

# BLT-sets of $Q(4, 37)$

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# Chapter 1

## Summary

There are 7 BLT-sets.



## Chapter 2

# Invariants



## Chapter 3

# The BLT-Sets

### 3.1 Isomorphism Type 0

Stabilizer has order 3846816  
 Plane intersection type is 38  
 Plane invariant is

$$[ 38 ]$$

$$\frac{\rightarrow \mid 1_1}{38_0 \mid 1} \quad \frac{\downarrow \mid 1_1}{38_0 \mid 38}$$

$C_0 = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37\}_{38}$   
 $C_1 = \{0\}_1$

$$\frac{\rightarrow \mid 1_1}{38_0 \mid 1}$$

$$\frac{\downarrow \mid 1_1}{38_0 \mid 38}$$

$C_0 = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37\}_{38}$   
 $C_1 = \{0\}_1$

Column cell 1:

Order of the group that is induced on the object is 50616

Number of ancestors on 5-sets is 15.

Number of orbits on 5-sets is 15.

With 1 orbits on the object

Orbit lengths: 38

The points by ranks:

$i$	Rank	$i$	Rank	$i$	Rank	$i$	Rank
0	0	10	189	20	192	30	208
1	1	11	191	21	194	31	209
2	184	12	187	22	195	32	210
3	185	13	193	23	197	33	211
4	186	14	196	24	198	34	213
5	203	15	205	25	199	35	214
6	188	16	206	26	200	36	216
7	202	17	212	27	201	37	218
8	219	18	215	28	204		
9	217	19	190	29	207		

The points:

$$P_0 = (0, 1, 0, 0, 0)P_1 = (0, 0, 1, 0, 0)P_2 = (0, 1, 18, 36, 18)P_3 = (0, 1, 23, 18, 9)$$

$$P_4 = (0, 1, 2, 12, 6)P_5 = (0, 1, 8, 24, 12)P_6 = (0, 1, 17, 22, 11)P_7 = (0, 1, 35, 35, 36)$$

$$P_8 = (0, 1, 18, 1, 19)P_9 = (0, 1, 2, 25, 31)P_{10} = (0, 1, 19, 6, 3)P_{11} = (0, 1, 13, 23, 30)$$

$$P_{12} = (0, 1, 15, 9, 23)P_{13} = (0, 1, 32, 11, 24)P_{14} = (0, 1, 22, 17, 27)P_{15} = (0, 1, 6, 5, 21)$$

$$P_{16} = (0, 1, 5, 8, 4)P_{17} = (0, 1, 13, 14, 7)P_{18} = (0, 1, 17, 15, 26)P_{19} = (0, 1, 20, 21, 29)$$

$$P_{20} = (0, 1, 29, 4, 2)P_{21} = (0, 1, 24, 10, 5)P_{22} = (0, 1, 14, 3, 20)P_{23} = (0, 1, 5, 29, 33)$$

$$P_{24} = (0, 1, 6, 32, 16)P_{25} = (0, 1, 31, 30, 15)P_{26} = (0, 1, 8, 13, 25)P_{27} = (0, 1, 35, 2, 1)$$

$$P_{28} = (0, 1, 31, 7, 22)P_{29} = (0, 1, 22, 20, 10)P_{30} = (0, 1, 14, 34, 17)P_{31} = (0, 1, 24, 27, 32)$$

$$P_{32} = (0, 1, 32, 26, 13)P_{33} = (0, 1, 29, 33, 35)P_{34} = (0, 1, 20, 16, 8)P_{35} = (0, 1, 19, 31, 34)$$

$$P_{36} = (0, 1, 15, 28, 14)P_{37} = (0, 1, 23, 19, 28)$$



Stabilizer of order 3846816 is generated by:

$$g_1 = \begin{bmatrix} 19 & 0 & 0 & 0 & 0 \\ 0 & 18 & 0 & 0 & 0 \\ 0 & 0 & 18 & 0 & 0 \\ 0 & 0 & 0 & 18 & 0 \\ 0 & 0 & 0 & 0 & 18 \end{bmatrix}$$

with 1444 fixed points

$$g_2 = \begin{bmatrix} 30 & 0 & 0 & 0 & 0 \\ 0 & 16 & 0 & 0 & 0 \\ 0 & 0 & 10 & 0 & 0 \\ 0 & 0 & 0 & 7 & 0 \\ 0 & 0 & 0 & 0 & 7 \end{bmatrix}$$

with 4 fixed points

$$g_3 = \begin{bmatrix} 3 & 0 & 0 & 0 & 0 \\ 0 & 3 & 0 & 0 & 0 \\ 0 & 0 & 3 & 0 & 0 \\ 0 & 0 & 0 & 34 & 0 \\ 0 & 0 & 0 & 0 & 34 \end{bmatrix}$$

with 40 fixed points

$$g_4 = \begin{bmatrix} 18 & 0 & 0 & 0 & 0 \\ 0 & 9 & 0 & 0 & 0 \\ 0 & 0 & 36 & 0 & 0 \\ 0 & 0 & 0 & 18 & 0 \\ 0 & 0 & 0 & 0 & 18 \end{bmatrix}$$

with 40 fixed points

$$g_5 = \begin{bmatrix} 13 & 0 & 0 & 5 & 16 \\ 0 & 29 & 0 & 0 & 0 \\ 0 & 0 & 29 & 0 & 0 \\ 29 & 0 & 0 & 21 & 4 \\ 16 & 0 & 0 & 16 & 21 \end{bmatrix}$$

with 38 fixed points

$$g_6 = \begin{bmatrix} 19 & 0 & 0 & 24 & 25 \\ 0 & 31 & 0 & 0 & 0 \\ 0 & 34 & 31 & 1 & 19 \\ 6 & 19 & 0 & 31 & 6 \\ 25 & 1 & 0 & 24 & 31 \end{bmatrix}$$

with 2 fixed points

$$g_7 = \begin{bmatrix} 33 & 0 & 0 & 8 & 33 \\ 0 & 13 & 0 & 0 & 0 \\ 0 & 7 & 13 & 15 & 26 \\ 35 & 26 & 0 & 14 & 5 \\ 4 & 15 & 0 & 20 & 14 \end{bmatrix}$$

with 40 fixed points

$$g_8 = \begin{bmatrix} 33 & 0 & 0 & 36 & 19 \\ 0 & 16 & 29 & 21 & 29 \\ 0 & 0 & 16 & 0 & 0 \\ 28 & 0 & 29 & 31 & 32 \\ 18 & 0 & 21 & 17 & 31 \end{bmatrix}$$

with 38 fixed points

## 3.2 Isomorphism Type 1

Stabilizer has order 2888

Plane intersection type is  $19^2 3^{6498}$

Plane invariant is

$$\begin{bmatrix} 19 & 0 \\ 0 & 19 \end{bmatrix}$$

$$\begin{array}{c|c} \rightarrow & 2_1 \\ \hline 38_0 & 1 \end{array} \quad \begin{array}{c|c} \downarrow & 2_1 \\ \hline 38_0 & 19 \end{array}$$

$$C_0 = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37\}_{38}$$

$$C_1 = \{0, 1\}_2$$

$$\begin{array}{c|c} \rightarrow & 2_1 \\ \hline 38_0 & 1 \end{array}$$

$$\begin{array}{c|c} \downarrow & 2_1 \\ \hline 38_0 & 19 \end{array}$$

$$C_0 = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37\}_{38}$$

$$C_1 = \{0, 1\}_2$$

Column cell 1:

Order of the group that is induced on the object is 2888

Number of ancestors on 5-sets is 714.

Number of orbits on 5-sets is 714.

With 1 orbits on the object

Orbit lengths: 38

The points by ranks:

$i$	Rank	$i$	Rank	$i$	Rank	$i$	Rank
0	0	10	189	20	8639	30	35865
1	1	11	191	21	37417	31	29990
2	184	12	187	22	19559	32	18571
3	185	13	193	23	13531	33	14737
4	186	14	196	24	44012	34	19485
5	203	15	205	25	36359	35	48331
6	188	16	206	26	29138	36	9992
7	202	17	212	27	19058	37	44759
8	219	18	215	28	42031		
9	217	19	37558	29	16130		

