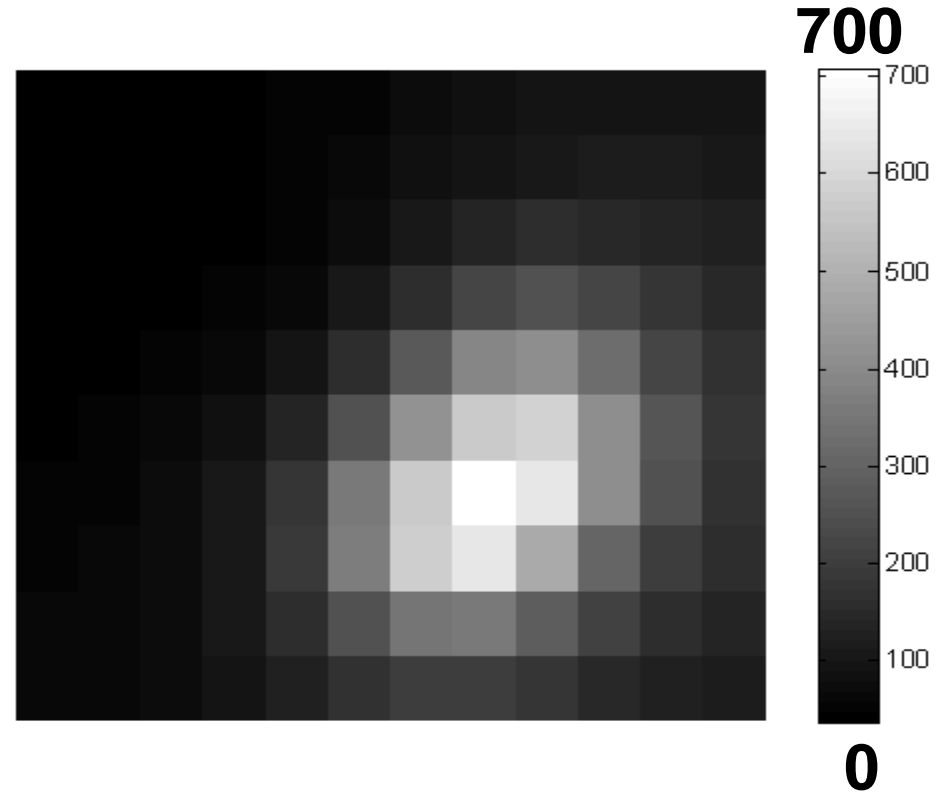
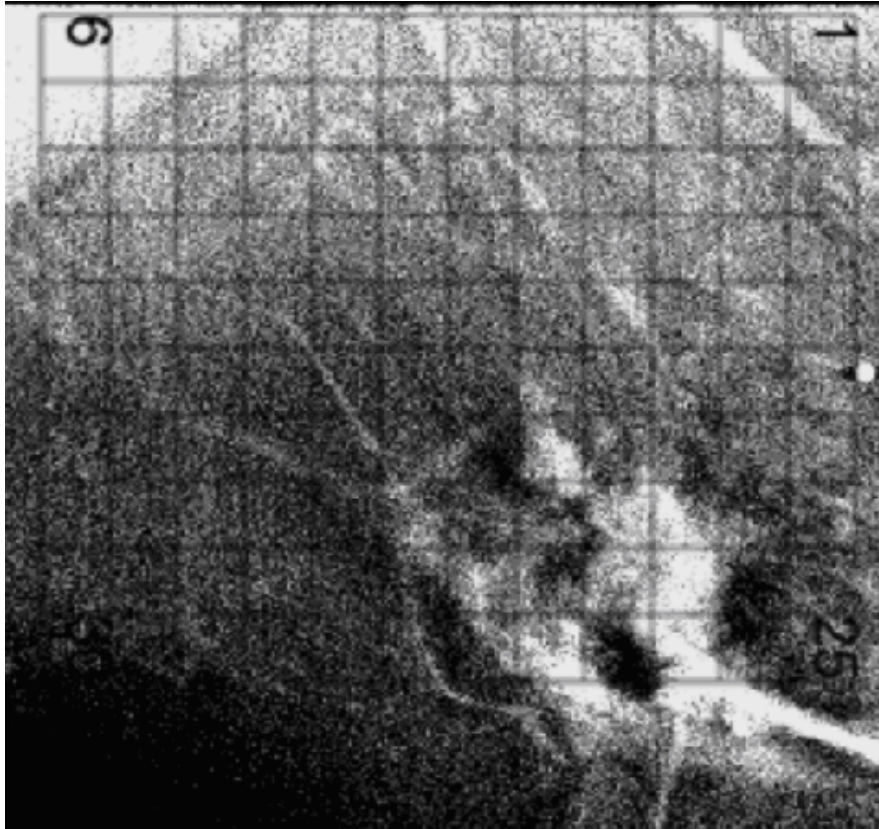


