## Homework 2

Due: Friday, September 1

1. $[B C] 4.4,4.5$.
2. $[B C] 5.1,5.2,5.3$.
3. (a) $[B C] 5.11$.
(b) Describe all $z$ for which $\bar{z}=i z$. Prove that your answer is correct.
4. [BC] 5.14
5. [BC] 7.1, 7.6.
6. Assume $\alpha$ and $\beta$ are real numbers.
(a) Write each of $e^{i \alpha}, e^{i \beta}$, and $e^{i(\alpha+\beta)}$ in rectangular coordinates.
(b) Prove the following formulas from trigonometry, without using trigonometry.

$$
\begin{aligned}
\cos (\alpha+\beta) & =\cos (\alpha) \cos (\beta)-\sin (\alpha) \sin (\beta) \\
\sin (\alpha+\beta) & =\sin (\alpha) \cos (\beta)+\sin (\beta) \cos (\alpha)
\end{aligned}
$$

(HINT: $\left.e^{i \alpha} e^{i \beta}=e^{i(\alpha+\beta)}.\right)$