The points:

$$P_0 = (0, 1, 0, 0, 0)P_1 = (0, 0, 1, 0, 0)P_2 = (0, 1, 18, 36, 18)P_3 = (0, 1, 23, 18, 9)$$

$$P_4 = (0, 1, 2, 12, 6)P_5 = (0, 1, 8, 24, 12)P_6 = (0, 1, 17, 22, 11)P_7 = (0, 1, 35, 35, 36)$$

$$P_8 = (0, 1, 18, 1, 19)P_9 = (0, 1, 2, 25, 31)P_{10} = (0, 1, 19, 6, 3)P_{11} = (0, 1, 13, 23, 30)$$

$$P_{12} = (0, 1, 15, 9, 23)P_{13} = (0, 1, 32, 11, 24)P_{14} = (0, 1, 22, 17, 27)P_{15} = (0, 1, 6, 5, 21)$$

$$P_{16} = (0, 1, 5, 8, 4)P_{17} = (0, 1, 13, 14, 7)P_{18} = (0, 1, 17, 15, 26)P_{19} = (1, 15, 16, 6, 3)$$

$$P_{20} = (1, 16, 22, 34, 19)P_{21} = (1, 29, 26, 32, 3)P_{22} = (1, 27, 14, 12, 27)P_{23} = (1, 13, 4, 15, 31)$$

$$P_{24} = (1, 4, 24, 13, 21)P_{25} = (1, 16, 22, 1, 17)P_{26} = (1, 23, 27, 15, 35)P_{27} = (1, 23, 27, 33, 26)$$

$$P_{28} = (1, 32, 7, 24, 23)P_{29} = (1, 3, 18, 4, 14)P_{30} = (1, 36, 31, 17, 17)P_{31} = (1, 3, 18, 28, 2)$$

$$P_{32} = (1, 13, 4, 25, 26)P_{33} = (1, 29, 26, 6, 16)P_{34} = (1, 36, 31, 34, 27)P_{35} = (1, 32, 7, 9, 12)$$

$$P_{36} = (1, 4, 24, 5, 25)P_{37} = (1, 27, 14, 17, 6)$$

Stabilizer of order 2888 is generated by:

$$g_1 = \begin{bmatrix} 15 & 0 & 0 & 17 & 10 \\ 0 & 32 & 0 & 0 & 0 \\ 0 & 0 & 32 & 0 & 0 \\ 32 & 0 & 0 & 5 & 32 \\ 10 & 0 & 0 & 17 & 5 \end{bmatrix}$$

with 38 fixed points

$$g_2 = \begin{bmatrix} 19 & 0 & 0 & 24 & 25 \\ 0 & 6 & 0 & 0 & 0 \\ 0 & 0 & 6 & 0 & 0 \\ 31 & 0 & 0 & 12 & 34 \\ 12 & 0 & 0 & 25 & 12 \end{bmatrix}$$

with 1370 fixed points

$$g_3 = \begin{bmatrix} 22 & 0 & 0 & 19 & 9 \\ 0 & 10 & 0 & 0 & 0 \\ 0 & 18 & 10 & 26 & 13 \\ 23 & 13 & 0 & 21 & 3 \\ 28 & 26 & 0 & 12 & 21 \end{bmatrix}$$

with 40 fixed points

$$g_4 = \begin{bmatrix} 20 & 0 & 0 & 36 & 19 \\ 0 & 23 & 7 & 14 & 7 \\ 0 & 1 & 23 & 18 & 9 \\ 9 & 9 & 7 & 31 & 24 \\ 19 & 18 & 14 & 22 & 31 \end{bmatrix}$$

with 2 fixed points

$$g_5 = \begin{bmatrix} 22 & 0 & 0 & 19 & 9 \\ 0 & 0 & 23 & 0 & 0 \\ 0 & 14 & 0 & 0 & 0 \\ 23 & 0 & 0 & 31 & 8 \\ 28 & 0 & 0 & 32 & 31 \end{bmatrix}$$

with 40 fixed points

$$g_6 = \begin{bmatrix} 0 & 2 & 12 & 14 & 7 \\ 36 & 22 & 21 & 31 & 34 \\ 19 & 16 & 22 & 12 & 30 \\ 16 & 17 & 3 & 17 & 32 \\ 32 & 1 & 19 & 34 & 27 \end{bmatrix}$$

with 0 fixed points

### 3.3 Isomorphism Type 2

Stabilizer has order 4

Plane intersection type is  $5^8 4^{190} 3^{7596}$

Plane invariant is

$$\begin{bmatrix} 5 & 0 & 0 & 1 & 0 & 0 & 2 & 1 \\ 0 & 5 & 1 & 0 & 1 & 2 & 0 & 0 \\ 0 & 1 & 5 & 0 & 0 & 0 & 1 & 2 \\ 1 & 0 & 0 & 5 & 2 & 1 & 0 & 0 \\ 0 & 1 & 0 & 2 & 5 & 0 & 1 & 0 \\ 0 & 2 & 0 & 1 & 0 & 5 & 0 & 1 \\ 2 & 0 & 1 & 0 & 1 & 0 & 5 & 0 \\ 1 & 0 & 2 & 0 & 0 & 1 & 0 & 5 \end{bmatrix}$$

$$\begin{array}{c|c} \rightarrow & 8_1 \\ \hline 16_0 & 2 \\ 8_2 & 1 \\ 14_3 & 0 \end{array} \quad \begin{array}{c|c} \downarrow & 8_1 \\ \hline 16_0 & 4 \\ 8_2 & 1 \\ 14_3 & 0 \end{array}$$

$$C_0 = \{1, 2, 3, 4, 5, 7, 10, 12, 20, 21, 22, 24, 29, 30, 35, 36\}_{16}$$

$$C_1 = \{0, 1, 2, 3, 4, 5, 6, 7\}_8$$

$$C_2 = \{0, 6, 14, 19, 23, 27, 28, 33\}_8$$

$$C_3 = \{8, 9, 11, 13, 15, 16, 17, 18, 25, 26, 31, 32, 34, 37\}_{14}$$

$\rightarrow$	$4_1$	$4_{55}$	$4_2$	$4_{12}$	$4_{11}$	$4_{14}$	$2_{13}$	$4_{10}$	$4_{18}$	$4_{57}$	$4_{17}$	$4_{56}$	$4_{19}$	$4_{16}$	$4_{20}$	$4_{58}$	$4_{22}$	$4_{59}$	$4_{23}$	$4_{21}$	$4_{24}$	$4_{15}$	$2_{26}$	$4_{27}$	$4_{25}$
$4_0$	1	1	2	2	2	2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0
$4_4$	1	1	0	0	0	0	0	1	1	1	1	1	1	0	0	0	0	0	0	0	0	2	1	2	1
$4_5$	1	1	1	1	0	0	0	1	1	0	0	0	0	1	1	0	1	0	0	0	0	0	0	0	0
$4_{54}$	1	1	0	0	0	0	0	0	0	1	0	0	0	1	0	1	0	1	1	0	0	1	0	0	1
$4_3$	1	0	0	0	1	0	0	0	0	0	2	1	0	0	0	1	0	0	0	2	0	1	1	1	0
$4_{53}$	0	1	0	0	0	1	0	0	0	0	0	1	0	0	1	0	0	0	0	0	1	0	0	0	1
$4_6$	0	0	0	0	1	0	1	1	0	0	0	0	2	1	0	0	0	0	0	0	2	0	0	1	0
$4_7$	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	1	0	0	0	0	0
$4_9$	0	0	0	1	0	0	0	0	1	1	0	0	0	0	1	1	1	1	1	0	0	0	0	0	1
$2_8$	0	0	0	0	0	2	0	0	0	0	0	0	0	0	0	0	0	0	2	0	0	0	0	0	0
$\downarrow$	$4_1$	$4_{55}$	$4_2$	$4_{12}$	$4_{11}$	$4_{14}$	$2_{13}$	$4_{10}$	$4_{18}$	$4_{57}$	$4_{17}$	$4_{56}$	$4_{19}$	$4_{16}$	$4_{20}$	$4_{58}$	$4_{22}$	$4_{59}$	$4_{23}$	$4_{21}$	$4_{24}$	$4_{15}$	$2_{26}$	$4_{27}$	$4_{25}$
$4_0$	1	1	2	2	2	2	2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0
$4_4$	1	1	0	0	0	0	0	1	1	1	1	1	1	0	0	0	0	0	0	0	0	2	2	2	1
$4_5$	1	1	1	1	0	0	0	1	1	0	0	0	0	1	1	0	1	0	0	0	0	0	0	0	0
$4_{54}$	1	1	0	0	0	0	0	0	0	1	0	0	0	1	0	1	0	1	1	0	0	1	0	0	1
$4_3$	1	0	0	0	1	0	0	0	0	0	2	1	0	0	0	1	0	0	0	2	0	1	2	1	0
$4_{53}$	0	1	0	0	0	1	0	0	0	0	0	1	0	0	1	0	0	0	0	0	1	0	0	0	1
$4_6$	0	0	0	0	1	0	2	1	0	0	0	0	2	1	0	0	0	0	0	0	2	0	0	1	0
$4_7$	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	1	0	0	0	0	0
$4_9$	0	0	0	1	0	0	0	0	1	1	0	0	0	0	1	1	1	1	1	0	0	0	0	0	1
$2_8$	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0

- $C_0 = \{1, 5, 7, 30\}_4$
- $C_1 = \{10, 59, 102, 197\}_4$
- $C_2 = \{62, 103, 148, 191\}_4$
- $C_3 = \{0, 6, 19, 28\}_4$
- $C_4 = \{4, 20, 22, 35\}_4$
- $C_5 = \{2, 12, 21, 36\}_4$
- $C_6 = \{17, 26, 31, 34\}_4$
- $C_7 = \{11, 18, 25, 32\}_4$
- $C_8 = \{8, 37\}_2$
- $C_9 = \{9, 13, 15, 16\}_4$
- $C_{10} = \{13, 47, 67, 89\}_4$
- $C_{11} = \{6, 48, 66, 138\}_4$
- $C_{12} = \{28, 41, 115, 194\}_4$
- $C_{13} = \{63, 185\}_2$
- $C_{14} = \{40, 74, 113, 147\}_4$
- $C_{15} = \{94, 149, 155, 192\}_4$
- $C_{16} = \{26, 61, 98, 195\}_4$
- $C_{17} = \{76, 78, 87, 182\}_4$
- $C_{18} = \{49, 95, 124, 158\}_4$
- $C_{19} = \{20, 52, 119, 189\}_4$
- $C_{20} = \{51, 70, 104, 118\}_4$
- $C_{21} = \{69, 81, 123, 136\}_4$
- $C_{22} = \{45, 73, 105, 177\}_4$
- $C_{23} = \{30, 108, 110, 112\}_4$
- $C_{24} = \{14, 38, 71, 151\}_4$
- $C_{25} = \{86, 100, 133, 153\}_4$
- $C_{26} = \{93, 130\}_2$
- $C_{27} = \{3, 55, 72, 88\}_4$
- $C_{28} = \{97, 107, 126, 184\}_4$
- $C_{29} = \{19, 53, 154, 171\}_4$
- $C_{30} = \{75, 128, 134, 141\}_4$
- $C_{31} = \{91, 135, 144, 196\}_4$
- $C_{32} = \{33, 111, 140, 143\}_4$
- $C_{33} = \{56, 58, 96, 142\}_4$

