

1 BLT set 3 over GF(41)

Points on the quadric $x_0^2 + x_1x_2 + x_3x_4$:

$$P_1 = (0, 1, 0, 0, 0)$$

$$P_2 = (0, 0, 1, 0, 0)$$

$$P_3 = (0, 1, 27, 40, 27)$$

$$P_4 = (0, 1, 17, 20, 34)$$

$$P_5 = (0, 1, 6, 8, 30)$$

$$P_6 = (0, 1, 22, 27, 25)$$

$$P_7 = (0, 1, 38, 14, 9)$$

$$P_8 = (1, 23, 6, 15, 29)$$

$$P_9 = (1, 25, 6, 20, 15)$$

$$P_{10} = (1, 17, 10, 34, 1)$$

$$P_{11} = (1, 21, 6, 2, 39)$$

$$P_{12} = (1, 39, 11, 20, 40)$$

$$P_{13} = (1, 37, 24, 28, 40)$$

$$P_{14} = (1, 24, 18, 36, 21)$$

$$P_{15} = (1, 18, 6, 28, 21)$$

$$P_{16} = (1, 9, 35, 24, 21)$$

$$P_{17} = (1, 23, 17, 40, 23)$$

$$P_{18} = (1, 34, 36, 39, 18)$$

$$P_{19} = (1, 19, 21, 30, 14)$$

$$P_{20} = (1, 38, 39, 38, 16)$$

$$P_{21} = (1, 35, 18, 8, 39)$$

$$P_{22} = (1, 14, 25, 31, 31)$$

$$P_{23} = (1, 17, 4, 14, 39)$$

$$P_{24} = (1, 19, 8, 26, 2)$$

$$P_{25} = (1, 30, 9, 37, 37)$$

$$P_{26} = (1, 32, 19, 19, 37)$$

$$P_{27} = (1, 10, 17, 6, 33)$$

$$P_{28} = (1, 33, 27, 7, 19)$$

$$P_{29} = (1, 30, 36, 21, 11)$$

$$P_{30} = (1, 38, 21, 24, 6)$$

$$P_{31} = (1, 39, 6, 5, 35)$$

$$P_{32} = (1, 32, 3, 35, 23)$$

$$P_{33} = (1, 4, 12, 20, 16)$$

$$P_{34} = (1, 38, 21, 37, 5)$$

$$P_{35} = (1, 6, 32, 27, 5)$$

$$P_{36} = (1, 20, 24, 6, 36)$$

$$P_{37} = (1, 31, 17, 8, 16)$$

$$P_{38} = (1, 17, 37, 39, 28)$$

$$P_{39} = (1, 31, 35, 16, 9)$$

$$P_{40} = (1, 28, 9, 24, 39)$$

$$P_{41} = (1, 28, 1, 26, 32)$$

$$P_{42} = (1, 33, 24, 17, 4)$$

Stabilizer of order 2 is generated by:

$$g_1 = \begin{pmatrix} 3 & 33 & 29 & 20 & 3 \\ 35 & 15 & 5 & 37 & 38 \\ 37 & 32 & 15 & 13 & 6 \\ 22 & 6 & 38 & 24 & 25 \\ 10 & 13 & 37 & 39 & 24 \end{pmatrix}$$

Induced action on the BLT-set:

The induced group has order 2 and is generated by:

$$g_1 = (1, 15)(2, 28)(3, 42)(4, 20)(5, 21)(6, 31)(7, 11)(8, 18)(9, 35)(10, 26)(12, 23)(13, 19)(14, 39)(16, 37)(17, 30)(22, 27)(24, 32)(25, 34)(29, 36)(33, 40)(38, 41)$$

Kernel has order 1 and is generated by:

There are 21 orbits on the BLT set.

The orbit length are $[2^{21}]$

The orbits are:

$$O_0 = \{1, 15\} \text{ (length 2)}$$

$$O_1 = \{2, 28\} \text{ (length 2)}$$

$$O_2 = \{3, 42\} \text{ (length 2)}$$

$$O_3 = \{4, 20\} \text{ (length 2)}$$

$$O_4 = \{5, 21\} \text{ (length 2)}$$

$$O_5 = \{6, 31\} \text{ (length 2)}$$

$$O_6 = \{7, 11\} \text{ (length 2)}$$

$$O_7 = \{8, 18\} \text{ (length 2)}$$

$$O_8 = \{9, 35\} \text{ (length 2)}$$

$$O_9 = \{10, 26\} \text{ (length 2)}$$

$$O_{10} = \{12, 23\} \text{ (length 2)}$$

$$O_{11} = \{13, 19\} \text{ (length 2)}$$

$$O_{12} = \{14, 39\} \text{ (length 2)}$$

$$O_{13} = \{16, 37\} \text{ (length 2)}$$

$$O_{14} = \{17, 30\} \text{ (length 2)}$$

$$O_{15} = \{22, 27\} \text{ (length 2)}$$

$$O_{16} = \{24, 32\} \text{ (length 2)}$$

$$O_{17} = \{25, 34\} \text{ (length 2)}$$

$$O_{18} = \{29, 36\} \text{ (length 2)}$$

$$O_{19} = \{33, 40\} \text{ (length 2)}$$

$$O_{20} = \{38, 41\} \text{ (length 2)}$$

The actions induced on the orbits are:

Induced action on orbit $O_0 = \{1, 15\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_1 = \{2, 28\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_2 = \{3, 42\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_3 = \{4, 20\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_4 = \{5, 21\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_5 = \{6, 31\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_6 = \{7, 11\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_7 = \{8, 18\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_8 = \{9, 35\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_9 = \{10, 26\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_{10} = \{12, 23\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_{11} = \{13, 19\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_{12} = \{14, 39\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_{13} = \{16, 37\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_{14} = \{17, 30\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_{15} = \{22, 27\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_{16} = \{24, 32\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_{17} = \{25, 34\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_{18} = \{29, 36\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_{19} = \{33, 40\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by:

Induced action on orbit $O_{20} = \{38, 41\}$ (length 2)

The induced group has order 2 and is generated by:

$$g_1 = (1, 2)$$

Kernel has order 1 and is generated by: