

HW 4
Math 261

Please see the course syllabus for details on how to turn in your homework assignments.

1. (5 pts.) TRUE OR FALSE

(a) Let $x = 3, y = 4, z = 5t$, and $f(x, y, z)$ be a function from \mathbb{R}^3 to \mathbb{R} . Then $\frac{\partial f}{\partial t} = \frac{\partial f}{\partial z}$.

(b) Let $x = 3, y = 4, z = 5t$, and $f(x, y, z)$ be a function from \mathbb{R}^3 to \mathbb{R} . Then $\frac{\partial f}{\partial t} = 5 \frac{\partial f}{\partial z}$.

(c) Let $x = 3, y = 4, z = 5t$, and $f(x, y, z)$ be a function from \mathbb{R}^3 to \mathbb{R} . Then $\frac{\partial f}{\partial t} = 1/5 \frac{\partial f}{\partial z}$.

(d) Let $h(x, y)$ be a function from \mathbb{R}^2 to \mathbb{R} and P a point in the domain of h . It is possible that the directional derivative of h at P is equal to 1 for every direction vector.

(e) Let $h(x, y)$ be a function from \mathbb{R}^2 to \mathbb{R} and P a point in the domain of h . It is possible that the directional derivative of h at P is equal to 0 for every direction vector.

2. (3 pts.) Suppose function $f(x, y)$ depends on variables x and y , which are themselves functions of variables α, β , and γ (i.e., $x = x(\alpha, \beta, \gamma)$ and $y = y(\alpha, \beta, \gamma)$). Fill in the blanks for the chain rule to compute $\frac{\partial f}{\partial \beta}$:

$$\frac{\partial f}{\partial \beta} = \frac{\partial \square}{\partial \square} \frac{\partial \square}{\partial \square} + \frac{\partial \square}{\partial \square} \frac{\partial \square}{\partial \square}$$

3. (3 pts.) Let

$$g(u, v) = u^2 + v^3,$$

$$u(t) = \cos(t),$$

$$v(t) = \ln(t).$$

Compute $\frac{dg}{dt}$. (Please use only the variable t in your response, but do not bother multiplying everything out.)

4. (3 pts.) Suppose z is a function of x and y and that $x^2 z^2 + y \sin(z) = 1$. Find $\frac{\partial z}{\partial x}$.

5. (3 pts.) Find the derivative of $f(x, y) = xy - y^2$ at point $(1, 2)$ in the direction of $\mathbf{v} = \langle 3, 4 \rangle$. Please simplify your answer to a number. (Notice that \mathbf{v} is not a unit vector!)
6. (3 pts.) Find a direction vector \mathbf{v} such that the derivative of $f(x, y) = xy - y^2$ at point $(1, 2)$ in the direction of \mathbf{v} is equal to 0.