$C_{34} = \{32, 85, 167, 186\}_4$   
 $C_{35} = \{18, 127, 132, 161\}_4$   
 $C_{36} = \{2, 23, 79, 137\}_4$   
 $C_{37} = \{173, 183\}_2$   
 $C_{38} = \{7, 16, 101, 160\}_4$   
 $C_{39} = \{11, 24, 34, 44\}_4$   
 $C_{40} = \{17, 29, 169, 181\}_4$   
 $C_{41} = \{129, 150\}_2$   
 $C_{42} = \{22, 92, 145, 178\}_4$   
 $C_{43} = \{57, 77, 139, 168\}_4$   
 $C_{44} = \{5, 31, 46, 64\}_4$   
 $C_{45} = \{15, 39, 106, 172\}_4$   
 $C_{46} = \{36, 37, 159, 166\}_4$   
 $C_{47} = \{0, 60, 114, 176\}_4$   
 $C_{48} = \{43, 164, 187, 193\}_4$   
 $C_{49} = \{35, 122, 156, 165\}_4$   
 $C_{50} = \{42, 65\}_2$   
 $C_{51} = \{82, 131\}_2$   
 $C_{52} = \{1, 4, 68, 121\}_4$   
 $C_{53} = \{14, 23, 27, 33\}_4$   
 $C_{54} = \{3, 10, 24, 29\}_4$   
 $C_{55} = \{9, 12, 27, 125\}_4$   
 $C_{56} = \{50, 84, 99, 152\}_4$   
 $C_{57} = \{8, 109, 117, 179\}_4$   
 $C_{58} = \{25, 116, 162, 170\}_4$   
 $C_{59} = \{90, 163, 180, 190\}_4$   
 $C_{60} = \{21, 146, 174, 175\}_4$   
 $C_{61} = \{54, 80, 120, 188\}_4$   
 $C_{62} = \{83, 157\}_2$

Column cell 1:

Column cell 2:

Column cell 10:

Column cell 11:

Column cell 12:

Column cell 13:

Column cell 14:

Column cell 15:

Column cell 16:

Column cell 17:

Column cell 18:

Column cell 19:

Column cell 20:

Column cell 21:

Column cell 22:

Column cell 23:

Column cell 24:

Column cell 25:

Column cell 26:

Column cell 27:

Column cell 28:

Column cell 29:

Column cell 30:

Column cell 31:

Column cell 32:

Column cell 33:

Column cell 34:

Column cell 35:

Column cell 36:

Column cell 37:

Column cell 38:  
 Column cell 39:  
 Column cell 40:  
 Column cell 41:  
 Column cell 42:  
 Column cell 43:  
 Column cell 44:  
 Column cell 45:  
 Column cell 46:  
 Column cell 47:  
 Column cell 48:  
 Column cell 49:  
 Column cell 50:  
 Column cell 51:  
 Column cell 52:  
 Column cell 55:  
 Column cell 56:  
 Column cell 57:  
 Column cell 58:  
 Column cell 59:  
 Column cell 60:  
 Column cell 61:  
 Column cell 62:

Order of the group that is induced on the object is 4

Number of ancestors on 5-sets is 125562.

Number of orbits on 5-sets is 125562.

With 10 orbits on the object

Orbit lengths: 2,  $4^9$

The points by ranks:

$i$	Rank	$i$	Rank	$i$	Rank	$i$	Rank
0	0	10	27018	20	35650	30	27514
1	1	11	17497	21	39427	31	28003
2	184	12	50059	22	36907	32	24596
3	185	13	14893	23	31731	33	41322
4	188	14	38973	24	44657	34	16159
5	7371	15	15118	25	38816	35	12866
6	32403	16	24505	26	11192	36	42488
7	21678	17	7356	27	6869	37	14245
8	11001	18	23594	28	42680		
9	37129	19	12873	29	12224		

The points:

$$\begin{aligned}
 P_0 &= (0, 1, 0, 0, 0) P_1 = (0, 0, 1, 0, 0) P_2 = (0, 1, 18, 36, 18) P_3 = (0, 1, 23, 18, 9) \\
 P_4 &= (0, 1, 17, 22, 11) P_5 = (1, 12, 17, 17, 1) P_6 = (1, 23, 36, 18, 30) P_7 = (1, 22, 25, 11, 34) \\
 P_8 &= (1, 11, 35, 10, 28) P_9 = (1, 23, 26, 10, 3) P_{10} = (1, 1, 5, 9, 24) P_{11} = (1, 14, 12, 33, 33) \\
 P_{12} &= (1, 18, 7, 32, 18) P_{13} = (1, 26, 32, 15, 16) P_{14} = (1, 26, 35, 31, 10) P_{15} = (1, 4, 6, 10, 16) \\
 P_{16} &= (1, 36, 32, 21, 5) P_{17} = (1, 23, 33, 17, 1) P_{18} = (1, 17, 27, 35, 8) P_{19} = (1, 21, 35, 20, 15) \\
 P_{20} &= (1, 23, 16, 23, 29) P_{21} = (1, 29, 28, 26, 10) P_{22} = (1, 29, 28, 24, 17) P_{23} = (1, 2, 34, 26, 13) \\
 P_{24} &= (1, 33, 8, 36, 6) P_{25} = (1, 16, 15, 24, 10) P_{26} = (1, 25, 23, 27, 28) P_{27} = (1, 19, 10, 31, 1) \\
 P_{28} &= (1, 7, 24, 20, 23) P_{29} = (1, 16, 24, 36, 15) P_{30} = (1, 22, 16, 30, 24) P_{31} = (1, 8, 4, 31, 24) \\
 P_{32} &= (1, 3, 15, 13, 5) P_{33} = (1, 15, 11, 14, 4) P_{34} = (1, 23, 4, 33, 14) P_{35} = (1, 19, 27, 20, 15) \\
 P_{36} &= (1, 1, 15, 17, 23) P_{37} = (1, 30, 32, 6, 31)
 \end{aligned}$$

Stabilizer of order 4 is generated by:

$$g_1 = \begin{bmatrix} 14 & 30 & 19 & 24 & 21 \\ 28 & 33 & 18 & 5 & 13 \\ 15 & 32 & 33 & 33 & 15 \\ 29 & 15 & 13 & 12 & 0 \\ 12 & 33 & 5 & 2 & 12 \end{bmatrix}$$

with 40 fixed points

$$g_2 = \begin{bmatrix} 3 & 25 & 10 & 6 & 5 \\ 28 & 15 & 9 & 23 & 26 \\ 31 & 16 & 35 & 8 & 18 \\ 26 & 4 & 4 & 3 & 16 \\ 12 & 5 & 26 & 22 & 1 \end{bmatrix}$$

with 2 fixed points

### 3.4 Isomorphism Type 3

Stabilizer has order 4

Plane intersection type is  $4^{210} 3^{7596}$

Plane invariant is too big (210 planes)

$\rightarrow$	$2_1$	$4_7$	$4_{11}$	$4_{10}$	$4_9$	$4_{12}$	$8_{15}$	$4_{14}$	$4_{16}$	$4_{46}$	$4_{13}$	$4_{18}$	$4_{17}$	$4_8$	$2_{20}$	$2_{21}$	$8_{47}$	$2_{22}$	$4_{19}$	$4_{25}$	$4_{49}$	$4_{26}$	$4_{24}$	$4_{48}$	$4_{29}$	
$2_0$	2	2	2	2	2	2	4	2	2	2	2	2	2	0	0	0	0	0	0	0	0	0	0	0	0	0
$4_3$	0	1	1	1	0	0	0	0	0	0	0	0	0	2	1	1	4	1	1	1	1	1	1	1	1	1
$4_2$	0	1	1	0	1	1	2	0	0	0	0	0	0	1	0	0	0	0	1	1	1	1	1	1	0	0
$4_{42}$	0	0	0	0	1	0	0	1	1	1	0	0	0	0	0	0	0	0	2	1	1	1	0	1	1	
$4_6$	0	1	0	0	0	1	2	0	0	0	1	1	0	0	1	0	0	0	0	0	0	0	1	1	1	
$4_5$	1	0	0	0	0	0	0	1	0	0	1	1	0	1	0	0	0	0	0	0	0	0	0	0	0	
$4_{43}$	0	0	1	0	0	0	0	0	1	0	1	0	0	0	0	1	0	0	0	1	0	0	0	0	0	
$4_{44}$	0	0	0	1	1	0	0	1	0	0	0	0	0	0	0	0	4	0	0	0	1	0	1	0	0	
$4_{45}$	0	0	0	0	0	1	0	0	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	1	0	
$4_4$	0	0	0	1	0	0	2	0	1	1	0	1	2	0	0	0	0	1	0	0	0	1	0	0	1	

$$C_0 = \{26, 28\}_2$$

$$C_1 = \{175, 176\}_2$$

$$C_2 = \{18, 27, 35, 36\}_4$$

$$C_3 = \{2, 3, 14, 21\}_4$$

$$C_4 = \{12, 16, 19, 31\}_4$$

$$C_5 = \{8, 20, 32, 33\}_4$$

$$C_6 = \{6, 23, 24, 29\}_4$$

$$C_7 = \{72, 82, 127, 200\}_4$$

$$C_8 = \{13, 38, 114, 131\}_4$$

$$C_9 = \{40, 88, 141, 148\}_4$$

$$C_{10} = \{41, 90, 157, 159\}_4$$

$$C_{11} = \{3, 129, 142, 162\}_4$$

$$C_{12} = \{26, 49, 140, 194\}_4$$

$$C_{13} = \{47, 73, 83, 182\}_4$$

$$C_{14} = \{21, 70, 138, 202\}_4$$

$$C_{15} = \{28, 46, 55, 59, 76, 85, 119, 150\}_8$$

$$C_{16} = \{1, 25, 125, 144\}_4$$

$$C_{17} = \{57, 68, 174, 199\}_4$$

$$C_{18} = \{63, 69, 137, 204\}_4$$

$$C_{19} = \{0, 11, 35, 52\}_4$$

$$C_{20} = \{100, 153\}_2$$

$$C_{21} = \{45, 192\}_2$$

$$C_{22} = \{91, 209\}_2$$

$$C_{23} = \{130, 203\}_2$$

$$C_{24} = \{14, 99, 111, 113\}_4$$

- $C_{25} = \{135, 169, 190, 197\}_4$   
 $C_{26} = \{9, 58, 109, 172\}_4$   
 $C_{27} = \{79, 122, 152, 180\}_4$   
 $C_{28} = \{31, 117, 118, 166\}_4$   
 $C_{29} = \{16, 29, 126, 158\}_4$   
 $C_{30} = \{15, 34, 106, 160\}_4$   
 $C_{31} = \{5, 8, 97, 112\}_4$   
 $C_{32} = \{75, 136, 161, 181\}_4$   
 $C_{33} = \{19, 65, 93, 167\}_4$   
 $C_{34} = \{39, 92, 110, 154\}_4$   
 $C_{35} = \{42, 89, 147, 189\}_4$   
 $C_{36} = \{7, 128\}_2$   
 $C_{37} = \{98, 121, 165, 206\}_4$   
 $C_{38} = \{33, 53, 78, 96, 168, 191, 196, 205\}_8$   
 $C_{39} = \{56, 86, 95, 195\}_4$   
 $C_{40} = \{124, 134\}_2$   
 $C_{41} = \{37, 71, 81, 123\}_4$   
 $C_{42} = \{4, 13, 25, 37\}_4$   
 $C_{43} = \{7, 11, 15, 34\}_4$   
 $C_{44} = \{0, 1, 9, 22\}_4$   
 $C_{45} = \{5, 10, 17, 30\}_4$   
 $C_{46} = \{48, 60, 133, 198\}_4$   
 $C_{47} = \{12, 30, 61, 107, 116, 164, 185, 193\}_8$   
 $C_{48} = \{6, 101, 104, 143\}_4$   
 $C_{49} = \{4, 10, 36, 171\}_4$   
 $C_{50} = \{20, 108, 179, 188\}_4$   
 $C_{51} = \{22, 54, 87, 207\}_4$   
 $C_{52} = \{50, 66, 184, 187\}_4$   
 $C_{53} = \{62, 80, 84, 145\}_4$   
 $C_{54} = \{24, 32, 103, 132\}_4$   
 $C_{55} = \{94, 105, 149, 177\}_4$   
 $C_{56} = \{2, 139, 163, 201\}_4$   
 $C_{57} = \{44, 170\}_2$   
 $C_{58} = \{43, 64\}_2$   
 $C_{59} = \{23, 115, 146, 186\}_4$   
 $C_{60} = \{51, 77, 151, 183\}_4$   
 $C_{61} = \{18, 74, 155, 178\}_4$   
 $C_{62} = \{102, 173\}_2$   
 $C_{63} = \{17, 208\}_2$   
 $C_{64} = \{67, 156\}_2$   
 $C_{65} = \{27, 120\}_2$

$\rightarrow$	$2_1$	$4_7$	$4_{11}$	$4_{10}$	$4_9$	$4_{12}$	$8_{15}$	$4_{14}$	$4_{16}$	$4_{46}$	$4_{13}$	$4_{18}$	$4_{17}$	$4_8$	$2_{20}$	$2_{21}$	$8_{47}$	$2_{22}$	$4_{19}$	$4_{25}$	$4_{49}$	$4_{26}$	$4_{24}$	$4_{48}$	$4_{29}$	
$2_0$	2	2	2	2	2	2	4	2	2	2	2	2	2	0	0	0	0	0	0	0	0	0	0	0	0	0
$4_3$	0	1	1	1	0	0	0	0	0	0	0	0	0	2	1	1	4	1	1	1	1	1	1	1	1	1
$4_2$	0	1	1	0	1	1	2	0	0	0	0	0	0	1	0	0	0	0	0	1	1	1	1	0	0	0
$4_{42}$	0	0	0	0	1	0	0	1	1	1	0	0	0	0	0	0	0	0	2	1	1	1	0	1	1	1
$4_6$	0	1	0	0	0	1	2	0	0	0	1	1	0	0	1	0	0	0	0	0	0	0	1	1	1	1
$4_5$	1	0	0	0	0	0	0	1	0	0	1	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0
$4_{43}$	0	0	1	0	0	0	0	0	1	0	1	0	0	0	0	1	0	0	0	1	0	0	0	0	0	0
$4_{44}$	0	0	0	1	1	0	0	1	0	0	0	0	0	0	0	0	4	0	0	0	1	0	1	0	0	0
$4_{45}$	0	0	0	0	0	1	0	0	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	1	0
$4_4$	0	0	0	1	0	0	2	0	1	1	0	1	2	0	0	0	0	1	0	0	0	1	0	0	0	1



$\downarrow$	$2_1$	$4_7$	$4_{11}$	$4_{10}$	$4_9$	$4_{12}$	$8_{15}$	$4_{14}$	$4_{16}$	$4_{46}$	$4_{13}$	$4_{18}$	$4_{17}$	$4_8$	$2_{20}$	$2_{21}$	$8_{47}$	$2_{22}$	$4_{19}$	$4_{25}$	$4_{49}$	$4_{26}$	$4_{24}$	$4_{48}$	$4_{29}$	
$2_0$	2	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0
$4_3$	0	1	1	1	0	0	0	0	0	0	0	0	0	2	2	2	2	2	1	1	1	1	1	1	1	1
$4_2$	0	1	1	0	1	1	1	0	0	0	0	0	0	1	0	0	0	0	1	1	1	1	1	1	0	0
$4_{42}$	0	0	0	0	1	0	0	1	1	1	0	0	0	0	0	0	0	0	2	1	1	1	0	1	1	1
$4_6$	0	1	0	0	0	1	1	0	0	0	1	1	0	0	2	0	0	0	0	0	0	0	1	1	1	1
$4_5$	2	0	0	0	0	0	0	1	0	0	1	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0
$4_{43}$	0	0	1	0	0	0	0	0	1	0	1	0	0	0	0	2	0	0	0	1	0	0	0	0	0	0
$4_{44}$	0	0	0	1	1	0	0	1	0	0	0	0	0	0	0	0	2	0	0	0	1	0	1	0	0	0
$4_{45}$	0	0	0	0	0	1	0	0	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	1	0
$4_4$	0	0	0	1	0	0	1	0	1	1	0	1	2	0	0	0	0	2	0	0	0	1	0	0	0	1

