
Homework 10
Due: Friday, November 4

1. [F]2.7.2
2. [F]2.8.1
3. [F]2.8.4
4. [F]2.8.5
5. Consider the function $f(x, y) = (x^2 - y)(2x^2 - y) = y^2 - 3x^2y + 2x^4$. Note that $f(0, 0) = 0$.

(a) Describe the sets

$$S = \{(x, y) : f(x, y) > 0\}$$

$$T = \{(x, y) : f(x, y) < 0\}$$

- (b) Show that for every straight line through the origin, $f > 0$ for some interval around the origin.
- (c) Nonetheless, show that every open neighborhood of the origin contains points (x, y) such that $f(x, y) < 0$.