compute for  
each voxel



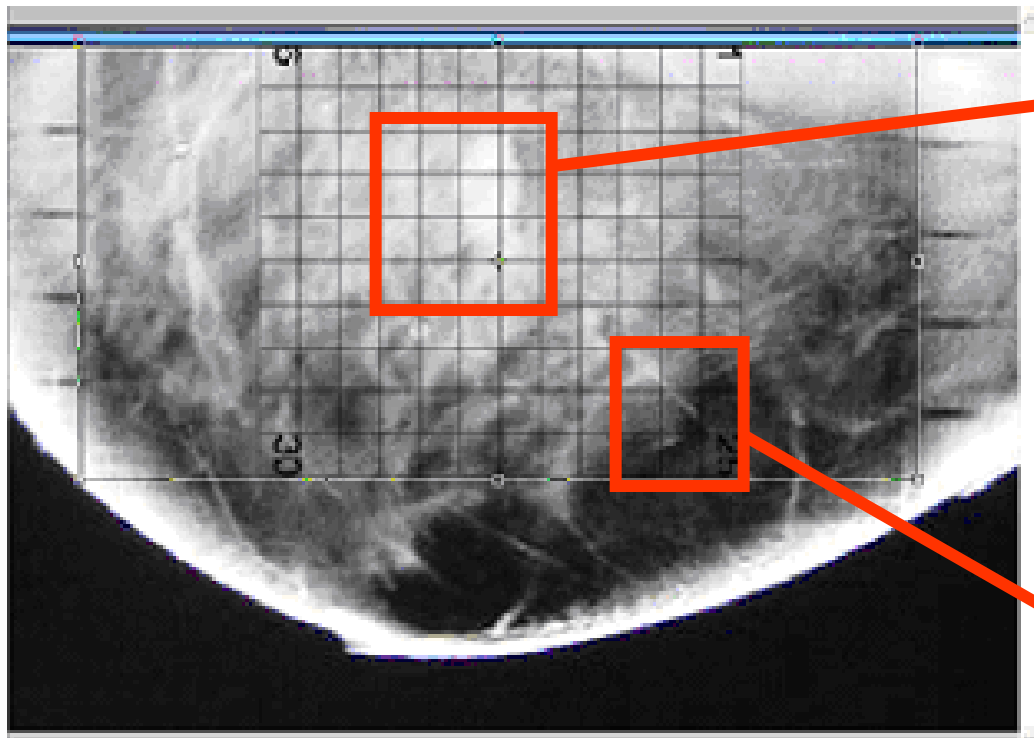


# LCM Image of invasive ductal CA (HS25\_L)

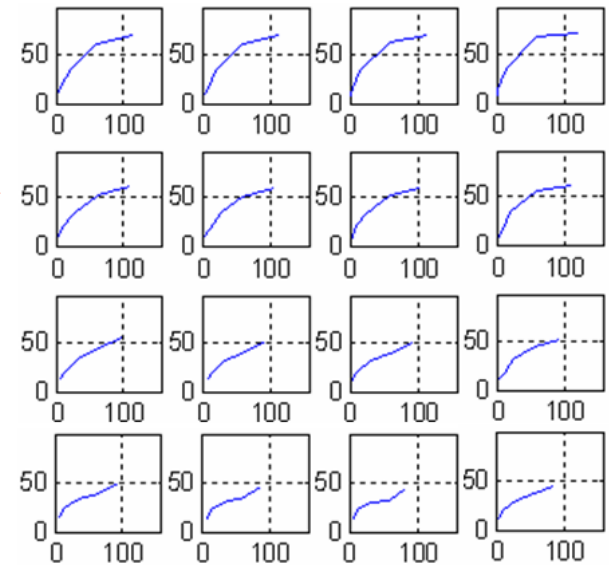


**Gray scale image of LCM**

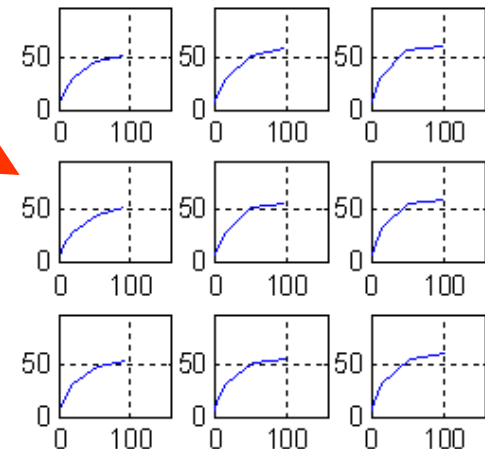
# HS21\_R: Fibroadenoma in the upper box



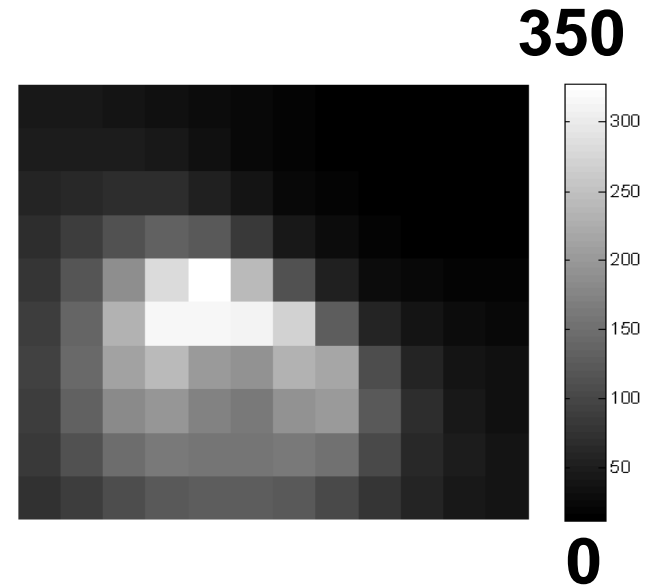
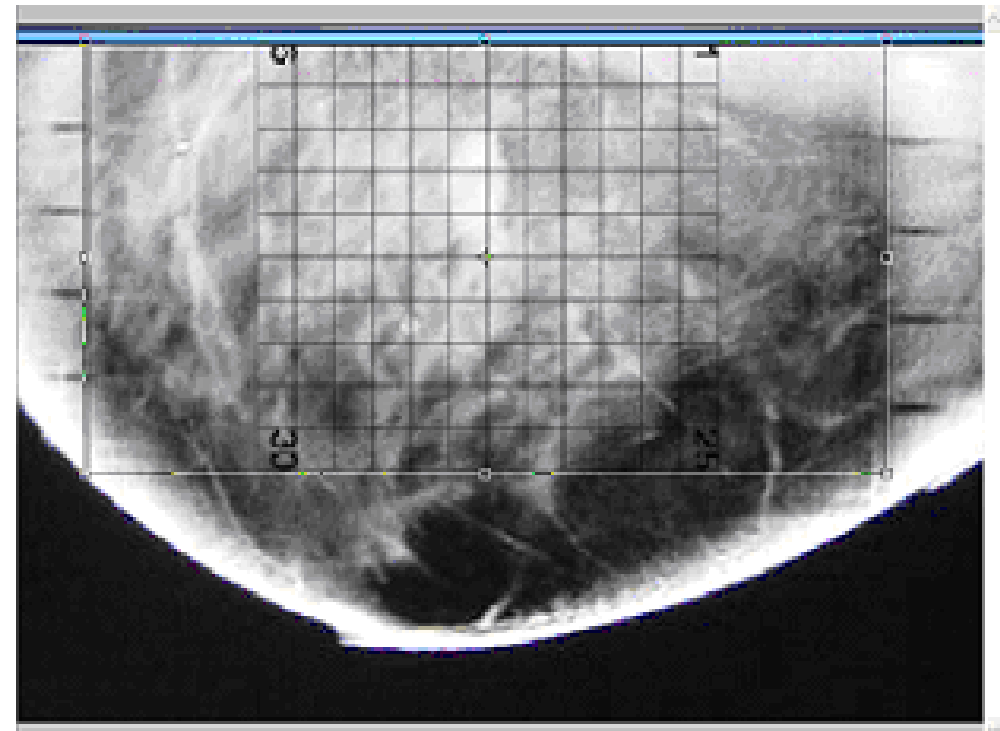
## ROI 1