$$C_0 = \{26, 28\}_2$$

$$C_1 = \{132, 133\}_2$$

$$C_2 = \{18, 27, 35, 36\}_4$$

$$C_3 = \{2, 3, 14, 21\}_4$$

$$C_4 = \{12, 16, 19, 31\}_4$$

$$C_5 = \{8, 20, 32, 33\}_4$$

$$C_6 = \{6, 23, 24, 29\}_4$$

$$C_7 = \{19, 97, 156, 178\}_4$$

$$C_8 = \{35, 86, 154, 207\}_4$$

$$C_9 = \{77, 93, 107, 148\}_4$$

$$C_{10} = \{92, 141, 142, 192\}_4$$

$$C_{11} = \{49, 74, 114, 155\}_4$$

$$C_{12} = \{13, 104, 149, 199\}_4$$

$$C_{13} = \{51, 53, 105, 127\}_4$$

$$C_{14} = \{31, 66, 151, 202\}_4$$

$$C_{15} = \{110, 145, 160, 177, 180, 184, 186, 189\}_8$$

$$C_{16} = \{27, 79, 116, 200\}_4$$

$$C_{17} = \{5, 41, 181, 185\}_4$$

$$C_{18} = \{98, 121, 152, 182\}_4$$

$$C_{19} = \{103, 112, 117, 196\}_4$$

$$C_{20} = \{144, 170\}_2$$

$$C_{21} = \{42, 190\}_2$$

$$C_{22} = \{2, 63\}_2$$

$$C_{23} = \{65, 82\}_2$$

$$C_{24} = \{60, 90, 162, 164\}_4$$

$$C_{25} = \{68, 124, 135, 153\}_4$$

$$C_{26} = \{22, 101, 113, 165\}_4$$

$$C_{27} = \{47, 94, 129, 159\}_4$$

$$C_{28} = \{84, 85, 109, 137\}_4$$

$$C_{29} = \{1, 75, 198, 205\}_4$$

$$C_{30} = \{10, 140, 167, 206\}_4$$

$$C_{31} = \{38, 62, 163, 172\}_4$$

$$C_{32} = \{9, 80, 128, 139\}_4$$

$$C_{33} = \{8, 99, 136, 204\}_4$$

$$C_{34} = \{87, 91, 143, 193\}_4$$

$$C_{35} = \{20, 146, 175, 191\}_4$$

$$C_{36} = \{26, 61\}_2$$

$$C_{37} = \{7, 24, 119, 171\}_4$$

$$C_{38} = \{6, 34, 69, 95, 108, 120, 123, 173\}_8$$

$$C_{39} = \{33, 70, 174, 176\}_4$$

$$C_{40} = \{0, 157\}_2$$

$$C_{41} = \{52, 54, 158, 194\}_4$$

$$C_{42} = \{4, 13, 25, 37\}_4$$

$$C_{43} = \{7, 11, 15, 34\}_4$$

$$C_{44} = \{0, 1, 9, 22\}_4$$

$$C_{45} = \{5, 10, 17, 30\}_4$$

$$C_{46} = \{12, 15, 56, 57\}_4$$

$$C_{47} = \{28, 36, 43, 100, 122, 138, 166, 208\}_8$$

$$C_{48} = \{39, 147, 168, 169\}_4$$

$$C_{49} = \{23, 40, 195, 209\}_4$$

$$C_{50} = \{29, 44, 71, 203\}_4$$

$$C_{51} = \{3, 64, 102, 111\}_4$$

$$C_{52} = \{21, 32, 125, 188\}_4$$

$$C_{53} = \{17, 25, 179, 183\}_4$$

$$C_{54} = \{16, 81, 197, 201\}_4$$

$$C_{55} = \{48, 50, 88, 131\}_4$$

$$C_{56} = \{67, 73, 115, 150\}_4$$

$$C_{57} = \{106, 134\}_2$$

$$C_{58} = \{55, 58\}_2$$

$$C_{59} = \{11, 78, 126, 161\}_4$$

$$C_{60} = \{14, 72, 96, 187\}_4$$

$$C_{61} = \{4, 30, 46, 130\}_4$$

$$C_{62} = \{45, 89\}_2$$

$$C_{63} = \{37, 118\}_2$$

$$C_{64} = \{18, 76\}_2$$

$$C_{65} = \{59, 83\}_2$$

Column cell 1:

Column cell 7:

Column cell 8:

Column cell 9:

Column cell 10:

Column cell 11:

Column cell 12:

Column cell 13:

Column cell 14:

Column cell 15:

Column cell 16:

Column cell 17:

Column cell 18:

Column cell 19:

Column cell 20:

Column cell 21:

Column cell 22:

Column cell 23:

Column cell 24:

Column cell 25:

Column cell 26:

Column cell 27:

Column cell 28:

Column cell 29:

Column cell 30:

Column cell 31:

Column cell 32:

Column cell 33:

Column cell 34:

Column cell 35:

Column cell 36:

Column cell 37:

Column cell 38:

Column cell 39:

Column cell 40:

Column cell 41:

Column cell 46:

Column cell 47:

Column cell 48:

Column cell 49:

Column cell 50:

Column cell 51:  
 Column cell 52:  
 Column cell 53:  
 Column cell 54:  
 Column cell 55:  
 Column cell 56:  
 Column cell 57:  
 Column cell 58:  
 Column cell 59:  
 Column cell 60:  
 Column cell 61:  
 Column cell 62:  
 Column cell 63:  
 Column cell 64:  
 Column cell 65:

Order of the group that is induced on the object is 4

Number of ancestors on 5-sets is 125562.

Number of orbits on 5-sets is 125562.

With 10 orbits on the object

Orbit lengths: 2,  $4^9$

The points by ranks:

$i$	Rank	$i$	Rank	$i$	Rank	$i$	Rank
0	0	10	50998	20	48933	30	32677
1	1	11	17296	21	43061	31	12761
2	184	12	44268	22	27664	32	50344
3	185	13	49507	23	46255	33	47806
4	295	14	43060	24	39343	34	12866
5	6849	15	12883	25	40225	35	39747
6	26689	16	30901	26	47523	36	917
7	18223	17	13652	27	7501	37	28764
8	30408	18	46338	28	30079		
9	19166	19	27449	29	18617		

The points:

$$\begin{aligned}
 P_0 &= (0, 1, 0, 0, 0) P_1 = (0, 0, 1, 0, 0) P_2 = (0, 1, 18, 36, 18) P_3 = (0, 1, 23, 18, 9) \\
 P_4 &= (0, 1, 6, 9, 24) P_5 = (1, 30, 31, 31, 1) P_6 = (1, 14, 26, 6, 7) P_7 = (1, 24, 28, 4, 26) \\
 P_8 &= (1, 17, 30, 22, 2) P_9 = (1, 19, 27, 3, 26) P_{10} = (1, 3, 2, 7, 36) P_{11} = (1, 10, 20, 4, 33) \\
 P_{12} &= (1, 17, 30, 25, 21) P_{13} = (1, 29, 28, 34, 12) P_{14} = (1, 31, 1, 34, 23) P_{15} = (1, 8, 4, 20, 15) \\
 P_{16} &= (1, 6, 26, 5, 13) P_{17} = (1, 21, 15, 28, 31) P_{18} = (1, 14, 25, 16, 22) P_{19} = (1, 16, 8, 27, 24) \\
 P_{20} &= (1, 3, 31, 23, 12) P_{21} = (1, 25, 19, 34, 23) P_{22} = (1, 3, 20, 36, 24) P_{23} = (1, 22, 4, 1, 22) \\
 P_{24} &= (1, 8, 4, 30, 10) P_{25} = (1, 35, 26, 8, 11) P_{26} = (1, 23, 36, 23, 9) P_{27} = (1, 8, 26, 13, 1) \\
 P_{28} &= (1, 24, 7, 8, 2) P_{29} = (1, 34, 19, 5, 26) P_{30} = (1, 3, 32, 35, 30) P_{31} = (1, 36, 8, 35, 15) \\
 P_{32} &= (1, 3, 20, 11, 18) P_{33} = (1, 16, 6, 18, 9) P_{34} = (1, 19, 27, 20, 15) P_{35} = (1, 29, 36, 16, 11) \\
 P_{36} &= (0, 1, 24, 29, 3) P_{37} = (1, 2, 9, 28, 35)
 \end{aligned}$$

Stabilizer of order 4 is generated by:

$$g_1 = \begin{bmatrix} 22 & 0 & 0 & 17 & 34 \\ 0 & 0 & 31 & 0 & 0 \\ 0 & 8 & 0 & 0 & 0 \\ 17 & 0 & 0 & 21 & 25 \\ 27 & 0 & 0 & 34 & 21 \end{bmatrix}$$

with 38 fixed points

$$g_2 = \begin{bmatrix} 31 & 18 & 17 & 31 & 33 \\ 27 & 32 & 26 & 7 & 36 \\ 9 & 27 & 32 & 28 & 31 \\ 35 & 31 & 36 & 2 & 32 \\ 34 & 28 & 7 & 27 & 2 \end{bmatrix}$$

with 38 fixed points

### 3.5 Isomorphism Type 4

Stabilizer has order 4

Plane intersection type is  $4^{230} 3^{7516}$

Plane invariant is too big (230 planes)

