

# 1 BLT set 1 over GF(31)

Points on the quadric  $x_0^2 + x_1x_2 + x_3x_4$ :

$$P_1 = (0, 1, 0, 0, 0)$$

$$P_2 = (0, 0, 1, 0, 0)$$

$$P_3 = (0, 1, 10, 30, 10)$$

$$P_4 = (0, 1, 18, 15, 5)$$

$$P_5 = (0, 1, 8, 10, 24)$$

$$P_6 = (0, 1, 20, 23, 18)$$

$$P_7 = (0, 1, 28, 3, 1)$$

$$P_8 = (0, 1, 2, 26, 19)$$

$$P_9 = (0, 1, 19, 6, 2)$$

$$P_{10} = (0, 1, 10, 1, 21)$$

$$P_{11} = (0, 1, 25, 7, 23)$$

$$P_{12} = (0, 1, 14, 19, 27)$$

$$P_{13} = (0, 1, 2, 5, 12)$$

$$P_{14} = (0, 1, 18, 16, 26)$$

$$P_{15} = (0, 1, 1, 20, 17)$$

$$P_{16} = (0, 1, 14, 12, 4)$$

$$P_{17} = (0, 1, 25, 24, 8)$$

$$P_{18} = (0, 1, 19, 25, 29)$$

$$P_{19} = (0, 1, 9, 2, 11)$$

$$P_{20} = (0, 1, 7, 17, 16)$$

$$P_{21} = (0, 1, 4, 22, 28)$$

$$P_{22} = (0, 1, 8, 21, 7)$$

$$P_{23} = (0, 1, 1, 11, 14)$$

$$P_{24} = (0, 1, 28, 28, 30)$$

$$P_{25} = (0, 1, 5, 27, 9)$$

$$P_{26} = (0, 1, 20, 8, 13)$$

$$P_{27} = (0, 1, 16, 18, 6)$$

$$P_{28} = (0, 1, 5, 4, 22)$$

$$P_{29} = (0, 1, 7, 14, 15)$$

$$P_{30} = (0, 1, 4, 9, 3)$$

$$P_{31} = (0, 1, 16, 13, 25)$$

$$P_{32} = (0, 1, 9, 29, 20)$$

Stabilizer of order 1904640 is generated by:

$$g_1 = \begin{pmatrix} 21 & 0 & 0 & 24 & 23 \\ 0 & 30 & 0 & 0 & 0 \\ 0 & 17 & 30 & 19 & 27 \\ 4 & 27 & 0 & 11 & 7 \\ 19 & 19 & 0 & 1 & 11 \end{pmatrix}$$

$$g_2 = \begin{pmatrix} 0 & 0 & 0 & 11 & 17 \\ 0 & 30 & 0 & 0 & 0 \\ 0 & 0 & 30 & 0 & 0 \\ 24 & 0 & 0 & 15 & 5 \\ 21 & 0 & 0 & 14 & 15 \end{pmatrix}$$

$$g_3 = \begin{pmatrix} 24 & 0 & 0 & 19 & 4 \\ 0 & 30 & 0 & 0 & 0 \\ 0 & 0 & 30 & 0 & 0 \\ 2 & 0 & 0 & 3 & 9 \\ 25 & 0 & 0 & 19 & 3 \end{pmatrix}$$

$$g_4 = \begin{pmatrix} 7 & 0 & 0 & 19 & 4 \\ 0 & 2 & 5 & 30 & 10 \\ 0 & 8 & 2 & 18 & 6 \\ 29 & 6 & 10 & 1 & 29 \\ 6 & 18 & 30 & 13 & 1 \end{pmatrix}$$

$$g_5 = \begin{pmatrix} 5 & 0 & 0 & 17 & 15 \\ 0 & 30 & 0 & 0 & 0 \\ 0 & 0 & 30 & 0 & 0 \\ 23 & 0 & 0 & 28 & 11 \\ 24 & 0 & 0 & 6 & 28 \end{pmatrix}$$

$$g_6 = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 30 & 0 & 0 & 0 \\ 0 & 0 & 30 & 0 & 0 \\ 0 & 0 & 0 & 30 & 0 \\ 0 & 0 & 0 & 0 & 30 \end{pmatrix}$$

$$g_7 = \begin{pmatrix} 2 & 0 & 0 & 3 & 30 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 4 & 1 & 9 & 3 \\ 16 & 3 & 0 & 16 & 15 \\ 14 & 9 & 0 & 11 & 16 \end{pmatrix}$$

$$g_8 = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 5 & 0 & 0 & 0 \\ 0 & 0 & 25 & 0 & 0 \\ 0 & 0 & 0 & 30 & 0 \\ 0 & 0 & 0 & 0 & 30 \end{pmatrix}$$

$$g_9 = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 21 & 0 & 0 & 0 \\ 0 & 0 & 3 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