## ROI 2



# LCM Image of fibroadenoma (HS21\_R)

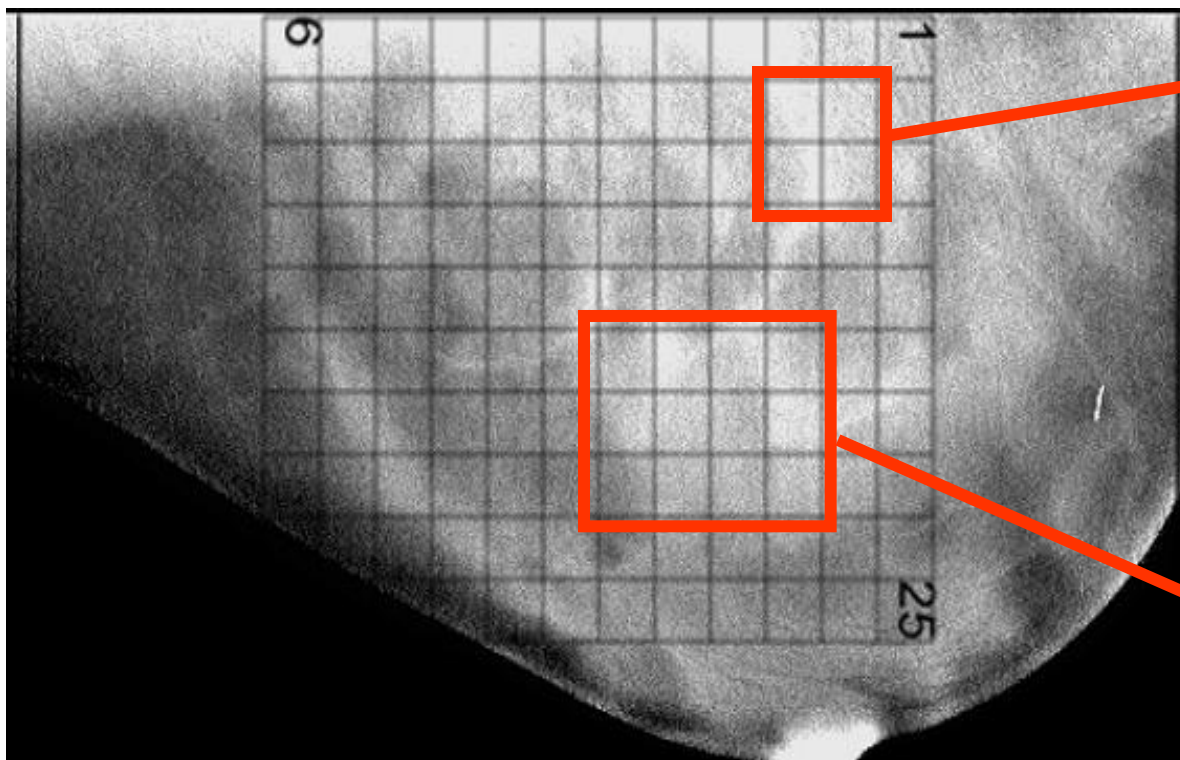


**Gray scale image of LCM**

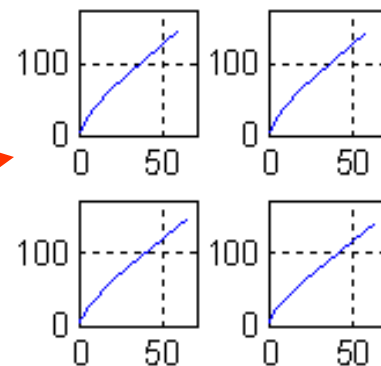


# HS10\_L: Invasive Ductal CA

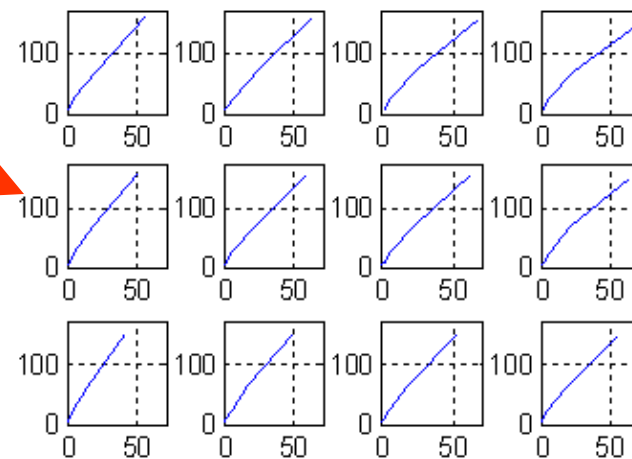
“Proliferation is worrisome”