$\rightarrow$	$2_1$	$4_{12}$	$2_{11}$	$2_{70}$	$4_{14}$	$2_{15}$	$4_{16}$	$2_{17}$	$4_{18}$	$2_{19}$	$2_{20}$	$2_{21}$	$2_{22}$	$4_{13}$	$4_{23}$	$4_{10}$	$2_{25}$	$6_{71}$	$4_{26}$	$4_{27}$	$4_{24}$	$4_{30}$	$4_{29}$	$4_{72}$	$4_{33}$	
$1_0$	2	4	2	2	4	2	4	2	4	2	2	2	2	4	4	0	0	0	0	0	0	0	0	0	0	0
$1_3$	2	0	2	2	0	2	0	2	0	2	2	2	2	0	0	0	0	0	4	4	0	0	0	0	0	0
$4_{69}$	1	2	0	0	1	0	1	0	1	0	0	0	0	0	0	3	1	3	1	1	1	1	1	1	1	1
$4_2$	0	0	1	0	1	0	0	0	0	0	0	0	0	0	1	0	1	0	0	0	2	0	1	0	1	
$4_{68}$	0	0	0	1	0	0	0	0	0	0	0	0	0	1	0	0	0	3	0	0	0	2	0	1	0	
$4_5$	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	1	1	1	
$4_4$	0	0	0	0	1	0	0	1	1	0	0	0	0	0	0	0	0	0	1	0	1	0	1	1	0	
$4_8$	0	0	0	0	0	0	1	0	1	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	
$4_7$	0	0	0	0	0	0	0	0	0	0	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	
$4_9$	0	1	0	0	0	0	0	0	0	0	0	1	0	0	0	1	0	0	0	2	0	1	0	0	0	
$4_6$	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	0	0	0	0	0	0	0	0	0	0	

$$C_0 = \{35\}_1$$

$$C_1 = \{98, 111\}_2$$

$$C_2 = \{9, 25, 33, 36\}_4$$

$$C_3 = \{30\}_1$$

$$C_4 = \{7, 21, 24, 29\}_4$$

$$C_5 = \{0, 17, 22, 31\}_4$$

$$C_6 = \{19, 20, 23, 34\}_4$$

$$C_7 = \{5, 13, 16, 32\}_4$$

$$C_8 = \{11, 26, 27, 37\}_4$$

$$C_9 = \{2, 3, 6, 28\}_4$$

$$C_{10} = \{72, 154, 170, 218\}_4$$

$$C_{11} = \{138, 147\}_2$$

$$C_{12} = \{29, 50, 136, 146\}_4$$

$$C_{13} = \{173, 195, 212, 217\}_4$$

$$C_{14} = \{46, 153, 155, 185\}_4$$

$$C_{15} = \{8, 156\}_2$$

$$C_{16} = \{45, 51, 189, 193\}_4$$

$$C_{17} = \{55, 175\}_2$$

$$C_{18} = \{19, 141, 167, 215\}_4$$

$$C_{19} = \{83, 229\}_2$$

$$C_{20} = \{127, 182\}_2$$

$$C_{21} = \{5, 84\}_2$$

$$C_{22} = \{30, 161\}_2$$

$$C_{23} = \{21, 22, 38, 149\}_4$$

$$C_{24} = \{71, 92, 106, 165\}_4$$

$$C_{25} = \{12, 32\}_2$$

$$C_{26} = \{37, 52, 122, 210\}_4$$

$$C_{27} = \{42, 100, 117, 171\}_4$$

$$C_{28} = \{77, 160\}_2$$

$$C_{29} = \{0, 24, 137, 190\}_4$$

$$C_{30} = \{56, 60, 67, 96\}_4$$



$\downarrow$	2 <sub>1</sub>	4 <sub>12</sub>	2 <sub>11</sub>	2 <sub>70</sub>	4 <sub>14</sub>	2 <sub>15</sub>	4 <sub>16</sub>	2 <sub>17</sub>	4 <sub>18</sub>	2 <sub>19</sub>	2 <sub>20</sub>	2 <sub>21</sub>	2 <sub>22</sub>	4 <sub>13</sub>	4 <sub>23</sub>	4 <sub>10</sub>	2 <sub>25</sub>	6 <sub>71</sub>	4 <sub>26</sub>	4 <sub>27</sub>	4 <sub>24</sub>	4 <sub>30</sub>	4 <sub>29</sub>	4 <sub>72</sub>	4 <sub>33</sub>	
1 <sub>0</sub>	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0
1 <sub>3</sub>	1	0	1	1	0	1	0	1	0	1	1	1	1	0	0	0	0	0	1	1	0	0	0	0	0	0
4 <sub>69</sub>	2	2	0	0	1	0	1	0	1	0	0	0	0	0	0	3	2	2	1	1	1	1	1	1	1	1
4 <sub>2</sub>	0	0	2	0	1	0	0	0	0	0	0	0	0	0	1	0	2	0	0	0	2	0	1	0	1	1
4 <sub>68</sub>	0	0	0	2	0	0	0	0	0	0	0	0	0	1	0	0	0	2	0	0	0	2	0	1	0	0
4 <sub>5</sub>	0	0	0	0	0	2	1	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	1	1	1	1
4 <sub>4</sub>	0	0	0	0	1	0	0	2	1	0	0	0	0	0	0	0	0	0	1	0	1	0	1	1	1	0
4 <sub>8</sub>	0	0	0	0	0	0	1	0	1	2	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0
4 <sub>7</sub>	0	0	0	0	0	0	0	0	0	0	2	0	0	0	1	0	0	0	0	0	0	0	0	0	0	1
4 <sub>9</sub>	0	1	0	0	0	0	0	0	0	0	0	2	0	0	0	1	0	0	0	2	0	1	0	0	0	0
4 <sub>6</sub>	0	0	0	0	0	0	0	0	0	0	0	0	2	1	1	0	0	0	0	0	0	0	0	0	0	0

- $C_0 = \{35\}_1$
- $C_1 = \{44, 90\}_2$
- $C_2 = \{9, 25, 33, 36\}_4$
- $C_3 = \{30\}_1$
- $C_4 = \{7, 21, 24, 29\}_4$
- $C_5 = \{0, 17, 22, 31\}_4$
- $C_6 = \{19, 20, 23, 34\}_4$
- $C_7 = \{5, 13, 16, 32\}_4$
- $C_8 = \{11, 26, 27, 37\}_4$
- $C_9 = \{2, 3, 6, 28\}_4$
- $C_{10} = \{70, 117, 152, 191\}_4$
- $C_{11} = \{76, 80\}_2$
- $C_{12} = \{1, 158, 202, 214\}_4$
- $C_{13} = \{8, 16, 36, 69\}_4$
- $C_{14} = \{9, 27, 74, 133\}_4$
- $C_{15} = \{151, 226\}_2$
- $C_{16} = \{17, 101, 131, 204\}_4$
- $C_{17} = \{4, 51\}_2$
- $C_{18} = \{41, 71, 119, 218\}_4$
- $C_{19} = \{12, 114\}_2$
- $C_{20} = \{136, 165\}_2$
- $C_{21} = \{24, 228\}_2$
- $C_{22} = \{148, 213\}_2$
- $C_{23} = \{30, 31, 75, 104\}_4$
- $C_{24} = \{145, 176, 184, 192\}_4$
- $C_{25} = \{106, 223\}_2$
- $C_{26} = \{62, 83, 100, 210\}_4$
- $C_{27} = \{142, 170, 181, 207\}_4$
- $C_{28} = \{149, 190\}_2$
- $C_{29} = \{55, 66, 157, 216\}_4$
- $C_{30} = \{91, 98, 195, 199\}_4$
- $C_{31} = \{78, 96, 123, 140\}_4$
- $C_{32} = \{53, 84, 150, 159\}_4$
- $C_{33} = \{50, 81, 88, 121\}_4$
- $C_{34} = \{42, 87, 124, 203\}_4$
- $C_{35} = \{73, 118, 196, 222\}_4$
- $C_{36} = \{37, 77, 89, 162\}_4$
- $C_{37} = \{102, 125, 130, 198\}_4$
- $C_{38} = \{2, 72, 208, 220\}_4$
- $C_{39} = \{43, 110, 129, 146\}_4$
- $C_{40} = \{23, 137, 171, 186\}_4$
- $C_{41} = \{13, 20, 112, 153\}_4$
- $C_{42} = \{68, 161, 172, 201\}_4$
- $C_{43} = \{58, 139, 156, 217\}_4$
- $C_{44} = \{48, 97, 111, 219\}_4$
- $C_{45} = \{26, 82, 115, 205\}_4$
- $C_{46} = \{21, 99, 187, 221\}_4$

$$\begin{aligned}
C_{47} &= \{0, 7, 15, 116\}_4 \\
C_{48} &= \{34, 126, 189, 224\}_4 \\
C_{49} &= \{52, 120, 122, 197\}_4 \\
C_{50} &= \{29, 67, 135, 200\}_4 \\
C_{51} &= \{33, 38, 86, 108\}_4 \\
C_{52} &= \{5, 6, 18, 46\}_4 \\
C_{53} &= \{95, 138, 173, 180\}_4 \\
C_{54} &= \{28, 93, 132, 166\}_4 \\
C_{55} &= \{19, 79, 85, 154\}_4 \\
C_{56} &= \{3, 25, 61, 177\}_4 \\
C_{57} &= \{147, 182, 185, 188\}_4 \\
C_{58} &= \{54, 107, 225, 229\}_4 \\
C_{59} &= \{10, 11, 60, 179\}_4 \\
C_{60} &= \{35, 127, 134, 141\}_4 \\
C_{61} &= \{39, 92, 175, 194\}_4 \\
C_{62} &= \{32, 49, 57, 59, 105, 167, 169, 209\}_8 \\
C_{63} &= \{64, 128, 155, 178\}_4 \\
C_{64} &= \{63, 65, 103, 168\}_4 \\
C_{65} &= \{14, 160, 174, 193\}_4 \\
C_{66} &= \{22, 45\}_2 \\
C_{67} &= \{47, 94, 109, 163\}_4 \\
C_{68} &= \{1, 4, 12, 14\}_4 \\
C_{69} &= \{8, 10, 15, 18\}_4 \\
C_{70} &= \{206, 227\}_2 \\
C_{71} &= \{40, 56, 144, 164, 183, 212\}_6 \\
C_{72} &= \{113, 143, 211, 215\}_4
\end{aligned}$$

Column cell 1:

Column cell 10:

Column cell 11:

Column cell 12:

Column cell 13:

Column cell 14:

Column cell 15:

Column cell 16:

Column cell 17:

Column cell 18:

Column cell 19:

Column cell 20:

Column cell 21:

Column cell 22:

Column cell 23:

Column cell 24:

Column cell 25:

Column cell 26:

Column cell 27:

Column cell 28:

Column cell 29:

Column cell 30:

Column cell 31:

Column cell 32:

Column cell 33:

Column cell 34:

Column cell 35:

Column cell 36:

Column cell 37:

Column cell 38:

Column cell 39:

Column cell 40:

Column cell 41:

Column cell 42:  
 Column cell 43:  
 Column cell 44:  
 Column cell 45:  
 Column cell 46:  
 Column cell 47:  
 Column cell 48:  
 Column cell 49:  
 Column cell 50:  
 Column cell 51:  
 Column cell 52:  
 Column cell 53:  
 Column cell 54:  
 Column cell 55:  
 Column cell 56:  
 Column cell 57:  
 Column cell 58:  
 Column cell 59:  
 Column cell 60:  
 Column cell 61:  
 Column cell 62:  
 Column cell 63:  
 Column cell 64:  
 Column cell 65:  
 Column cell 66:  
 Column cell 67:  
 Column cell 70:  
 Column cell 71:  
 Column cell 72:

Order of the group that is induced on the object is 4

Number of ancestors on 5-sets is 125571.

