Mathematics Seminar



Rocky Mountain Algebraic Combinatorics Seminar

An introduction to topological combinatorics

Henry Adams Colorado State University

The chromatic number of a graph is the number of vertex colors needed so that adjacent vertices have different colors. In 1955, Kneser made a conjecture about the chromatic number of a certain famil y of graphs (now called Kneser graphs). This conjecture remained unproven for 23 years until Lovász gave a topological proof in 1978. This marked the beginning of a new field, topological combinato rics, in which tools from algebraic topology are used to solve problems in combinatorics. In the first part of my talk, I will share a proof of Kneser's conjecture.

The second part of my talk will fast-forward to the present day. The Gromov-Hausdorff distance is a notion of dissimilarity between two metric spaces. It is an important tool in geometry, but notori ously difficult to compute. I will show how topological combinatorics provides (potentially tight) lower bounds on the Gromov-Hausdorff distance between unit spheres of different dimensions. This is joint work in a polymath-style project with many people who are currently or formerly at Colorado State, Ohio State, Carnegie Mellon, or Freie Universität Berlin.

Notes for first part: https://www.math.colostate.edu/ adams/talks/KneserConjecture.pdf Notes for second part: https://www.math.colostate.edu/ adams/talks/GH-BU-VR-3.pdf

Weber 223 4–6 pm, Friday, Sept 16, 2022 (Refreshments 3:30–4 pm) Colorado State University 4 pm, Friday, Sept 16, 2022

This is a joint Denver U / UC Boulder / U of Wyoming / CSU seminar that meets biweekly. Anyone interested is welcome to join us at a local restaurant for dinner after the talks.



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