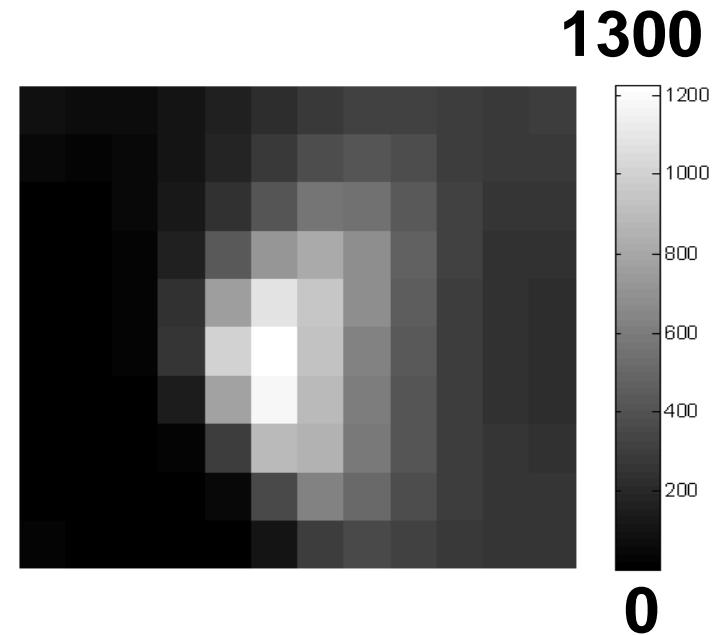
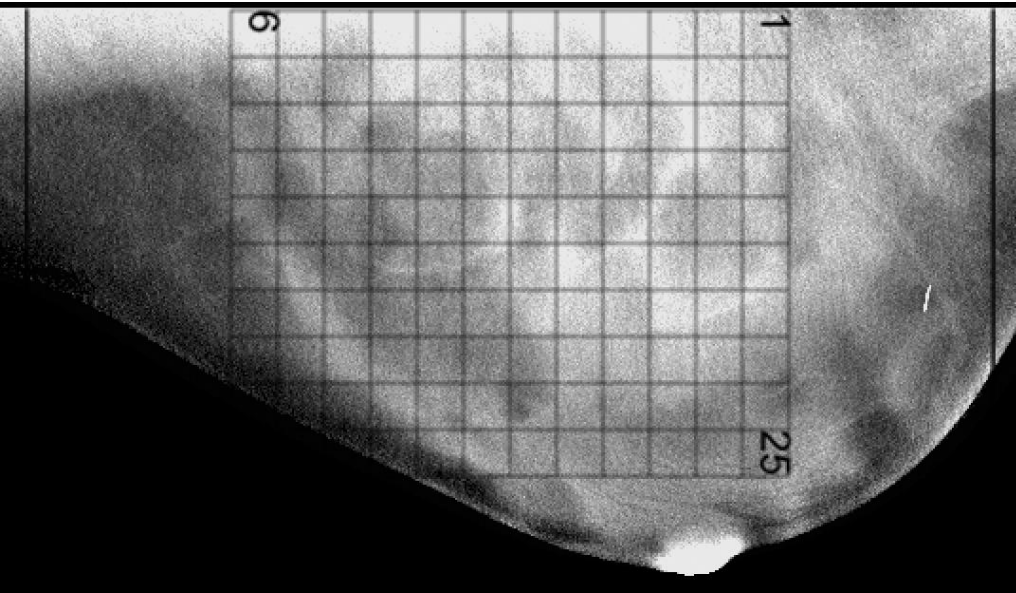
## ROI 1