Number of orbits on 5-sets is 125571.

With 11 orbits on the object

Orbit lengths:  $1^2, 4^9$

The points by ranks:

$i$	Rank	$i$	Rank	$i$	Rank	$i$	Rank
0	0	10	13166	20	10756	30	620
1	1	11	10736	21	46356	31	42023
2	184	12	33349	22	9803	32	10315
3	185	13	20539	23	50784	33	30498
4	295	14	36183	24	51894	34	41968
5	13258	15	9065	25	6756	35	931
6	14908	16	30901	26	16186	36	20556
7	48939	17	1298	27	34872	37	38023
8	14406	18	39058	28	24531		
9	37446	19	35827	29	28160		

The points:

$$\begin{aligned}
 P_0 &= (0, 1, 0, 0, 0) P_1 = (0, 0, 1, 0, 0) P_2 = (0, 1, 18, 36, 18) P_3 = (0, 1, 23, 18, 9) \\
 P_4 &= (0, 1, 6, 9, 24) P_5 = (1, 19, 16, 20, 31) P_6 = (1, 19, 1, 8, 16) P_7 = (1, 6, 34, 23, 12) \\
 P_8 &= (1, 15, 25, 32, 16) P_9 = (1, 8, 25, 7, 3) P_{10} = (1, 4, 29, 1, 31) P_{11} = (1, 3, 15, 1, 28) \\
 P_{12} &= (1, 23, 26, 31, 32) P_{13} = (1, 5, 7, 11, 27) P_{14} = (1, 23, 36, 10, 17) P_{15} = (1, 29, 10, 10, 19) \\
 P_{16} &= (1, 6, 26, 5, 13) P_{17} = (0, 1, 13, 19, 11) P_{18} = (1, 4, 6, 16, 10) P_{19} = (1, 20, 28, 4, 17) \\
 P_{20} &= (1, 15, 3, 1, 28) P_{21} = (1, 24, 30, 16, 22) P_{22} = (1, 25, 14, 20, 25) P_{23} = (1, 32, 30, 35, 18)
 \end{aligned}$$



$$\begin{aligned}
P_{24} &= (1, 21, 5, 32, 36) P_{25} = (1, 5, 30, 34, 1) P_{26} = (1, 28, 2, 25, 14) P_{27} = (1, 14, 30, 11, 29) \\
P_{28} &= (1, 35, 34, 6, 5) P_{29} = (1, 10, 15, 20, 35) P_{30} = (0, 1, 13, 22, 28) P_{31} = (1, 16, 14, 24, 23) \\
P_{32} &= (1, 15, 7, 15, 25) P_{33} = (1, 22, 25, 2, 2) P_{34} = (1, 24, 3, 28, 4) P_{35} = (0, 1, 6, 33, 20) \\
P_{36} &= (1, 8, 9, 11, 27) P_{37} = (1, 13, 28, 14, 3)
\end{aligned}$$

Stabilizer of order 4 is generated by:

$$g_1 = \begin{bmatrix} 26 & 0 & 0 & 0 & 0 \\ 0 & 3 & 2 & 20 & 33 \\ 0 & 19 & 3 & 23 & 12 \\ 0 & 12 & 33 & 34 & 21 \\ 0 & 23 & 20 & 30 & 34 \end{bmatrix}$$

with 40 fixed points

$$g_2 = \begin{bmatrix} 2 & 15 & 29 & 12 & 25 \\ 33 & 11 & 18 & 31 & 11 \\ 26 & 6 & 10 & 29 & 18 \\ 31 & 35 & 19 & 28 & 8 \\ 6 & 1 & 15 & 34 & 17 \end{bmatrix}$$

with 2 fixed points

### 3.6 Isomorphism Type 5

Stabilizer has order 72

Plane intersection type is  $4^{216} 3^{7572}$

Plane invariant is too big (216 planes)

$$\begin{array}{c|cc} \rightarrow & 198_1 & 18_3 \\ \hline 36_0 & 22 & 1 \\ 2_2 & 0 & 18 \end{array} \quad \begin{array}{c|cc} \downarrow & 198_1 & 18_3 \\ \hline 36_0 & 4 & 2 \\ 2_2 & 0 & 2 \end{array}$$

$$C_0 = \{0, 2, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37\}_{36}$$

$$C_1 = \{0, 1, 3, 4, 5, 6, 7, 8, 9, 10, 12, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49\}_{36}$$

$$C_2 = \{1, 3\}_2$$

$$C_3 = \{2, 11, 13, 28, 55, 64, 70, 85, 89, 92, 94, 106, 113, 138, 146, 171, 205, 206\}_{18}$$

$$\begin{array}{c|cc} \rightarrow & 198_1 & 18_3 \\ \hline 36_0 & 22 & 1 \\ 2_2 & 0 & 18 \end{array} \quad \begin{array}{c|cc} \downarrow & 198_1 & 18_3 \\ \hline 36_0 & 4 & 2 \\ 2_2 & 0 & 2 \end{array}$$

$$C_0 = \{0, 2, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37\}_{36}$$

$$C_1 = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 13, 14, 15, 16, 17, 18, 19, 20, 22, 23, 24, 25, 26, 27, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 43, 44, 47, 48, 49\}_{36}$$

$$C_2 = \{1, 3\}_2$$

$$C_3 = \{12, 21, 28, 42, 45, 46, 52, 68, 75, 86, 91, 96, 113, 149, 170, 185, 213, 215\}_{18}$$

Column cell 1:

Column cell 3:

Order of the group that is induced on the object is 72

Number of ancestors on 5-sets is 7053.

Number of orbits on 5-sets is 7053.

With 2 orbits on the object

Orbit lengths: 2, 36

The points by ranks:

$i$	Rank	$i$	Rank	$i$	Rank	$i$	Rank
0	0	10	32607	20	11297	30	46849
1	1	11	10956	21	21337	31	28003
2	184	12	36511	22	35208	32	24329
3	185	13	42676	23	13493	33	8578
4	318	14	1274	24	13633	34	16117
5	12008	15	49823	25	39935	35	18852
6	47213	16	11085	26	42153	36	18323
7	20130	17	24505	27	48134	37	29159
8	14936	18	36205	28	26414		
9	27554	19	44555	29	16288		

The points:

$$\begin{aligned}
P_0 &= (0, 1, 0, 0, 0) P_1 = (0, 0, 1, 0, 0) P_2 = (0, 1, 18, 36, 18) P_3 = (0, 1, 23, 18, 9) \\
P_4 &= (0, 1, 35, 26, 20) P_5 = (1, 25, 24, 29, 15) P_6 = (1, 10, 8, 28, 9) P_7 = (1, 35, 25, 21, 27) \\
P_8 &= (1, 33, 23, 8, 16) P_9 = (1, 35, 27, 13, 24) P_{10} = (1, 36, 17, 3, 30) P_{11} = (1, 15, 33, 14, 28) \\
P_{12} &= (1, 22, 28, 29, 17) P_{13} = (1, 1, 20, 20, 23) P_{14} = (0, 1, 20, 10, 35) P_{15} = (1, 34, 22, 18, 18) \\
P_{16} &= (1, 29, 21, 2, 28) P_{17} = (1, 36, 32, 21, 5) P_{18} = (1, 34, 32, 23, 17) P_{19} = (1, 3, 13, 18, 6) \\
P_{20} &= (1, 6, 10, 15, 28) P_{21} = (1, 3, 32, 20, 34) P_{22} = (1, 23, 9, 26, 29) P_{23} = (1, 31, 10, 21, 31) \\
P_{24} &= (1, 26, 32, 34, 31) P_{25} = (1, 1, 14, 2, 11) P_{26} = (1, 2, 21, 11, 23) P_{27} = (1, 12, 18, 17, 9) \\
P_{28} &= (1, 11, 29, 23, 7) P_{29} = (1, 27, 20, 1, 14) P_{30} = (1, 14, 26, 12, 22) P_{31} = (1, 8, 4, 31, 24) \\
P_{32} &= (1, 22, 10, 14, 8) P_{33} = (1, 15, 16, 36, 19) P_{34} = (1, 4, 32, 4, 14) P_{35} = (1, 2, 30, 19, 26) \\
P_{36} &= (1, 34, 22, 21, 26) P_{37} = (1, 3, 22, 15, 35)
\end{aligned}$$

