

## Homework 6

Due Friday, March 29 at the beginning of class

**Reading.** Chapters 5 and 6

**Remark.** Make grammatically correct sentences by adding in just a few English words.

**Problems.**

1. Write the element  $(1246)(45)(236)(1892673)(89) \in S_9$  in disjoint cycle form.
2. Let  $\alpha = (13)(2345)(28)(179825) \in S_9$ . Write  $\alpha^{-1} \in S_9$  in disjoint cycle form. Check that your answer is correct by computing  $\alpha\alpha^{-1}$  and  $\alpha^{-1}\alpha$ .  
*Hint: Does it help to first write  $\alpha$  in disjoint cycle form?*
3. Write the element  $\beta = (15246)(347)(19382657) \in S_9$  as a product of (not necessarily disjoint) 2-cycles. Is  $\beta$  an element of the alternating group  $A_9$ ?
4. Prove that the group  $S_n$  of permutations of  $\{1, 2, 3, \dots, n-1, n\}$  has  $n! = n \cdot (n-1) \cdot (n-2) \cdots 3 \cdot 2 \cdot 1$  elements. In other words, prove that there are  $n!$  permutations of the set  $\{1, 2, \dots, n\}$ .  
*Hint: Recall that a permutation of  $\{1, 2, \dots, n\}$  is a bijective function  $f: \{1, 2, \dots, n\} \rightarrow \{1, 2, \dots, n\}$ .*