## ROI 2

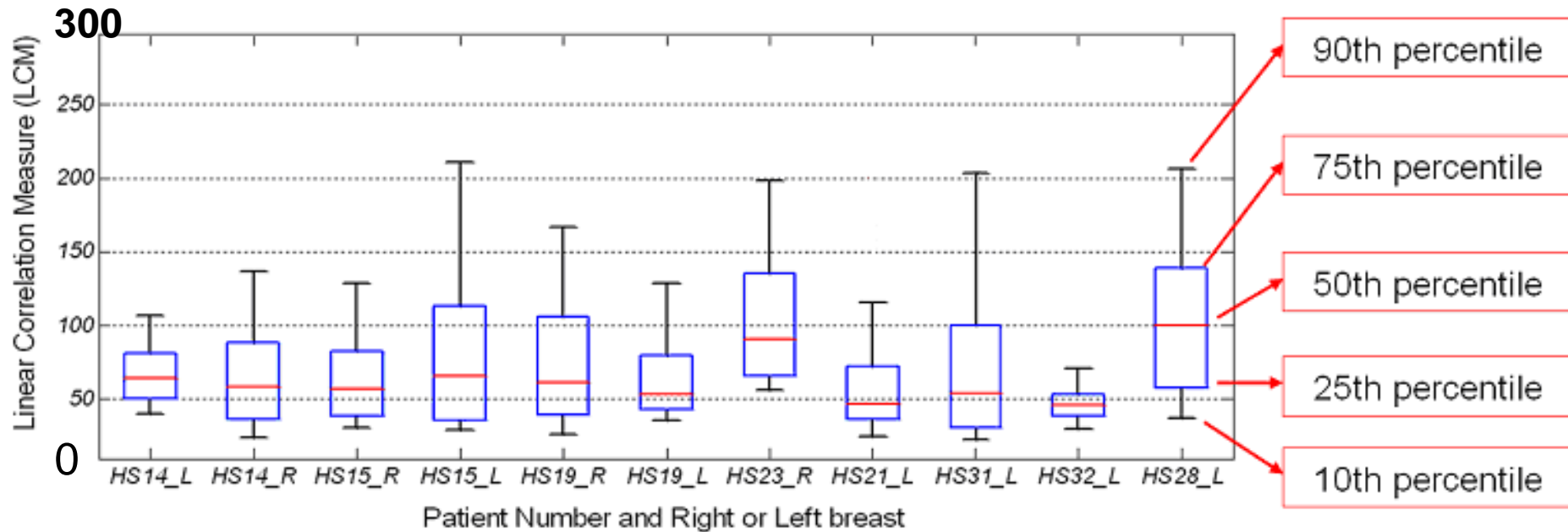


# LCM Image of invasive ductal CA (HS10\_L)



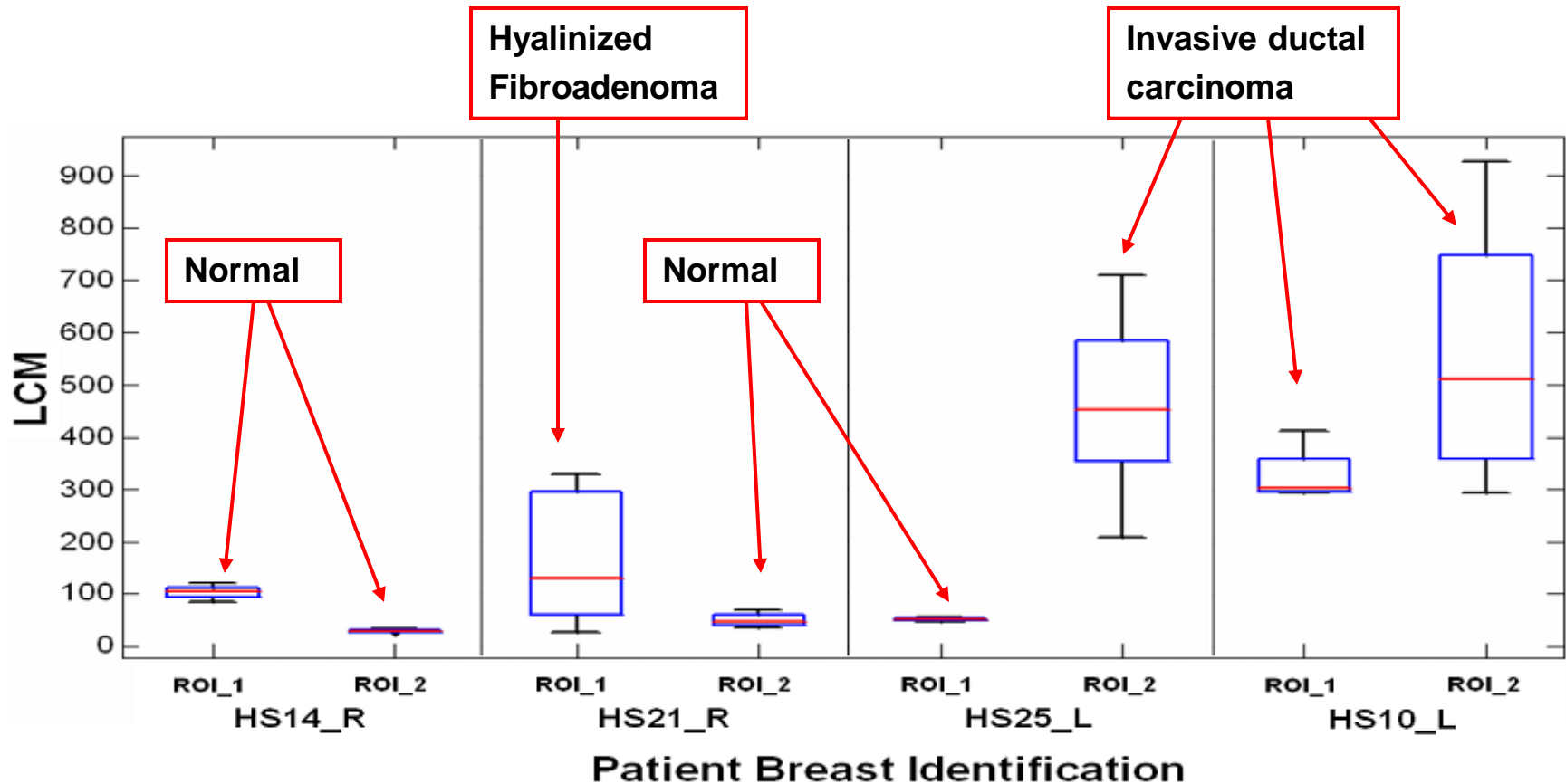
**Gray scale image of LCM**

# LCM for 11 normal breasts



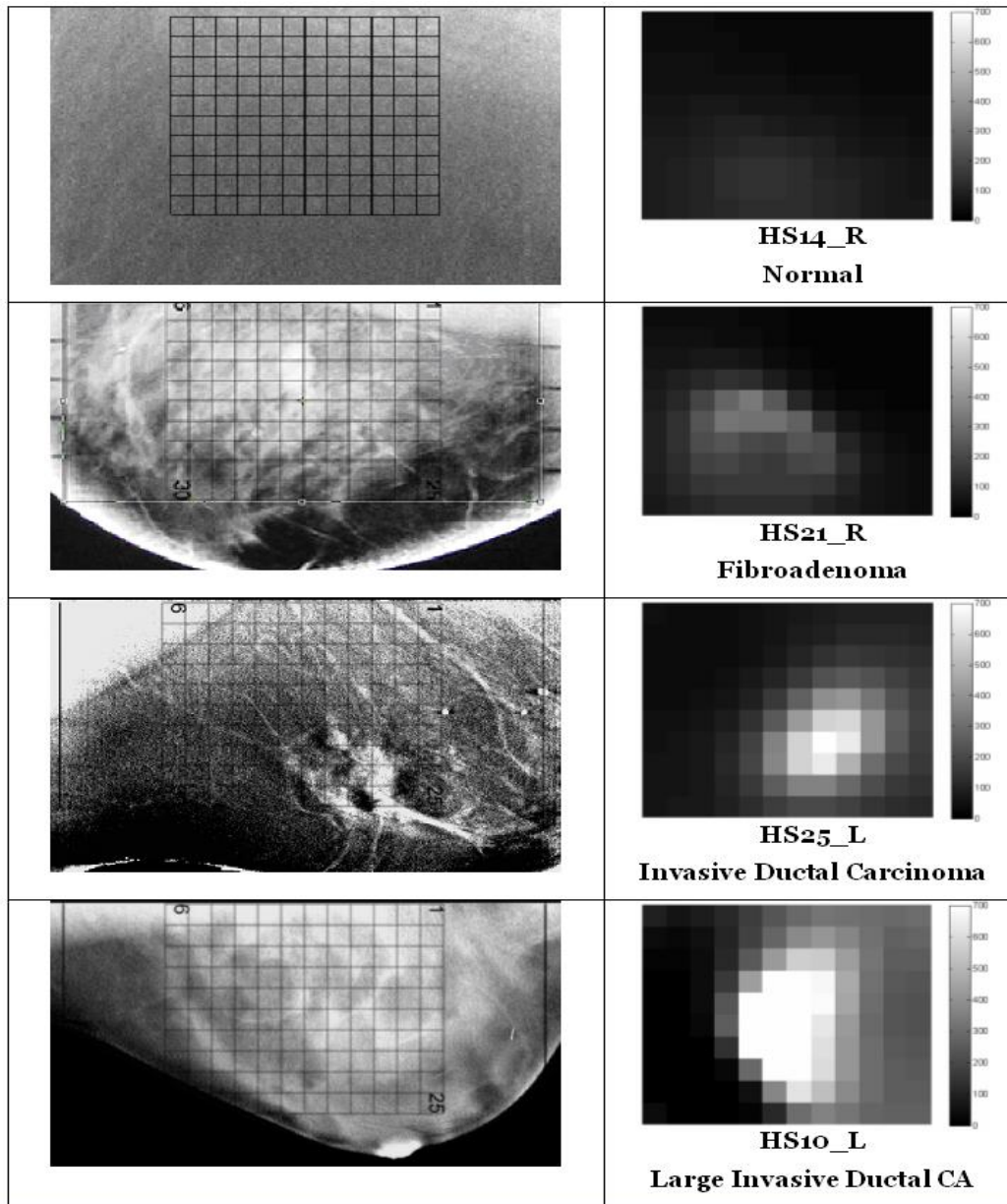
There are 120 EIS plots for layer 3 in each patient. The distribution of the LCM parameter in these plots is shown.

# LCM for the regions of interest in 4 patients



The distributions of the LCM for the regions of interest identified. Note the LCM values are much larger for voxels associated with the malignant lesions.

# LCM on the same scale



Normal Breast

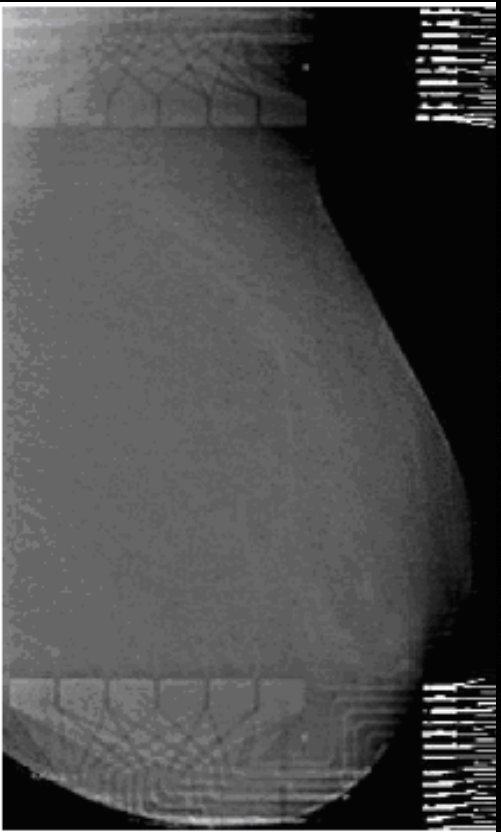
Fibroadenoma

Invasive Ductal  
Carcinoma

Invasive Ductal  
Carcinoma



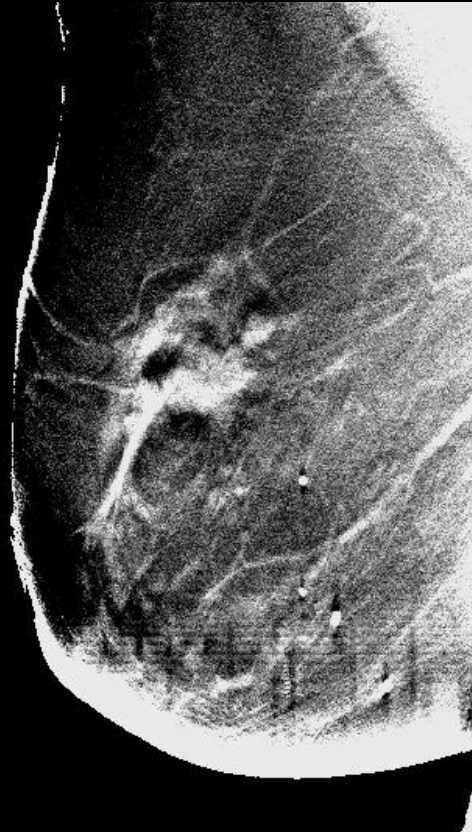
Which ones have cancer ?



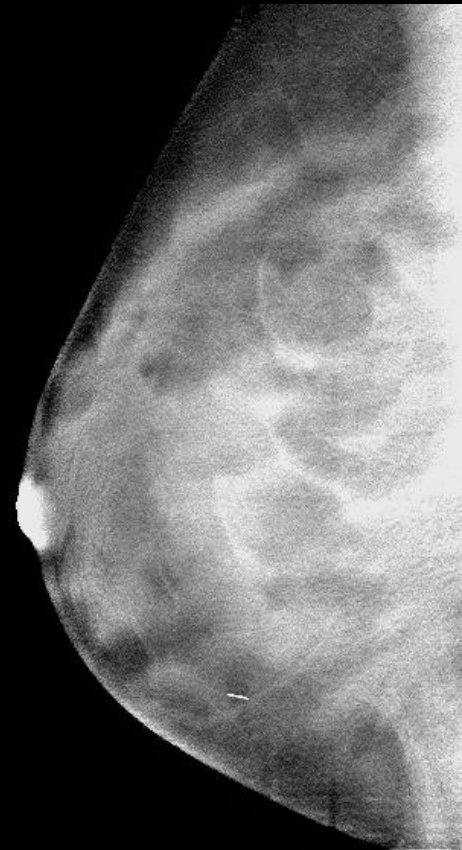
HS14R



HS21R



HS25L



HS10L

Which ones have cancer ?