Stabilizer of order 72 is generated by:

$$g_1 = \begin{bmatrix} 11 & 0 & 0 & 30 & 22 \\ 0 & 35 & 0 & 0 & 0 \\ 0 & 16 & 35 & 29 & 33 \\ 11 & 33 & 0 & 14 & 31 \\ 15 & 29 & 0 & 13 & 14 \end{bmatrix}$$

with 40 fixed points

$$g_2 = \begin{bmatrix} 25 & 0 & 0 & 11 & 13 \\ 0 & 18 & 28 & 19 & 28 \\ 0 & 4 & 18 & 35 & 36 \\ 25 & 36 & 28 & 16 & 2 \\ 24 & 35 & 19 & 8 & 16 \end{bmatrix}$$

with 40 fixed points

$$g_3 = \begin{bmatrix} 33 & 0 & 36 & 34 & 18 \\ 0 & 31 & 28 & 14 & 12 \\ 0 & 0 & 31 & 0 & 0 \\ 33 & 0 & 14 & 6 & 22 \\ 8 & 0 & 10 & 32 & 35 \end{bmatrix}$$

with 40 fixed points

$$g_4 = \begin{bmatrix} 31 & 0 & 36 & 14 & 28 \\ 18 & 32 & 33 & 23 & 14 \\ 0 & 3 & 32 & 17 & 27 \\ 14 & 27 & 14 & 33 & 14 \\ 7 & 17 & 23 & 36 & 33 \end{bmatrix}$$

with 40 fixed points

$$g_5 = \begin{bmatrix} 27 & 0 & 27 & 36 & 36 \\ 32 & 10 & 13 & 9 & 28 \\ 0 & 31 & 10 & 3 & 20 \\ 18 & 20 & 28 & 36 & 33 \\ 18 & 3 & 9 & 18 & 36 \end{bmatrix}$$

with 38 fixed points

### 3.7 Isomorphism Type 6

Stabilizer has order 72

Plane intersection type is  $5^{12} 4^{270} 3^{7236}$

Plane invariant is too big (12 planes)

$\rightarrow$	$12_1$	$\downarrow$	$12_1$
$2_0$	12	$2_0$	2
$36_2$	1	$36_2$	3

$$C_0 = \{0, 3\}_2$$

$$C_1 = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\}_{12}$$

$$C_2 = \{1, 2, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37\}_{36}$$

$\rightarrow$	$12_1$	$270_2$
$2_0$	12	0
$36_3$	1	30
$\downarrow$	$12_1$	$270_2$
$2_0$	2	0
$36_3$	3	4

$$C_0 = \{0, 3\}_2$$

$$C_1 = \{9, 95, 150, 155, 165, 183, 187, 218, 250, 251, 266, 281\}_{12}$$

$$C_2 = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43\}_{36}$$

$$C_3 = \{1, 2, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37\}_{36}$$

Column cell 1:

Column cell 2:

Order of the group that is induced on the object is 72

Number of ancestors on 5-sets is 7478.

Number of orbits on 5-sets is 7061.

With 2 orbits on the object

Orbit lengths: 2, 36

The points by ranks:

$i$	Rank	$i$	Rank	$i$	Rank	$i$	Rank
0	0	10	16327	20	28609	30	45341
1	1	11	28901	21	32998	31	42234
2	184	12	26133	22	26080	32	51880
3	187	13	47506	23	19349	33	17927
4	194	14	36992	24	40551	34	24092
5	10010	15	28402	25	8640	35	49304
6	39909	16	34880	26	14474	36	11176
7	26701	17	8134	27	27620	37	13501
8	39034	18	28303	28	31131		
9	31172	19	9481	29	26832		

The points:

$$P_0 = (0, 1, 0, 0, 0)P_1 = (0, 0, 1, 0, 0)P_2 = (0, 1, 18, 36, 18)P_3 = (0, 1, 15, 9, 23)$$

$$P_4 = (0, 1, 24, 10, 5)P_5 = (1, 30, 18, 5, 25)P_6 = (1, 12, 35, 29, 11)P_7 = (1, 16, 32, 6, 7)$$

$$P_8 = (1, 20, 16, 16, 10)P_9 = (1, 28, 23, 13, 13)P_{10} = (1, 35, 7, 30, 14)P_{11} = (1, 17, 10, 30, 35)$$

$$P_{12} = (1, 6, 21, 3, 7)P_{13} = (1, 7, 2, 23, 9)P_{14} = (1, 34, 24, 36, 3)P_{15} = (1, 26, 6, 23, 35)$$

$$P_{16} = (1, 7, 23, 11, 29)P_{17} = (1, 7, 6, 25, 19)P_{18} = (1, 24, 28, 22, 35)P_{19} = (1, 6, 26, 10, 25)$$

$$P_{20} = (1, 12, 32, 26, 35)P_{21} = (1, 34, 2, 31, 30)P_{22} = (1, 34, 20, 19, 7)P_{23} = (1, 28, 8, 4, 27)$$

$$P_{24} = (1, 2, 34, 24, 11)P_{25} = (1, 35, 9, 34, 19)P_{26} = (1, 25, 18, 25, 16)P_{27} = (1, 36, 15, 16, 24)$$

$$\begin{aligned}
P_{28} &= (1, 3, 17, 33, 13) P_{29} = (1, 19, 33, 16, 7) P_{30} = (1, 3, 8, 2, 6) P_{31} = (1, 24, 25, 35, 23) \\
P_{32} &= (1, 31, 1, 32, 36) P_{33} = (1, 25, 22, 36, 33) P_{34} = (1, 34, 15, 24, 8) P_{35} = (1, 12, 24, 16, 12) \\
P_{36} &= (1, 1, 20, 27, 28) P_{37} = (1, 32, 12, 21, 31)
\end{aligned}$$

Stabilizer of order 72 is generated by:

$$g_1 = \begin{bmatrix} 26 & 0 & 0 & 0 & 0 \\ 0 & 10 & 0 & 0 & 0 \\ 0 & 17 & 1 & 22 & 11 \\ 0 & 10 & 0 & 26 & 0 \\ 0 & 20 & 0 & 0 & 26 \end{bmatrix}$$

with 40 fixed points

$$g_2 = \begin{bmatrix} 15 & 30 & 0 & 35 & 25 \\ 0 & 2 & 0 & 0 & 0 \\ 29 & 33 & 32 & 20 & 18 \\ 14 & 7 & 0 & 2 & 13 \\ 11 & 6 & 0 & 18 & 20 \end{bmatrix}$$

with 4 fixed points

$$g_3 = \begin{bmatrix} 4 & 15 & 0 & 35 & 13 \\ 0 & 32 & 0 & 0 & 0 \\ 11 & 33 & 2 & 30 & 32 \\ 12 & 4 & 0 & 35 & 35 \\ 1 & 11 & 0 & 19 & 35 \end{bmatrix}$$

with 4 fixed points

$$g_4 = \begin{bmatrix} 4 & 0 & 0 & 20 & 27 \\ 0 & 26 & 20 & 12 & 6 \\ 0 & 22 & 26 & 15 & 26 \\ 32 & 26 & 6 & 28 & 16 \\ 10 & 15 & 12 & 27 & 28 \end{bmatrix}$$

with 40 fixed points

# Chapter 4

## The BLT-Sets in Numeric Form

0, 1, 184, 185, 186, 203, 188, 202, 219, 217, 189, 191, 187, 193, 196, 205, 206, 212, 215, 190, 192, 194, 195, 197, 198, 199, 200, 201, 204, 207, 208, 209, 210, 211, 213, 214, 216, 218  
0, 1, 184, 185, 186, 203, 188, 202, 219, 217, 189, 191, 187, 193, 196, 205, 206, 212, 215, 37558, 8639, 37417, 19559, 13531, 44012, 36359, 29138, 19058, 42031, 16130, 35865, 29990, 18571, 14737, 19485, 48331, 9992, 44759  
0, 1, 184, 185, 188, 7371, 32403, 21678, 11001, 37129, 27018, 17497, 50059, 14893, 38973, 15118, 24505, 7356, 23594, 12873, 35650, 39427, 36907, 31731, 44657, 38816, 11192, 6869, 42680, 12224, 27514, 28003, 24596, 41322, 16159, 12866, 42488, 14245  
0, 1, 184, 185, 295, 6849, 26689, 18223, 30408, 19166, 50998, 17296, 44268, 49507, 43060, 12883, 30901, 13652, 46338, 27449, 48933, 43061, 27664, 46255, 39343, 40225, 47523, 7501, 30079, 18617, 32677, 12761, 50344, 47806, 12866, 39747, 917, 28764  
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19, 0, 0, 24, 25, 0, 31, 0, 0, 0, 0, 34, 31, 1, 19, 6, 19, 0, 31, 6, 25, 1, 0, 24, 31,
33, 0, 0, 8, 33, 0, 13, 0, 0, 0, 0, 7, 13, 15, 26, 35, 26, 0, 14, 5, 4, 15, 0, 20, 14,
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