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Homework 12  
Due: Friday, November 17

1. [BC] 54.7
2. Suppose a function  $f(z)$  is represented in a neighborhood of 0 by the power series

$$f(z) = \sum_{n \geq 0} a_n z^n.$$

- (a) Write down the Maclaurin series for  $f'(z)$ .
  - (b) Prove that if  $f(z) = f'(z)$  then  $a_{n+1} = \frac{1}{n+1} a_n$ .
  - (c) Let  $\lambda$  be a nonzero complex number. Suppose that  $f'(z) = \lambda f(z)$ . Give a formula for  $a_n$  in terms of  $a_0$ .
3. [BC] 60.1.
  4. [BC] 60.4. (HINT: Find a series representation for  $\exp(z) - 1$ , and then for  $(\exp(z) - 1)/z$ .)