HS14L

LCM=137



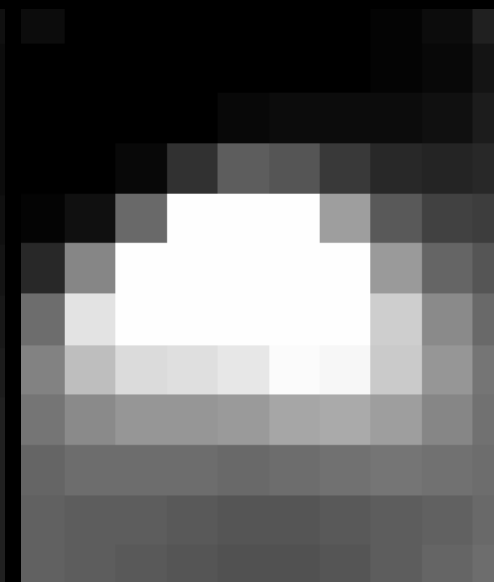
HS21L

LCM=328



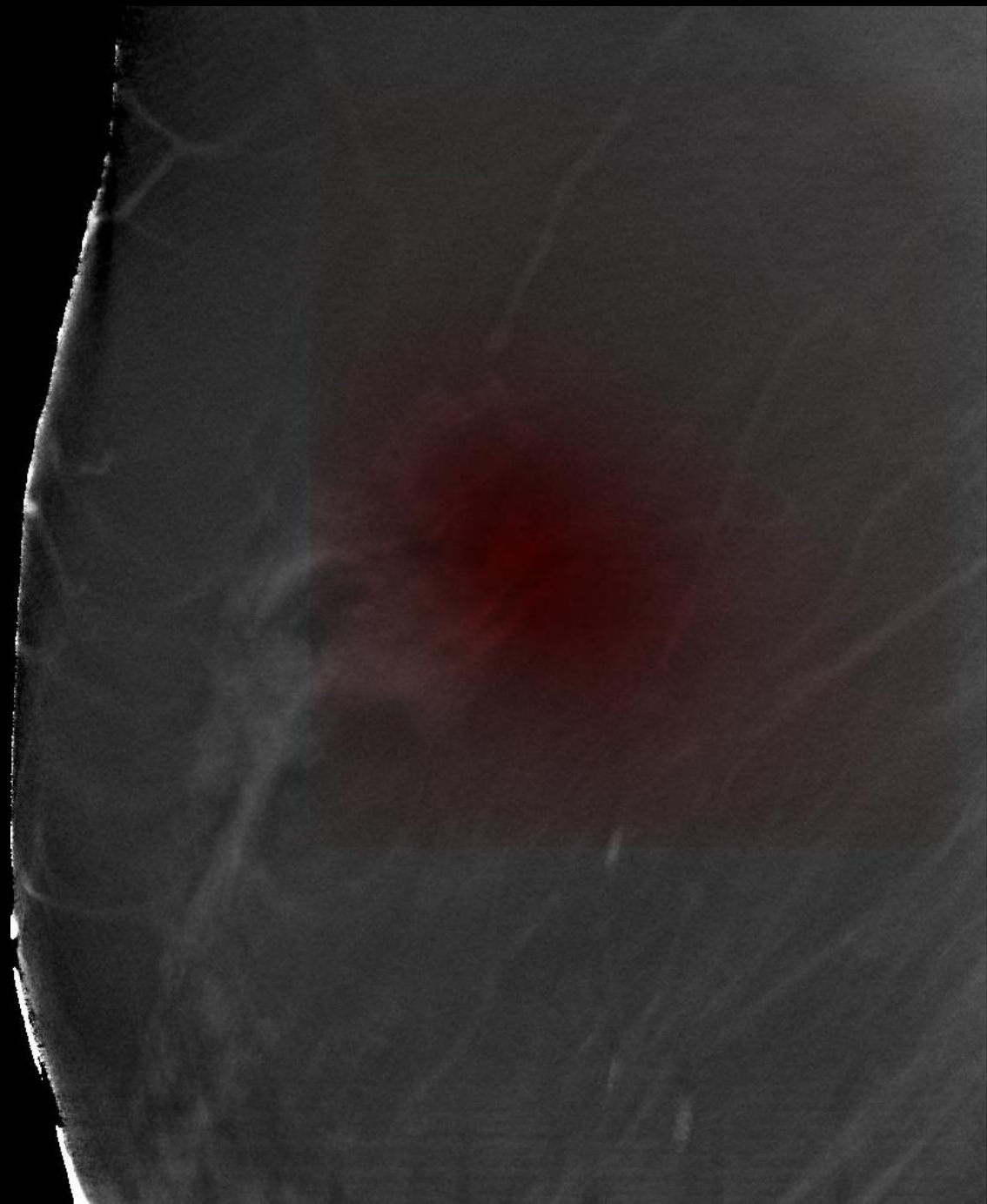
HS25R

LCM=709



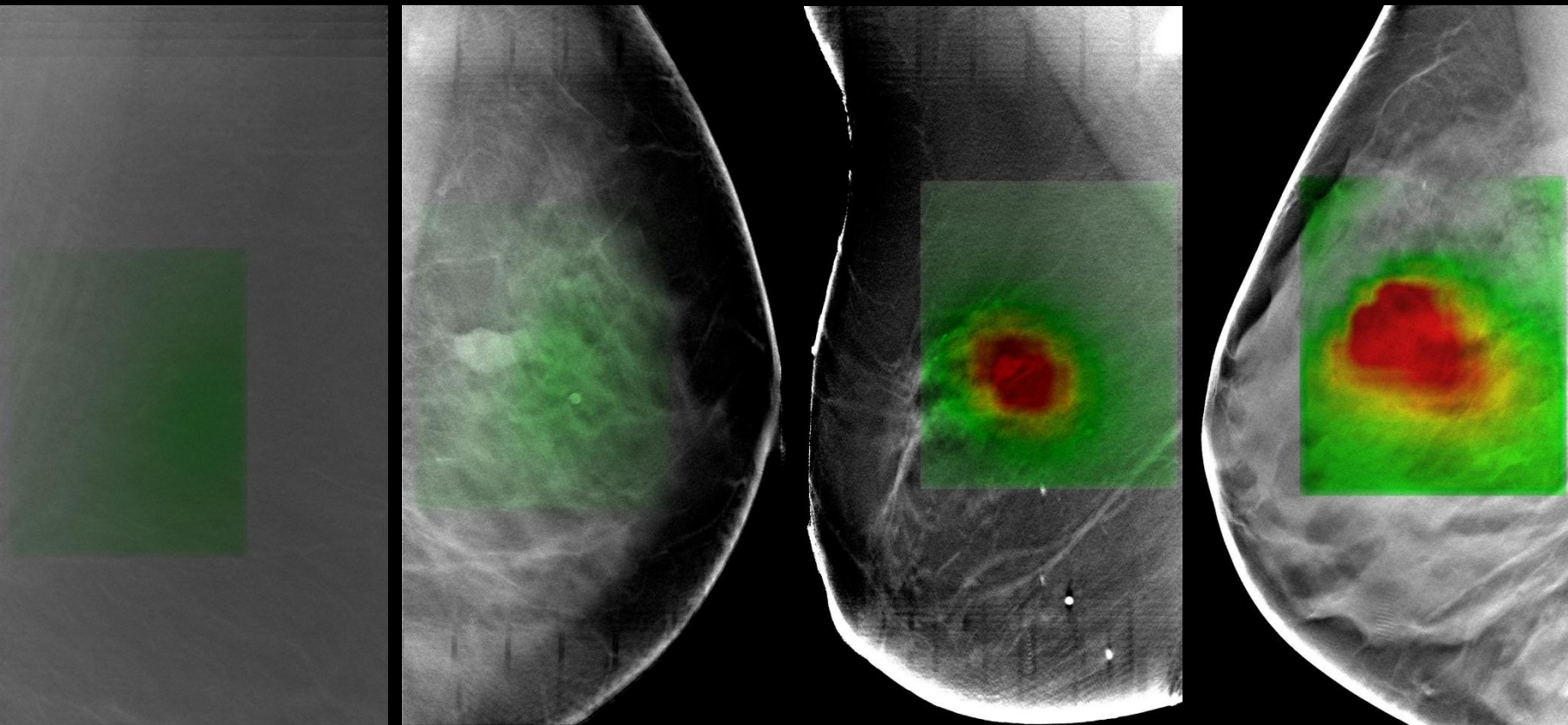
HS10R

LCM=1230





Which ones have cancer?



HS14R

HS21R

HS25L

HS10L



Can EIT Improve Sensitivity and  
Specificity in screening for  
Breast Cancer  
?

Questions and Suggestions  
Happily Received by

[isaacd@rpi.edu](mailto:isaacd@rpi.edu)

Thank you,  
especially

J.M., M.C., P.M.