Induced action on the BLT-set:

The induced group has order 29760 and is generated by:

$$g_1 = (2, 6)(3, 5)(7, 8)(9, 10)(11, 12)(13, 14)(15, 16)(17, 18)(19, 20)(21, 22)(23, 24)(25, 26)(27,$$

28)(29, 30)(31, 32)

$g_2 = \text{id}$

$g_3 = \text{id}$

$g_4 = (1, 4)(2, 5)(3, 6)(7, 8)(9, 11)(10, 12)(13, 15)(14, 16)(17, 19)(18, 20)(21, 23)(22, 24)(25, 27)(26, 28)(29, 31)(30, 32)$

$g_5 = \text{id}$

$g_6 = \text{id}$

$g_7 = (2, 5)(3, 4)(6, 10)(7, 30)(8, 17)(9, 14)(11, 27)(12, 24)(13, 22)(16, 32)(18, 25)(19, 31)(20, 23)(21, 26)(28, 29)$

$g_8 = (3, 18, 8, 10, 9, 13)(4, 24, 31, 14, 7, 27)(5, 32, 12, 22, 19, 16)(6, 29, 21, 26, 20, 30)(11, 23, 28, 17, 15, 25)$

$g_9 = (3, 24, 21, 28, 16, 13, 4, 29, 23, 19, 9, 27, 6, 11, 22, 10, 7, 30, 25, 12, 8, 14, 20, 15, 32, 18, 31, 26, 17, 5)$

Kernel has order 64 and is generated by:

$$b_1 = \begin{pmatrix} 0 & 0 & 0 & 11 & 17 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 24 & 0 & 0 & 16 & 26 \\ 21 & 0 & 0 & 17 & 16 \end{pmatrix}$$

$$b_2 = \begin{pmatrix} 5 & 0 & 0 & 14 & 16 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 23 & 0 & 0 & 3 & 20 \\ 24 & 0 & 0 & 25 & 3 \end{pmatrix}$$

$$b_3 = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$b_4 = \begin{pmatrix} 30 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

The kernel has 993 orbits on the quadric.

The orbit length are  $[32^{961}, 1^{32}]$

Induced action on orbit  $O_2 = \{3, 64, 2855, 2916, 2977, 3038, 3099, 3160, 3221, 3282, 3343, 3404, 3465, 3526, 3587, 3648, 3709, 3770, 3831, 3892, 3953, 4014, 4075, 4136, 4197, 4258, 4319, 4380, 4441, 4502, 4563, 4624, 4685, 4746, 4807, 4868, 4929, 4990, 5051, 5112, 5173, 5234, 5295, 5356, 5417, 5478, 5539, 5600, 5661, 5722, 5783, 5844, 5905, 5966, 6027, 6088, 6149, 6210, 6271, 6332, 6393, 6454, 6515, 6576, 6637, 6698, 6759, 6820, 6881, 6942, 7003, 7064, 7125, 7186, 7247, 7308, 7369, 7430, 7491, 7552, 7613, 7674, 7735, 7796, 7857, 7918, 7979, 8040, 8101, 8162, 8223, 8284, 8345, 8406, 8467, 8528, 8589, 8650, 8711, 8772, 8833, 8894, 8955, 9016, 9077, 9138, 9199, 9260, 9321, 9382, 9443, 9504, 9565, 9626, 9687, 9748, 9809, 9870, 9931, 9992, 10000\}$   
(length 32)

The induced group has order 64 and is generated by:

$$g_1 = (1, 22)(2, 13)(3, 6)(4, 12)(5, 26)(7, 10)(8, 18)(9, 32)(11, 31)(14, 15)(16, 23)(19, 24)(20, 25)(21, 28)(29, 30)$$

$$g_2 = (1, 14, 12, 9, 18, 30, 19, 7, 13, 20, 31, 3, 27, 6, 11, 25, 2, 10, 24, 29, 8, 32, 4, 15, 22, 28, 16, 5, 17, 26, 23, 21)$$

$$g_3 = \text{id}$$

$$g_4 = (3, 32)(4, 31)(5, 30)(6, 29)(7, 28)(8, 27)(9, 26)(10, 25)(11, 24)(12, 23)(13, 22)(14, 21)(15, 20)(16, 19)(17, 18)$$

Kernel has order 1 and is generated by:

There are 1 orbits on the BLT set.

The orbit length are [32]

The orbits are:

$O_0 = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32\}$   
(length 32)